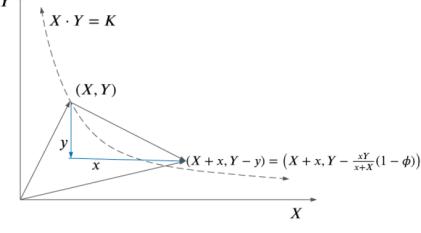


x	X	Slip-Based Fee (used by Sifchain)	Flat-Fee of 0.3% (used by Uniswap)	Fee Savings with Sifchain		x: Amount of token X added to pool by swapper
1	100000	0.000100%	0.30%	0.30%		
100	100000	0.01%	0.30%	0.29%		
1000	100000	0.10%	0.30%	0.20%		
10000	100000	0.99%	0.30%	-0.69%		
						When swappers are swapping low volume relative to the pool, they pay less in fees than on Uniswap. When they are swapping high volume relative to the pool, they pay more in fees than on Uniswap (negative fee savings implies the fee on Sifchain is higher than on Uniswap).
						Swappers benefit under normal conditions while poolers benefit during periods of high volatility when swap price will pay more in fees to change their position. In a single market, swap fee is a positive sum of fees under the Sifchain swap fee and the Uniswap fee. Further research - https://github.com/thorchain/Resources/blob/master/Audits/THORChain-Gauntlet-CLPReport-Nov2020.pdf
100000	100000	9.09%	0.30%	-8.79%		
1000000	100000	50.00%	0.30%	49.70%		
10000000	100000	99.91%	0.30%	-90.61%		
100000000	100000	99.91%	0.30%	-98.71%		
1	100000	0.00%	0.30%	0.30%		
10	100000	0.00%	0.30%	0.30%		
100	100000	0.01%	0.30%	0.29%		
1000	100000	0.10%	0.30%	0.20%		
10000	100000	0.99%	0.30%	-0.69%		
100000	100000	9.09%	0.30%	-8.79%		
1000000	100000	50.00%	0.30%	49.70%		
10000000	100000	99.91%	0.30%	-90.61%		
100000000	100000	99.91%	0.30%	-98.71%		
1	500000	0.00%	0.30%	0.30%		
10	500000	0.00%	0.30%	0.30%		
100	500000	0.00%	0.30%	0.30%		
1000	500000	0.02%	0.30%	0.28%		
10000	500000	0.20%	0.30%	0.10%		
100000	500000	1.96%	0.30%	-1.66%		
1000000	500000	16.67%	0.30%	-16.37%		
10000000	500000	66.67%	0.30%	-66.37%		
100000000	500000	95.24%	0.30%	-66.37%		
1	500000	0.00%	0.30%	-94.94%		
10	500000	0.00%	0.30%	0.30%		
100	500000	0.00%	0.30%	0.30%		
1000	500000	0.02%	0.30%	0.28%		
10000	500000	0.20%	0.30%	0.10%		
100000	500000	1.96%	0.30%	-1.66%		
1000000	500000	16.67%	0.30%	-16.37%		
10000000	500000	66.67%	0.30%	-66.37%		
100000000	500000	95.24%	0.30%	-66.37%		
1	50000	0.00%	0.30%	-94.94%		
10	50000	0.02%	0.30%	0.28%		
100	50000	0.20%	0.30%	0.10%		
1000	50000	1.96%	0.30%	-1.66%		
10000	50000	16.67%	0.30%	-16.37%		
100000	50000	66.67%	0.30%	-66.37%		
1000000	50000	95.24%	0.30%	-66.37%		
10000000	50000	99.50%	0.30%	-99.20%		
100000000	50000	99.50%	0.30%	-99.65%		
1	50000	0.00%	0.30%	0.30%		
10	50000	0.02%	0.30%	0.28%		
100	50000	0.20%	0.30%	0.10%		
1000	50000	1.96%	0.30%	-1.66%		
10000	50000	16.67%	0.30%	-16.37%		
100000	50000	66.67%	0.30%	-66.37%		
1000000	50000	95.24%	0.30%	-66.37%		
10000000	50000	99.50%	0.30%	-99.20%		
100000000	50000	99.50%	0.30%	-99.65%		
1	500	0.00%	0.30%	0.30%		
10	500	0.20%	0.30%	0.10%		
100	500	1.96%	0.30%	-1.66%		
1000	500	16.67%	0.30%	-16.37%		
10000	500	66.67%	0.30%	-66.37%		
100000	500	95.24%	0.30%	-66.37%		
1000000	500	99.50%	0.30%	-99.20%		
10000000	500	99.50%	0.30%	-99.65%		
1	500	0.00%	0.30%	0.30%		
10	500	0.00%	0.30%	0.30%		
100	500	0.01%	0.30%	0.29%		
1000	500	0.10%	0.30%	0.20%		
10000	500	0.99%	0.30%	-0.69%		
100000	500	9.09%	0.30%	-8.79%		
1000000	500	50.00%	0.30%	-49.70%		
10000000	500	90.91%	0.30%	-90.61%		
100000000	500	99.91%	0.30%	-98.71%		
1	100000	0.00%	0.30%	0.30%		
10	100000	0.00%	0.30%	0.30%		
100	100000	0.01%	0.30%	0.29%		
1000	100000	0.10%	0.30%	0.20%		
10000	100000	0.99%	0.30%	-0.69%		
100000	100000	9.09%	0.30%	-8.79%		
1000000	100000	50.00%	0.30%	-49.70%		
10000000	100000	90.91%	0.30%	-90.61%		
100000000	100000	99.91%	0.30%	-98.71%		
1	1000000	0.00%	0.30%	0.30%		
10	1000000	0.00%	0.30%	0.30%		
100	1000000	0.01%	0.30%	0.29%		
1000	1000000	0.10%	0.30%	0.20%		
10000	1000000	0.99%	0.30%	-0.69%		
100000	1000000	9.09%	0.30%	-8.79%		
1000000	1000000	50.00%	0.30%	-49.70%		
10000000	1000000	90.91%	0.30%	-90.61%		
100000000	1000000	99.91%	0.30%	-98.71%		
4.99999	1000000	0.00%	0.30%	0.30%		
499.900015	1000000	0.05%	0.30%	0.25%		
4990.01498	1000000	0.50%	0.30%	-0.20%		
49014.80247	1000000	4.67%	0.30%	-4.37%		
413223.1405	1000000	29.24%	0.30%	-28.94%		
1250000	1000000	55.56%	0.30%	-55.26%		
413223.1405	1000000	29.24%	0.30%	-28.94%		
49014.80247	1000000	4.67%	0.30%	-4.37%		
4.99999	5000000	0.00%	0.30%	0.30%		
49.99900001	5000000	0.00%	0.30%	0.30%		

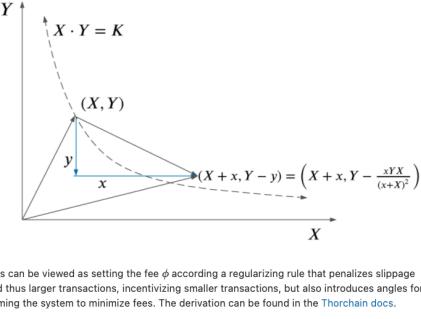
Fee Derivation from <https://hackmd.io/bVK2LSYjRTyeNC0hVt2hg>

Constant Product Market Maker: Flat Fee



There is an implementation of uniswap in cadCAD and an overview with video of the model.

Thorchain "Slip fee" (CLP)



This can be viewed as setting the fee ϕ according a regularizing rule that penalizes slippage and thus larger transactions, incentivizing smaller transactions, but also introduces angles for garning the system to minimize fees. The derivation can be found in the [Thorchain docs](#).

Comparing:

$$y_{ff} = \frac{xy}{x+X}(1-\phi)$$

with

$$y_{dp} = \frac{xyX}{(x+X)^2} = \frac{xy}{x+X} \frac{X}{x+X}$$

so

$$(1-\phi) = \frac{X}{x+X} = 1 - \frac{x}{x+X}$$

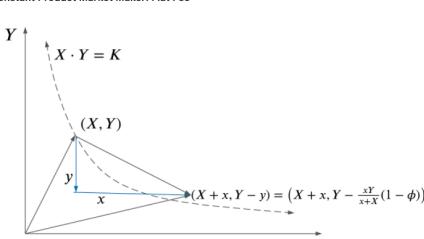
this is simply choosing a functional fee, as

$$\phi = \frac{x}{x+X}$$

499.900015	5000000	0.01%	0.30%	0.29%
4990.01498	5000000	0.10%	0.30%	0.20%
49014.80247	5000000	0.97%	0.30%	-0.67%
413223.1405	5000000	7.63%	0.30%	-7.33%
1250000	5000000	28.00%	0.30%	-19.70%
413223.1405	5000000	7.63%	0.30%	-7.33%
49014.80247	5000000	0.97%	0.30%	-0.67%
0.19999992	1000000	0.00%	0.30%	0.30%
1.999992	1000000	0.00%	0.30%	0.30%
19.99920002	1000000	0.00%	0.30%	0.30%
199.920024	1000000	0.02%	0.30%	0.28%
1992.023936	1000000	0.28%	0.30%	0.10%
19223.37562	1000000	1.89%	0.30%	-1.59%
138888.8889	1000000	12.20%	0.30%	-11.90%
222222.2222	1000000	18.18%	0.30%	-17.88%
45351.47392	1000000	4.34%	0.30%	-4.04%
0.19999992	5000000	0.00%	0.30%	0.30%
1.999992	5000000	0.00%	0.30%	0.30%
19.99920002	5000000	0.00%	0.30%	0.30%
199.920024	5000000	0.00%	0.30%	0.30%
1992.023936	5000000	0.04%	0.30%	0.26%
19223.37562	5000000	0.38%	0.30%	-0.08%
138888.8889	5000000	2.70%	0.30%	-2.40%
222222.2222	5000000	4.26%	0.30%	-3.96%
45351.47392	5000000	0.98%	0.30%	-0.60%
19.99920002	5000000	0.00%	0.30%	0.30%
199.920024	5000000	0.00%	0.30%	0.30%
1992.023936	5000000	0.04%	0.30%	0.26%
19223.37562	5000000	0.38%	0.30%	-0.08%
138888.8889	5000000	2.70%	0.30%	-2.40%
222222.2222	5000000	4.26%	0.30%	-3.96%
45351.47392	5000000	0.98%	0.30%	-0.60%
4950.372516	5000000	0.18%	0.30%	0.20%
499.5003748	5000000	0.01%	0.30%	0.29%
19.99920002	50000	0.04%	0.30%	0.26%
199.920024	50000	0.40%	0.30%	-0.10%
1992.023936	50000	3.83%	0.30%	-3.53%
19223.37562	50000	27.77%	0.30%	-27.47%
138888.8889	50000	73.53%	0.30%	-73.23%
222222.2222	50000	81.63%	0.30%	-81.33%
45351.47392	50000	47.56%	0.30%	-47.26%
4950.372516	50000	9.01%	0.30%	-8.71%
499.5003748	50000	0.99%	0.30%	-0.69%
1992.023936	50000	3.83%	0.30%	-3.53%
19223.37562	50000	27.77%	0.30%	-27.47%
138888.8889	50000	73.53%	0.30%	-73.23%
222222.2222	50000	81.63%	0.30%	-81.33%
45351.47392	50000	47.56%	0.30%	-47.26%
4950.372516	50000	9.01%	0.30%	-8.71%
499.5003748	50000	0.99%	0.30%	-0.69%
49.99500037	50000	0.10%	0.30%	0.20%
4.99995	50000	0.01%	0.30%	0.29%
1992.023936	500	79.94%	0.30%	-79.64%
19223.37562	500	97.46%	0.30%	-97.16%
138888.8889	500	99.64%	0.30%	-99.34%
222222.2222	500	99.78%	0.30%	-99.48%
45351.47392	500	98.91%	0.30%	-98.61%
4950.372516	500	98.83%	0.30%	-90.53%
499.5003748	500	49.98%	0.30%	-49.68%
49.99500037	500	0.09%	0.30%	-8.79%
4.99995	500	0.99%	0.30%	-0.69%
0.004999999	1000000	0.00%	0.30%	0.30%
0.004999999001	1000000	0.00%	0.30%	0.30%
0.0499900015	1000000	0.00%	0.30%	0.30%
0.499001498	1000000	0.00%	0.30%	0.30%
4.901480247	1000000	0.00%	0.30%	0.30%
41.32231405	1000000	0.00%	0.30%	0.30%
125	1000000	0.01%	0.30%	0.29%
41.32231405	1000000	0.00%	0.30%	0.30%
4.901480247	1000000	0.00%	0.30%	0.30%
0.0499999	1000000	0.00%	0.30%	0.30%
0.499990001	1000000	0.00%	0.30%	0.30%
4.99990015	1000000	0.00%	0.30%	0.30%
49.9001498	1000000	0.00%	0.30%	0.30%
490.1480247	1000000	0.05%	0.30%	0.25%
4132.231405	1000000	0.41%	0.30%	-0.11%
12500	1000000	1.23%	0.30%	-0.93%
4132.231405	1000000	0.41%	0.30%	-0.11%
490.1480247	1000000	0.05%	0.30%	0.25%

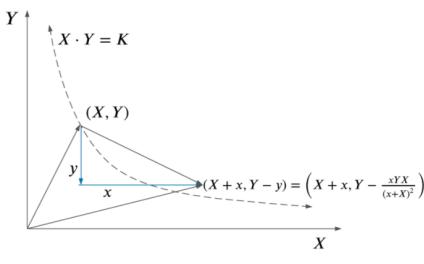
Number of Rowan in swap (x)	Number of Rowan in pool (X)	Number of TKN in pool (Y)	w_x	w_y	Slip Based Swap Fee	Number of TKN received from swap (y)	Percentage increase over equal weight purchasing power
1	1,000,000	1,000,000	0.50000	0.50000	0.000100%	1.00	0.00%
100	1,000,000	1,000,000	0.50000	0.50000	0.01%	99.98	0.00%
1000	1,000,000	1,000,000	0.50000	0.50000	0.10%	998.00	0.00%
10000	1,000,000	1,000,000	0.50000	0.50000	0.99%	9,802.96	0.00%
4000	1,000,000	1,000,000	0.50000	0.50000	0.40%	3,968.19	0.00%
4000	1,000,000	1,000,000	0.60000	0.40000	0.40%	5,946.35	49.85%
4000	1,000,000	1,000,000	0.70000	0.30000	0.40%	9,234.53	132.71%
4000	1,000,000	1,000,000	0.80000	0.20000	0.40%	15,778.16	297.62%
4000	1,000,000	1,000,000	0.90000	0.10000	0.40%	35,149.84	785.79%
4000	1,000,000	1,000,000	0.94000	0.06000	0.40%	60,384.54	1421.71%
4000	1,000,000	1,000,000	0.97000	0.03000	0.40%	120,609.83	2939.42%
4000	1,000,000	1,000,000	0.99000	0.01000	0.40%	325,160.85	8094.18%
4000	1,000,000	1,000,000	0.99900	0.00100	0.40%	977,553.58	24534.74%
4000	10,000,000	10,000,000	0.50000	0.50000	0.04%	3,996.80	0.00%
4000	10,000,000	10,000,000	0.90000	0.10000	0.04%	35,913.74	798.56%
4000	10,000,000	10,000,000	0.99000	0.01000	0.04%	388,030.36	9608.52%
4000	10,000,000	10,000,000	0.99900	0.00100	0.04%	3,292,265.00	82272.48%
4000	10,000,000	10,000,000	0.99990	0.00010	0.04%	9,812,698.67	245413.76%
1000	1,000,000	1,000,000	0.50000	0.50000	0.10%	998.00	0.00%
2000	1,000,000	1,000,000	0.50000	0.50000	0.20%	1,992.02	0.00%
3000	1,000,000	1,000,000	0.50000	0.50000	0.30%	2,982.08	0.00%
4000	1,000,000	1,000,000	0.50000	0.50000	0.40%	3,968.19	0.00%
1000	1,000,000	1,000,000	0.55000	0.45000	0.10%	1,219.65	122.21%
2000	1,000,000	1,000,000	0.55000	0.45000	0.20%	2,434.16	122.20%
3000	1,000,000	1,000,000	0.55000	0.45000	0.30%	3,643.55	122.18%
4000	1,000,000	1,000,000	0.55000	0.45000	0.40%	4,847.86	122.17%
1000	1,000,000	1,000,000	0.60000	0.40000	0.10%	1,496.63	149.96%
2000	1,000,000	1,000,000	0.60000	0.40000	0.20%	2,986.54	149.93%
3000	1,000,000	1,000,000	0.60000	0.40000	0.30%	4,469.77	149.89%
4000	1,000,000	1,000,000	0.60000	0.40000	0.40%	5,946.35	149.85%

x	X	Slip-Based Fee (used by Sifchain)	Flat-Fee of 0.3% (used by Uniswap)	Fee Savings with Sifchain		
1	100000	0.000100%	0.30%	0.30%	x: Amount of token X added to pool by swapper	
100	100000	0.01%	0.30%	0.29%	X: Amount of token X already in the pool	
1000	100000	0.10%	0.30%	0.20%	Slip-Based Fee: The fee paid by swappers and collected by poolers	
10000	100000	0.99%	0.30%	-0.69%		
					When swappers are swapping low volume relative to the pool, they pay less in fees than on Uniswap. When they are swapping high volume relative to the pool, they pay more in fees than on Uniswap (negative fee savings implies the fee on Sifchain is higher than on Uniswap). Swappers benefit under normal conditions while poolers benefit during periods of high volatility when swap price will move in fees to change their position. In a single market, swap fee is proportional to the amount swapped under the Sifchain swap fee than the Uniswap fee. Further research - https://github.com/thorchain/Resources/blob/master/Audits/THORChain-Gauntlet-CLPReport-Nov2020.pdf	
100000	100000	9.09%	0.30%	-8.79%		
1000000	100000	50.00%	0.30%	49.70%		
10000000	100000	99.91%	0.30%	-90.61%		
100000000	100000	99.91%	0.30%	-98.71%		
1	100000	0.00%	0.30%	0.30%		
10	100000	0.00%	0.30%	0.30%		
100	100000	0.01%	0.30%	0.29%		
1000	100000	0.10%	0.30%	0.20%		
10000	100000	0.99%	0.30%	-0.69%		
100000	100000	9.09%	0.30%	-8.79%		
1000000	100000	50.00%	0.30%	49.70%		
10000000	100000	99.91%	0.30%	-90.61%		
100000000	100000	99.91%	0.30%	-98.71%		
1	500000	0.00%	0.30%	0.30%		
10	500000	0.00%	0.30%	0.30%		
100	500000	0.00%	0.30%	0.30%		
1000	500000	0.02%	0.30%	0.28%		
10000	500000	0.20%	0.30%	0.10%		
100000	500000	1.96%	0.30%	-1.66%		
1000000	500000	16.67%	0.30%	-16.37%		
10000000	500000	66.67%	0.30%	-66.37%		
100000000	500000	95.24%	0.30%	-94.94%		
1	500000	0.00%	0.30%	0.30%		
10	500000	0.00%	0.30%	0.30%		
100	500000	0.00%	0.30%	0.30%		
1000	500000	0.02%	0.30%	0.28%		
10000	500000	0.20%	0.30%	0.10%		
100000	500000	1.96%	0.30%	-1.66%		
1000000	500000	16.67%	0.30%	-16.37%		
10000000	500000	66.67%	0.30%	-66.37%		
100000000	500000	95.24%	0.30%	-94.94%		
1	50000	0.00%	0.30%	0.30%		
10	50000	0.02%	0.30%	0.28%		
100	50000	0.20%	0.30%	0.10%		
1000	50000	1.96%	0.30%	-1.66%		
10000	50000	16.67%	0.30%	-16.37%		
100000	50000	66.67%	0.30%	-66.37%		
1000000	50000	95.24%	0.30%	-94.94%		
10000000	50000	99.50%	0.30%	-99.20%		
100000000	50000	99.95%	0.30%	-99.65%		
1	500	0.28%	0.30%	0.10%		
10	500	1.96%	0.30%	-1.66%		
100	500	16.67%	0.30%	-16.37%		
1000	500	66.67%	0.30%	-66.37%		
10000	500	95.24%	0.30%	-94.94%		
100000	500	99.50%	0.30%	-99.20%		
1000000	500	99.95%	0.30%	-99.65%		
10000000	500	100.00%	0.30%	-99.70%		
100000000	500	100.00%	0.30%	-99.70%		
1	500	0.28%	0.30%	0.10%		
10	500	1.96%	0.30%	-1.66%		
100	500	16.67%	0.30%	-16.37%		
1000	500	66.67%	0.30%	-66.37%		
10000	500	95.24%	0.30%	-94.94%		
100000	500	99.50%	0.30%	-99.20%		
1000000	500	99.95%	0.30%	-99.65%		
10000000	500	100.00%	0.30%	-99.70%		
100000000	500	100.00%	0.30%	-99.70%		
1	100000	0.00%	0.30%	0.30%		
10	100000	0.00%	0.30%	0.30%		
100	100000	0.01%	0.30%	0.29%		
1000	100000	0.10%	0.30%	0.20%		
10000	100000	0.99%	0.30%	-0.69%		
100000	100000	9.09%	0.30%	-8.79%		
1000000	100000	50.00%	0.30%	-49.70%		
10000000	100000	90.91%	0.30%	-90.61%		
100000000	100000	99.91%	0.30%	-98.71%		
1	1000000	0.00%	0.30%	0.30%		
10	1000000	0.00%	0.30%	0.30%		
100	1000000	0.01%	0.30%	0.29%		
1000	1000000	0.10%	0.30%	0.20%		
10000	1000000	0.99%	0.30%	-0.69%		
100000	1000000	9.09%	0.30%	-8.79%		
1000000	1000000	50.00%	0.30%	-49.70%		
10000000	1000000	90.91%	0.30%	-90.61%		
100000000	1000000	99.91%	0.30%	-98.71%		
4.99999	1000000	0.00%	0.30%	0.30%		
499.900015	1000000	0.05%	0.30%	0.25%		
4990.01498	1000000	0.50%	0.30%	-0.20%		
49014.80247	1000000	4.67%	0.30%	-4.37%		
413223.1405	1000000	29.24%	0.30%	-28.94%		
1250000	1000000	55.56%	0.30%	-55.26%		
413223.1405	1000000	29.24%	0.30%	-28.94%		
49014.80247	1000000	4.67%	0.30%	-4.37%		
4.99999	5000000	0.00%	0.30%	0.30%		
49.99900001	5000000	0.00%	0.30%	0.30%		
49.99999999	5000000	0.00%	0.30%	0.30%		



There is an [implementation](#) of uniswap in cadCAD and an [overview](#) with video of the model.

Thorchain "Slip fee" (CLP)



This can be viewed as setting the fee ϕ according a regularizing rule that penalizes slippage and thus larger transactions, incentivizing smaller transactions, but also introduces angles for garning the system to minimize fees. The derivation can be found in the [Thorchain docs](#).

Comparing:

$$y_{ff} = \frac{xY}{x + X} (1 - \phi)$$

with

$$y_{dp} = \frac{xYX}{(x + X)^2} = \frac{xY}{x + X} \frac{X}{x + X}$$

so

$$(1 - \phi) = \frac{X}{x + X} = 1 - \frac{x}{x + X}$$

this is simply choosing a functional fee, as

$$\phi = \frac{x}{x + X}$$

499.900015	5000000	0.01%	0.30%	0.29%
4990.01498	5000000	0.10%	0.30%	0.20%
49014.80247	5000000	0.97%	0.30%	-0.67%
413223.1405	5000000	7.63%	0.30%	-7.33%
1250000	5000000	20.00%	0.30%	-19.70%
413223.1405	5000000	7.63%	0.30%	-7.33%
49014.80247	5000000	0.97%	0.30%	-0.67%
0.19999992	1000000	0.00%	0.30%	0.30%
1.999992	1000000	0.00%	0.30%	0.30%
19.99920002	1000000	0.00%	0.30%	0.30%
199.920024	1000000	0.02%	0.30%	0.28%
1992.023936	1000000	0.20%	0.30%	0.10%
1923.37562	1000000	1.89%	0.30%	-1.59%
138888.8889	1000000	12.20%	0.30%	-11.90%
222222.2222	1000000	18.18%	0.30%	-17.88%
45351.47392	1000000	4.34%	0.30%	-4.04%
0.19999992	5000000	0.00%	0.30%	0.30%
1.999992	5000000	0.00%	0.30%	0.30%
19.99920002	5000000	0.00%	0.30%	0.30%
199.920024	5000000	0.00%	0.30%	0.30%
1992.023936	5000000	0.04%	0.30%	0.26%
1923.37562	5000000	0.38%	0.30%	-0.08%
138888.8889	5000000	2.70%	0.30%	-2.40%
222222.2222	5000000	4.26%	0.30%	-3.96%
45351.47392	5000000	0.90%	0.30%	-0.60%
19.99920002	5000000	0.00%	0.30%	0.30%
199.920024	5000000	0.00%	0.30%	0.30%
1992.023936	5000000	0.04%	0.30%	0.26%
1923.37562	5000000	0.38%	0.30%	-0.08%
138888.8889	5000000	2.70%	0.30%	-2.40%
222222.2222	5000000	4.26%	0.30%	-3.96%
45351.47392	5000000	0.90%	0.30%	-0.60%
4950.372516	5000000	0.10%	0.30%	0.20%
499.5003748	5000000	0.01%	0.30%	0.29%
19.99920002	50000	0.04%	0.30%	0.26%
199.920024	50000	0.40%	0.30%	-0.10%
1992.023936	50000	3.83%	0.30%	-3.53%
1923.37562	50000	27.77%	0.30%	-27.47%
138888.8889	50000	73.53%	0.30%	-73.23%
222222.2222	50000	81.63%	0.30%	-81.33%
45351.47392	50000	47.56%	0.30%	-47.26%
4950.372516	50000	9.01%	0.30%	-8.71%
499.5003748	50000	0.99%	0.30%	-0.69%
1992.023936	50000	3.83%	0.30%	-3.53%
1923.37562	50000	27.77%	0.30%	-27.47%
138888.8889	50000	73.53%	0.30%	-73.23%
222222.2222	50000	81.63%	0.30%	-81.33%
45351.47392	50000	47.56%	0.30%	-47.26%
4950.372516	50000	9.01%	0.30%	-8.71%
499.5003748	50000	0.99%	0.30%	-0.69%
49.999500037	50000	0.10%	0.30%	0.20%
4.99995	50000	0.01%	0.30%	0.29%
1992.023936	500	79.94%	0.30%	-79.64%
1923.37562	500	97.46%	0.30%	-97.16%
138888.8889	500	99.64%	0.30%	-99.34%
222222.2222	500	99.78%	0.30%	-99.48%
45351.47392	500	98.91%	0.30%	-98.61%
4950.372516	500	98.83%	0.30%	-90.53%
499.5003748	500	49.98%	0.30%	-49.68%
49.99500037	500	0.99%	0.30%	-8.79%
4.99995	500	0.99%	0.30%	-0.69%
0.004999999	1000000	0.00%	0.30%	0.30%
0.00499990001	1000000	0.00%	0.30%	0.30%
0.0499990015	1000000	0.00%	0.30%	0.30%
0.499001498	1000000	0.00%	0.30%	0.30%
4.901480247	1000000	0.00%	0.30%	0.30%
41.32231405	1000000	0.00%	0.30%	0.30%
125	1000000	0.01%	0.30%	0.29%
41.32231405	1000000	0.00%	0.30%	0.30%
4.901480247	1000000	0.00%	0.30%	0.30%
0.0499999	1000000	0.00%	0.30%	0.30%
0.499990001	1000000	0.00%	0.30%	0.30%
4.99990015	1000000	0.00%	0.30%	0.30%
49.9001498	1000000	0.00%	0.30%	0.30%
490.1480247	1000000	0.05%	0.30%	0.25%
4132.231405	1000000	0.41%	0.30%	-0.11%
12500	1000000	1.23%	0.30%	-0.93%
4132.231405	1000000	0.41%	0.30%	-0.11%
490.1480247	1000000	0.05%	0.30%	0.25%

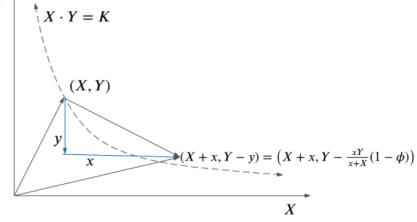
USD Value of Pool	USD Value of Pool Depth of Atom:Rowan	USD Value of Pool Depth of Rowan:TKN	Sifchain's Slip-Based Fee for swap of Rowan:Atom	Sifchain's Slip-Based Fee for swap of TKN	Sifchain's Total Slip-Based Fee for swap of Atom:TKN	Uniswap's Flat Fee of 0.3% plus 2% Slippage Allowance for ETH:TKN	Fee Savings with Sifchain	
1	5000000	1000000	0.00%	0.00%	0.00%	2.30%	2.30%	x: Amount of token X added to pool by swapper
100	5000000	1000000	0.00%	0.01%	0.01%	2.30%	2.30%	X: Amount of token X already in the pool
1000	5000000	1000000	0.02%	0.10%	0.12%	2.30%	2.28%	Sifchain's fee is lower than Uniswap's fee, so swappers save fees.
10000	5000000	1000000	0.20%	0.99%	1.19%	2.30%	2.10%	When swappers are swapping low volume relative to the pool, they pay less in fees than on Uniswap. When they are swapping high volume relative to the pool, they pay more in fees than on Uniswap (negative fee savings implies the fee on Sifchain is higher than on Uniswap).
20000	5000000	1000000	0.40%	1.95%	2.35%	2.30%		Swappers are willing to pay more in fees to change their position. In a single market, cycle swappers and poolers "both" profit more under the Sifchain swap fee than the Uniswap fee. Further research - https://github.com/chain-research/resources/blob/master/Analysis/OrChain-Gantlet-CLPReport-Nov2020.pdf
100000	5000000	1000000	1.96%	8.93%	10.89%	2.30%	0.34%	
1000000	5000000	1000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
10000000	5000000	1000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
1	5000000	1000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	1000000	0.00%	0.00%	0.00%	2.30%	2.30%	
100	5000000	1000000	0.02%	0.10%	0.12%	2.30%	2.28%	
1000	5000000	1000000	0.20%	0.99%	1.19%	2.30%	2.10%	
10000	5000000	1000000	1.96%	8.93%	10.89%	2.30%	0.34%	
100000	5000000	1000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	1000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	1000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
100	5000000	5000000	0.02%	0.00%	0.10%	2.30%	2.28%	
1000	5000000	5000000	0.20%	0.00%	0.20%	2.30%	2.10%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.28%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.28%	
100	5000000	5000000	0.02%	0.00%	0.00%	2.30%	2.10%	
1000	5000000	5000000	0.20%	0.00%	0.04%	2.30%	2.28%	
10000	5000000	5000000	1.96%	0.20%	0.40%	2.30%	2.10%	
100000	5000000	5000000	16.67%	45.45%	62.12%	2.30%	-14.3%	
1000000	5000000	5000000	66.67%	76.92%	143.59%	2.30%	-64.3%	
10000000	5000000	5000000	95.24%	82.64%	177.88%	2.30%	-92.9%	
1	5000000	5000000	0.00%	0.00%	0.00%	2.30%	2.30%	
10	5000000	5000000	0.00%	0.0				

4950.372516	500000	500000	0.10%	0.10%	0.20%	2.30%	2.20%	
499.5003748	500000	500000	0.01%	0.01%	0.02%	2.30%	2.20%	
19.99920002	50000	500000	0.04%	0.00%	0.04%	2.30%	2.20%	
199.920204	50000	500000	0.40%	0.00%	0.40%	2.30%	1.90%	
1992.023936	50000	500000	3.83%	0.04%	3.87%	2.30%	-1.53%	
19223.37662	50000	500000	27.77%	0.28%	28.05%	2.30%	-25.47%	
138868.8899	500000	500000	73.53%	0.73%	74.26%	2.30%	-71.23%	
222222.2222	50000	500000	81.63%	0.81%	82.44%	2.30%	-79.33%	
45351.47392	50000	500000	47.50%	0.47%	48.04%	2.30%	-45.26%	
4950.372516	50000	500000	9.01%	0.00%	9.10%	2.30%	-6.71%	
499.5003748	50000	500000	0.99%	0.01%	1.00%	2.30%	-1.31%	
1992.023936	50000	500000	3.83%	0.04%	3.87%	2.30%	-1.53%	
19223.37662	50000	500000	27.77%	0.28%	28.05%	2.30%	-25.47%	
138868.8899	500000	500000	73.53%	0.73%	74.26%	2.30%	-71.23%	
222222.2222	50000	500000	81.63%	0.81%	82.44%	2.30%	-79.33%	
45351.47392	50000	500000	47.50%	0.47%	48.04%	2.30%	-45.26%	
4950.372516	50000	500000	9.01%	0.00%	9.10%	2.30%	-6.71%	
499.5003748	50000	500000	0.99%	0.01%	1.00%	2.30%	-1.31%	
49.99500037	50000	500000	0.10%	0.00%	0.10%	2.30%	2.20%	
4.9995%	50000	500000	0.01%	0.00%	0.01%	2.30%	2.20%	
1992.023936	500	500000	79.34%	0.01%	79.34%	2.30%	-77.64%	
19223.37662	500	500000	97.40%	0.01%	97.47%	2.30%	-95.36%	
138868.8899	500	500000	99.64%	0.01%	99.65%	2.30%	-97.44%	
222222.2222	500	500000	99.78%	0.01%	99.79%	2.30%	-97.48%	
45351.47392	500	500000	98.51%	0.01%	98.52%	2.30%	-96.41%	
4950.372516	500	500000	98.83%	0.01%	98.84%	2.30%	-98.53%	
499.5003748	500	500000	98.95%	0.00%	98.98%	2.30%	-47.68%	
49.99500037	500	500000	9.09%	0.00%	9.09%	2.30%	-6.79%	
4.9995%	500	500000	0.99%	0.00%	0.99%	2.30%	-1.31%	
0.004999999	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
0.004999900001	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
0.0499900015	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
0.4999001498	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
4.901480247	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
41.32231405	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
125	1000000	500000	0.01%	0.00%	0.01%	2.30%	2.29%	
41.32231405	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
4.901480247	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
0.4999999	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
0.4999900001	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
4.99900015	1000000	500000	0.00%	0.00%	0.00%	2.30%	2.30%	
49.9001498	1000000	500000	0.00%	0.00%	0.01%	2.30%	2.30%	
490.1480247	1000000	500000	0.05%	0.01%	0.06%	2.30%	2.26%	
4132.231405	1000000	500000	0.41%	0.08%	0.49%	2.30%	1.89%	
12500	1000000	500000	1.23%	0.25%	1.48%	2.30%	1.07%	
4132.231405	1000000	500000	0.41%	0.08%	0.49%	2.30%	1.89%	
490.1480247	1000000	500000	0.05%	0.01%	0.06%	2.30%	2.25%	

x	X	Slip-Based Fee (used by Sifchain)	Flat-Fee of 0.3% (used by Uniswap)	Fee Savings with Sifchain		x: Amount of token X added to pool by swapper
1	30000	0.00%	0.30%	0.30%		
100	30000	0.33%	0.30%	-0.03%		
600	30000	1.96%	0.30%	-1.66%		
10000	30000	25.00%	0.30%	-24.70%		
						When swappers are swapping low volume relative to the pool, they pay less in fees than on Uniswap. When they are swapping high volume relative to the pool, they pay more in fees than on Uniswap (negative fee savings implies the fee on Sifchain is higher than on Uniswap). Swappers benefit under normal conditions while poolers benefit during periods of high volatility when swap price would pay more in fees to change their position. In a single market, swap fees are paid to both parties, but more under the Sifchain swap fee than the Uniswap fee. Further research - https://github.com/thorchain/Resources/blob/master/Audits/THORchain-Gauntlet-CLPReport-Nov2020.pdf
100000	1000000	9.09%	0.30%	-8.79%		
1000000	1000000	50.00%	0.30%	-49.70%		
10000000	1000000	99.91%	0.30%	-90.61%		
100000000	1000000	99.91%	0.30%	-98.71%		
1	100000	0.00%	0.30%	0.30%		
10	100000	0.00%	0.30%	0.30%		
100	100000	0.01%	0.30%	0.29%		
1000	100000	0.10%	0.30%	0.20%		
10000	100000	0.99%	0.30%	-0.69%		
100000	100000	9.09%	0.30%	-8.79%		
1000000	100000	50.00%	0.30%	-49.70%		
10000000	100000	99.91%	0.30%	-90.61%		
100000000	100000	99.91%	0.30%	-98.71%		
1	5000000	0.00%	0.30%	0.30%		
10	5000000	0.00%	0.30%	0.30%		
100	5000000	0.00%	0.30%	0.30%		
1000	5000000	0.02%	0.30%	0.28%		
10000	5000000	0.20%	0.30%	0.10%		
100000	5000000	1.96%	0.30%	-1.66%		
1000000	5000000	16.67%	0.30%	-16.37%		
10000000	5000000	66.67%	0.30%	-66.37%		
100000000	5000000	95.24%	0.30%	-94.94%		
1	500000	0.00%	0.30%	0.30%		
10	500000	0.00%	0.30%	0.30%		
100	500000	0.00%	0.30%	0.30%		
1000	500000	0.02%	0.30%	0.28%		
10000	500000	0.20%	0.30%	0.10%		
100000	500000	1.96%	0.30%	-1.66%		
1000000	500000	16.67%	0.30%	-16.37%		
10000000	500000	66.67%	0.30%	-66.37%		
100000000	500000	95.24%	0.30%	-94.94%		
1	50000	0.00%	0.30%	0.30%		
10	50000	0.02%	0.30%	0.28%		
100	50000	0.20%	0.30%	0.10%		
1000	50000	1.96%	0.30%	-1.66%		
10000	50000	16.67%	0.30%	-16.37%		
100000	50000	66.67%	0.30%	-66.37%		
1000000	50000	95.24%	0.30%	-94.94%		
10000000	50000	99.50%	0.30%	-99.20%		
100000000	50000	99.95%	0.30%	-99.65%		
1	500	0.28%	0.30%	0.10%		
10	500	1.96%	0.30%	-1.66%		
100	500	16.67%	0.30%	-16.37%		
1000	500	66.67%	0.30%	-66.37%		
10000	500	95.24%	0.30%	-94.94%		
100000	500	99.50%	0.30%	-99.20%		
1000000	500	99.95%	0.30%	-99.65%		
10000000	500	100.00%	0.30%	-99.70%		
100000000	500	100.00%	0.30%	-99.70%		
1	500	0.28%	0.30%	0.10%		
10	500	1.96%	0.30%	-1.66%		
100	500	16.67%	0.30%	-16.37%		
1000	500	66.67%	0.30%	-66.37%		
10000	500	95.24%	0.30%	-94.94%		
100000	500	99.50%	0.30%	-99.20%		
1000000	500	99.95%	0.30%	-99.65%		
10000000	500	100.00%	0.30%	-99.70%		
100000000	500	100.00%	0.30%	-99.70%		
1	100000	0.00%	0.30%	0.30%		
10	100000	0.00%	0.30%	0.30%		
100	100000	0.01%	0.30%	0.29%		
1000	100000	0.10%	0.30%	0.20%		
10000	100000	0.99%	0.30%	-0.69%		
100000	100000	9.09%	0.30%	-8.79%		
1000000	100000	50.00%	0.30%	-49.70%		
10000000	100000	90.91%	0.30%	-90.61%		
100000000	100000	99.91%	0.30%	-98.71%		
1	1000000	0.00%	0.30%	0.30%		
10	1000000	0.00%	0.30%	0.30%		
100	1000000	0.01%	0.30%	0.29%		
1000	1000000	0.10%	0.30%	0.20%		
10000	1000000	0.99%	0.30%	-0.69%		
100000	1000000	9.09%	0.30%	-8.79%		
1000000	1000000	50.00%	0.30%	-49.70%		
10000000	1000000	90.91%	0.30%	-90.61%		
100000000	1000000	99.91%	0.30%	-98.71%		
4.99999	1000000	0.00%	0.30%	0.30%		
499.900015	1000000	0.05%	0.30%	0.25%		
4990.01498	1000000	0.50%	0.30%	-0.20%		
49014.80247	1000000	4.67%	0.30%	-4.37%		
413223.1405	1000000	29.24%	0.30%	-28.94%		
1250000	1000000	55.56%	0.30%	-55.26%		
413223.1405	1000000	29.24%	0.30%	-28.94%		
49014.80247	1000000	4.67%	0.30%	-4.37%		
4.99999	5000000	0.00%	0.30%	0.30%		
49.99900001	5000000	0.00%	0.30%	0.30%		
49.99999999	5000000	0.00%	0.30%	0.30%		

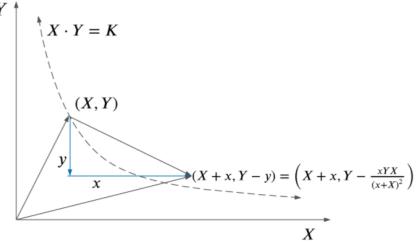
Fee Derivation from <https://hackmd.io/bVK2LSYjRTyeNC0hVt2hg>

Constant Product Market Maker: Flat Fee



There is an [implementation](#) of uniswap in cadCAD and an [overview](#) with video of the model.

Thorchain "Slip fee" (CLP)



This can be viewed as setting the fee ϕ according a regularizing rule that penalizes slippage and thus larger transactions, incentivizing smaller transactions, but also introduces angles for garning the system to minimize fees. The derivation can be found in the [Thorchain docs](#).

Comparing:

$$y_{ff} = \frac{xY}{x + X} (1 - \phi)$$

with

$$y_{dp} = \frac{xYX}{(x + X)^2} = \frac{xY}{x + X} \frac{X}{x + X}$$

so

$$(1 - \phi) = \frac{X}{x + X} = 1 - \frac{x}{x + X}$$

this is simply choosing a functional fee, as

$$\phi = \frac{x}{x + X}$$

499.900015	5000000	0.01%	0.30%	0.29%
4990.01498	5000000	0.10%	0.30%	0.20%
49014.80247	5000000	0.97%	0.30%	-0.67%
413223.1405	5000000	7.63%	0.30%	-7.33%
1250000	5000000	20.00%	0.30%	-19.70%
413223.1405	5000000	7.63%	0.30%	-7.33%
49014.80247	5000000	0.97%	0.30%	-0.67%
0.19999992	1000000	0.00%	0.30%	0.30%
1.999992	1000000	0.00%	0.30%	0.30%
19.99920002	1000000	0.00%	0.30%	0.30%
199.920024	1000000	0.02%	0.30%	0.28%
1992.023936	1000000	0.20%	0.30%	0.10%
1923.37562	1000000	1.89%	0.30%	-1.59%
138888.8889	1000000	12.20%	0.30%	-11.90%
222222.2222	1000000	18.18%	0.30%	-17.88%
45351.47392	1000000	4.34%	0.30%	-4.04%
0.19999992	5000000	0.00%	0.30%	0.30%
1.999992	5000000	0.00%	0.30%	0.30%
19.99920002	5000000	0.00%	0.30%	0.30%
199.920024	5000000	0.00%	0.30%	0.30%
1992.023936	5000000	0.04%	0.30%	0.26%
1923.37562	5000000	0.38%	0.30%	-0.08%
138888.8889	5000000	2.70%	0.30%	-2.40%
222222.2222	5000000	4.26%	0.30%	-3.96%
45351.47392	5000000	0.90%	0.30%	-0.60%
19.99920002	5000000	0.00%	0.30%	0.30%
199.920024	5000000	0.00%	0.30%	0.30%
1992.023936	5000000	0.04%	0.30%	0.26%
1923.37562	5000000	0.38%	0.30%	-0.08%
138888.8889	5000000	2.70%	0.30%	-2.40%
222222.2222	5000000	4.26%	0.30%	-3.96%
45351.47392	5000000	0.90%	0.30%	-0.60%
4950.372516	5000000	0.10%	0.30%	0.20%
499.5003748	5000000	0.01%	0.30%	0.29%
19.99920002	50000	0.04%	0.30%	0.26%
199.920024	50000	0.40%	0.30%	-0.10%
1992.023936	50000	3.83%	0.30%	-3.53%
1923.37562	50000	27.77%	0.30%	-27.47%
138888.8889	50000	73.53%	0.30%	-73.23%
222222.2222	50000	81.63%	0.30%	-81.33%
45351.47392	50000	47.56%	0.30%	-47.26%
4950.372516	50000	9.01%	0.30%	-8.71%
499.5003748	50000	0.99%	0.30%	-0.69%
1992.023936	50000	3.83%	0.30%	-3.53%
1923.37562	50000	27.77%	0.30%	-27.47%
138888.8889	50000	73.53%	0.30%	-73.23%
222222.2222	50000	81.63%	0.30%	-81.33%
45351.47392	50000	47.56%	0.30%	-47.26%
4950.372516	50000	9.01%	0.30%	-8.71%
499.5003748	50000	0.99%	0.30%	-0.69%
49.999500037	50000	0.10%	0.30%	0.20%
4.99995	50000	0.01%	0.30%	0.29%
1992.023936	500	79.94%	0.30%	-79.64%
1923.37562	500	97.46%	0.30%	-97.16%
138888.8889	500	99.64%	0.30%	-99.34%
222222.2222	500	99.78%	0.30%	-99.48%
45351.47392	500	98.91%	0.30%	-98.61%
4950.372516	500	98.83%	0.30%	-90.53%
499.5003748	500	49.98%	0.30%	-49.68%
49.99500037	500	0.99%	0.30%	-8.79%
4.99995	500	0.99%	0.30%	-0.69%
0.004999999	1000000	0.00%	0.30%	0.30%
0.00499990001	1000000	0.00%	0.30%	0.30%
0.0499990015	1000000	0.00%	0.30%	0.30%
0.499001498	1000000	0.00%	0.30%	0.30%
4.901480247	1000000	0.00%	0.30%	0.30%
41.32231405	1000000	0.00%	0.30%	0.30%
125	1000000	0.01%	0.30%	0.29%
41.32231405	1000000	0.00%	0.30%	0.30%
4.901480247	1000000	0.00%	0.30%	0.30%
0.0499999	1000000	0.00%	0.30%	0.30%
0.499990001	1000000	0.00%	0.30%	0.30%
4.99990015	1000000	0.00%	0.30%	0.30%
49.9001498	1000000	0.00%	0.30%	0.30%
490.1480247	1000000	0.05%	0.30%	0.25%
4132.231405	1000000	0.41%	0.30%	-0.11%
12500	1000000	1.23%	0.30%	-0.93%
4132.231405	1000000	0.41%	0.30%	-0.11%
490.1480247	1000000	0.05%	0.30%	0.25%

Swap ETH for erowan	Swap ETH for erowan	Swap erowan for ETH	\$3,931
\$3,931	\$3,931	\$1,341	\$3,931
1.6791	1.6791	2,198	\$1,341
ETH	ETH	erow...	\$1,638
6,517	6,517	0.5853	\$1,638
erow...	erow...	ETH	\$4,374
0x5285...d214	0x5285...d214	0x0d4a...1852	\$884.99
37 minutes ago	38 minutes ago	3 hours ago	\$884.99
Swap ETH for erowan	Swap ETH for erowan	Swap erowan for ETH	\$114.41
\$1,638	\$1,638	\$4,374	\$954.36
0.7	0.7	7,000	\$954.36
ETH	ETH	erow...	\$5,680
2,784	2,784	1.9115	\$542.20
erow...	erow...	ETH	\$542.20
0xdbf9...3a6c	0xdbf9...3a6c	0x322e...cd90	\$403.14
44 minutes ago	45 minutes ago	3 hours ago	\$2,338
Swap erowan for ETH	Swap erowan for ETH	Swap ETH for erowan	\$2,338
\$884.99	\$884.99	\$114.41	\$4,969
1,518	1,518	0.05	\$1,211
erow...	erow...	ETH	\$1,211
0.3781	0.3781	178.6617	\$1,356
ETH	ETH	erow...	\$162.37
0x811b...954f	0x811b...954f	0x6a3d...6ffa	\$162.37
45 minutes ago	46 minutes ago	3 hours ago	\$6,139
Swap ETH for erowan	Swap ETH for erowan	Swap erowan for ETH	\$5,843
\$954.36	\$954.36	\$5,680	\$5,843
0.4085	0.4085	2.482	\$3,497
ETH	ETH	ETH	\$2,719
1,631	1,631	9,096	\$2,719
erow...	erow...	erow...	\$4,697
0x73d5...ed75	0x73d5...ed75	0x6367...8925	\$2,434
54 minutes ago	54 minutes ago	3 hours ago	
Swap ETH for erowan	Swap ETH for erowan	Swap erowan for ETH	
\$542.20	\$542.20	\$403.14	
0.232	0.232	664.3322	
ETH	ETH	erow...	
932.3409	932.3409	0.1761	
erow...	erow...	ETH	
0x28fd...b0fe	0x28fd...b0fe	0xa9bd...ed49	
55 minutes ago	56 minutes ago	3 hours ago	
Swap ETH for erowan	Swap ETH for erowan	Swap erowan for ETH	
\$2,338	\$2,338	\$4,969	
1	1	8,000	

ETH	ETH	erow...
4,071	4,071	2.1711
erow...	erow...	ETH
0x300d...ea86	0x300d...ea86	0x7a25...488d
1 hour ago	1 hour ago	3 hours ago
Swap erowan for E Swap erowan for F Swap ETH for erowan		
\$1,211	\$1,211	\$1,356
2,138	2,138	0.593
erow...	erow...	ETH
0.5194	0.5194	2,138
ETH	ETH	erow...
0x0c24...2d63	0x0c24...2d63	0x15d4...abbb
1 hour ago	1 hour ago	3 hours ago
Swap ETH for ero Swap ETH for ero Swap ETH for erowan		
\$162.37	\$162.37	\$6,139
0.07	0.07	2.6839
ETH	ETH	ETH
285.0524	285.0524	10,000
erow...	erow...	erow...
0xedf5...eb79	0xedf5...eb79	0xaf1c...ee61
1 hour ago	1 hour ago	3 hours ago
Swap erowan for E Swap erowan for F Swap ETH for erowan		
\$5,843	\$5,843	\$3,497
10,009	10,009	1.53
erow...	erow...	ETH
2.506	2.506	5,950
ETH	ETH	erow...
0x10b1...376f	0x10b1...376f	0x7a51...1857
1 hour ago	1 hour ago	3 hours ago
Swap erowan for E Swap erowan for F Swap erowan for ETH		
\$2,719	\$2,719	\$4,697
4,500	4,500	8,000
erow...	erow...	erow...
1.1705	1.1705	2.0561
ETH	ETH	ETH
0x7a25...488d	0x7a25...488d	0x7a25...488d
1 hour ago	1 hour ago	4 hours ago