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MADNESS

Maximum-A-posteriori solution with Deep generative NEtworks for Source Separation

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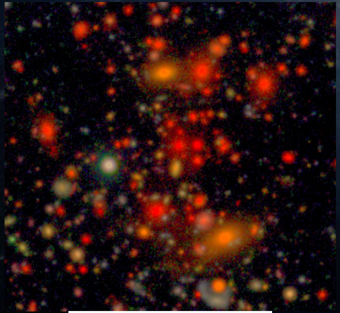
BDL Workshop
23rd June, 2022

ENS | PSL

Surveys and Challenges



HSC ultradeep image

Large survey of Space and Time (LSST) at Vera Rubin Observatory:

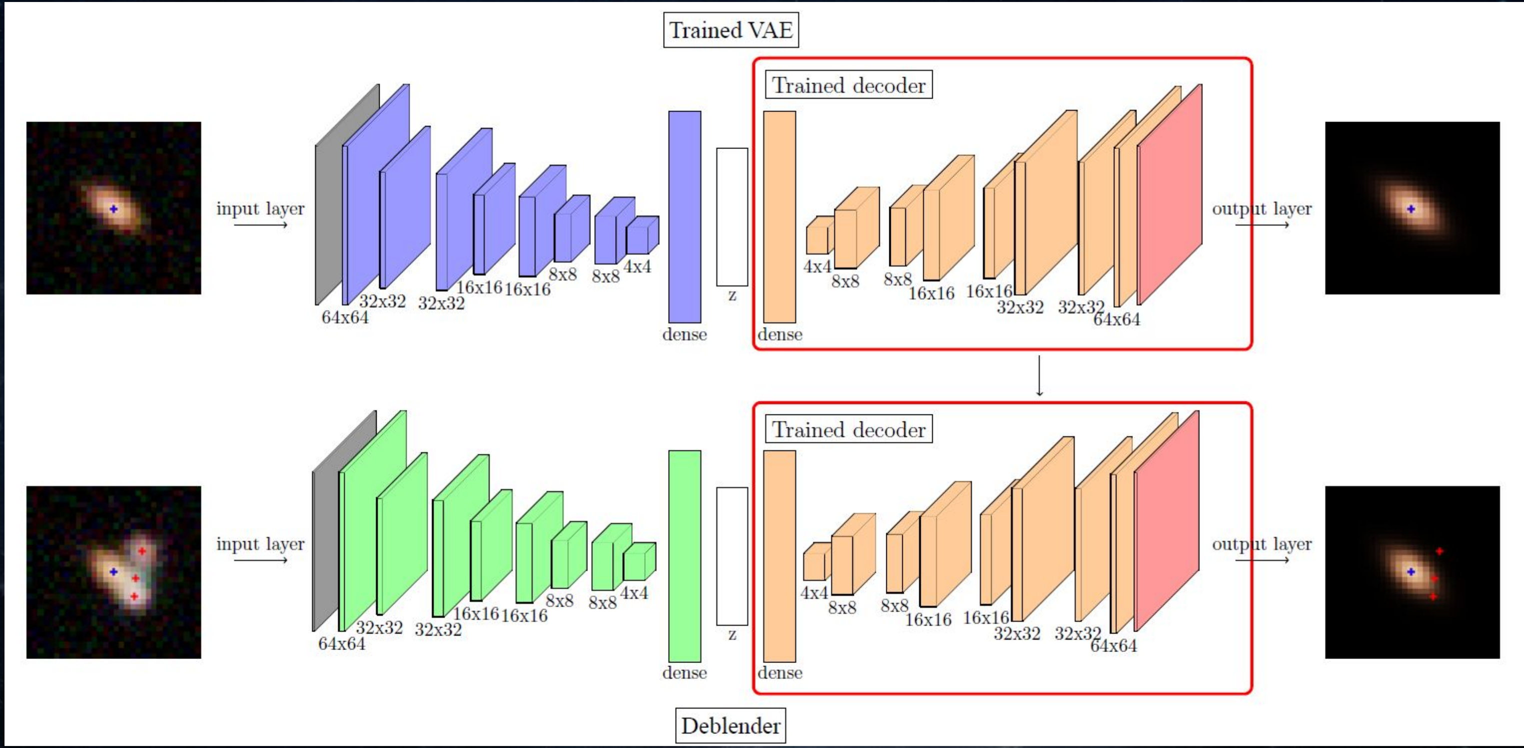
- Ground-based
- constrain Dark Energy
- 3.2 billion pixel camera
- 6 observation bands in visible range

more depth + area of coverage ⇒ More statistics!

greater depth means more complex data!

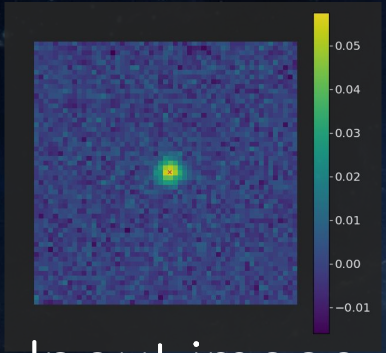
~ Galaxies (60% in LSST) are expected to overlap (blending) in images due to increased depth

ML for Deblending

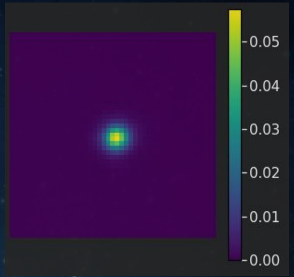


Arcelin et al (arXiv:2005.12039)

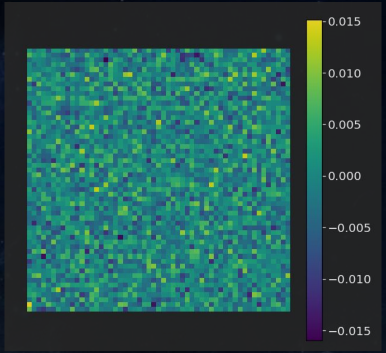
Denoising (Single source)



Input image (y)



Predicted image (x)



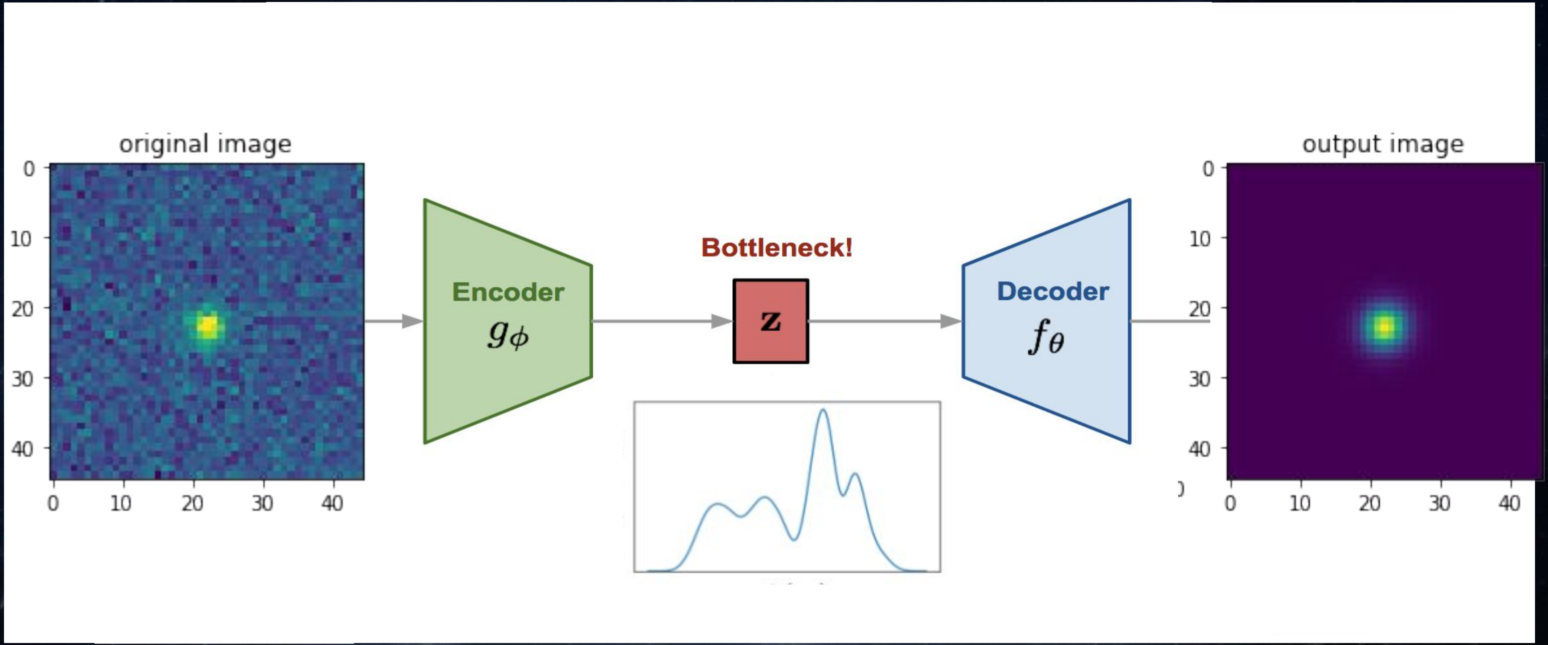
Residual (y-x)

$$x^* = \arg\min_x \; -\log p(y|x) - \log p(x)$$

$$x^* = \arg\min_x \; \frac{\| y - x \|^2}{2\sigma_{noise}^2} - \log p(x)$$

Where, $x*$ is the maximum a posteriori probability (MAP) estimate

Train VAE as generative model

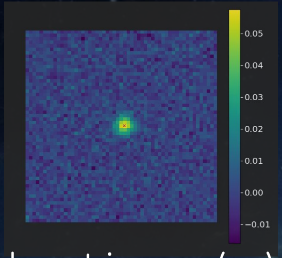


For example: Lanusse et al (arXiv:2008.03833)

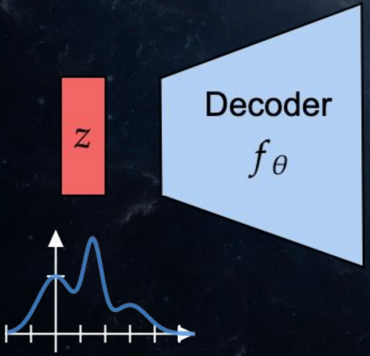
Training: $-\mathbb{E}_{\mathbf{z}\sim q_\phi(\mathbf{z}|\mathbf{x})} \log p_\theta(\mathbf{x}|\mathbf{z}) + D_{\mathrm{KL}}(q_\phi(\mathbf{z}|\mathbf{x}) \| p_\theta(\mathbf{z}))$

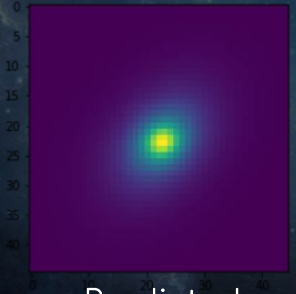
Reconstruction term Regularization term

MAP estimate in latent space



Input image (y)





Predicted galaxy (x)

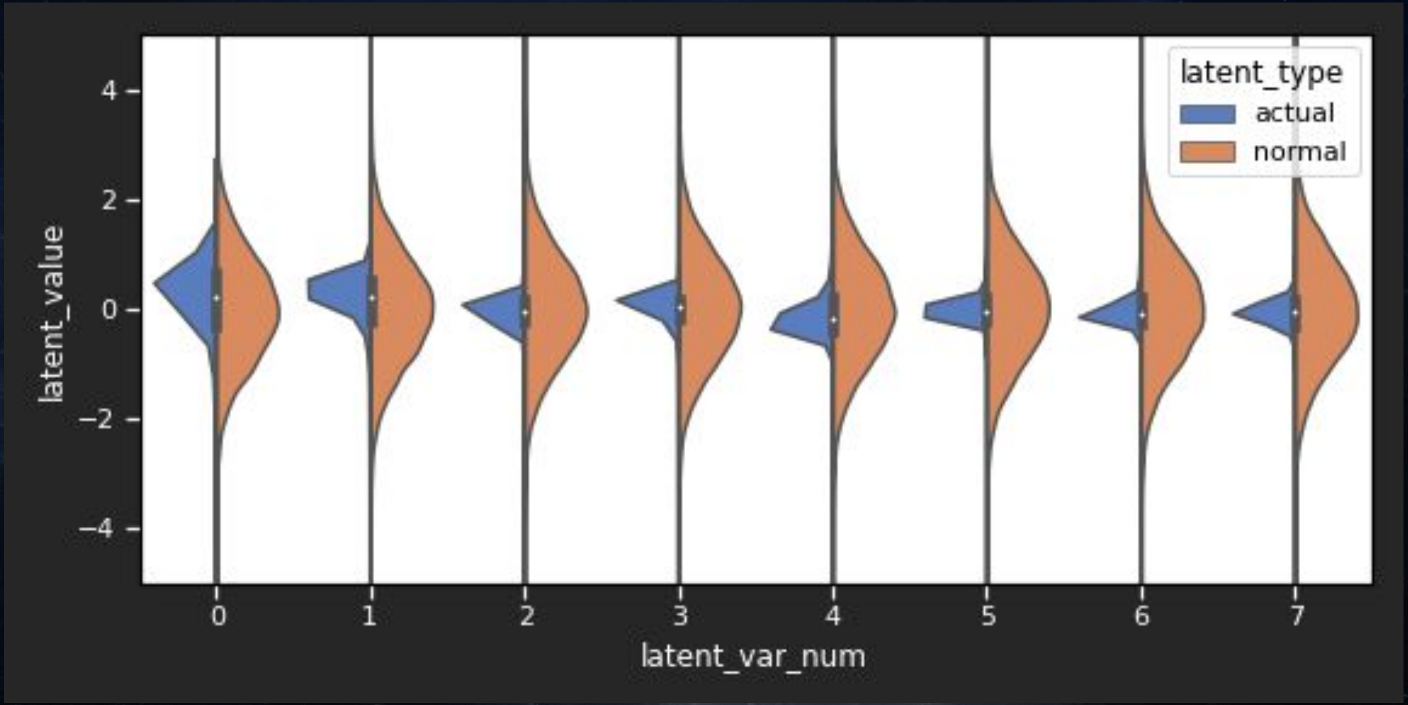
$$x^* = \arg\min_x - \frac{\| y - x \|^2}{2\sigma_{noise}^2} - \log p(x)$$

Going to the latent space

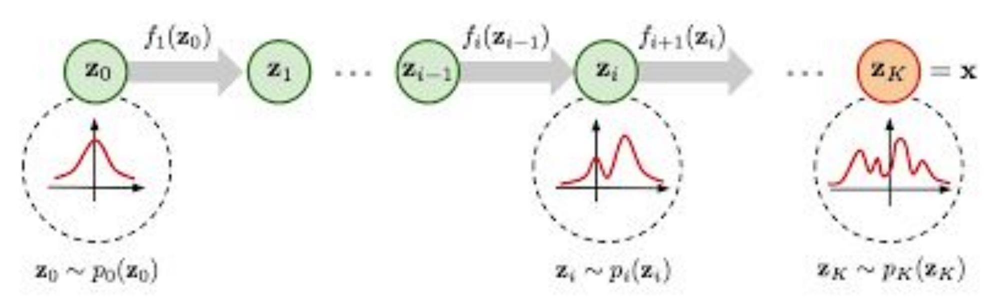
$$z^* = \arg\min_z \frac{\| y - f_\theta(z) \|^2}{2\sigma_{noise}^2} - \log p(z)$$

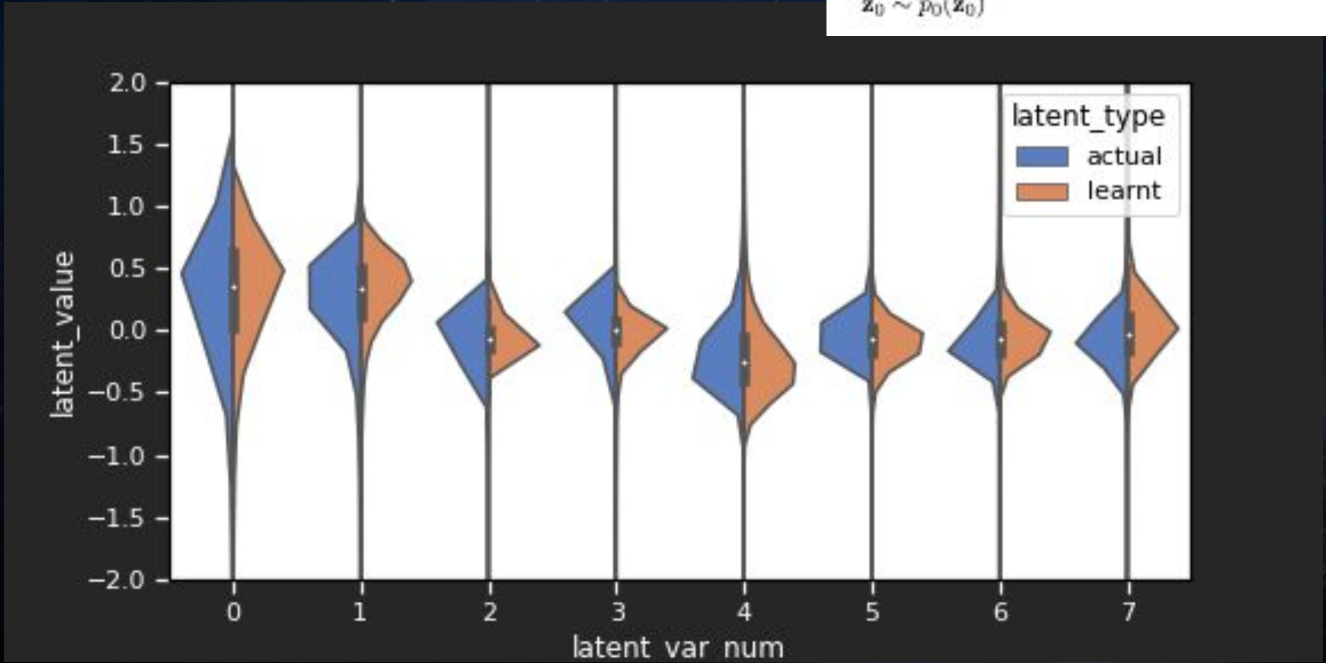
Where, z^* is the maximum a posteriori probability estimate in the latent space

How to choose a prior?

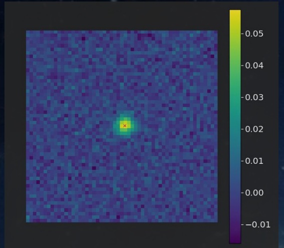


Normalizing flow



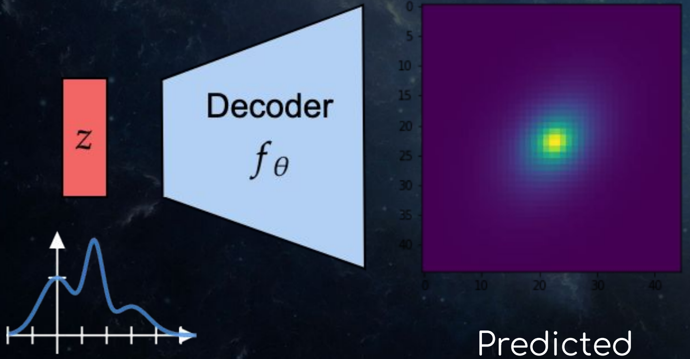


Minimization



Input image (y)

- Start with random z
- Do gradient descent in the latent space to minimize the objective function



Predicted galaxy (x)

$$z^* = \arg\min_{z} \frac{|| y - f_\theta(z) ||^2}{2\sigma^2_{noise}} - \log p(z)$$

Where, z^* is the maximum a posteriori probability estimate in the latent space

Deblending (Multiple sources)

$$Z = \{z_i \mid z_i \; being \; the \; latent \; space \; representation \; of \; i^{th} \; galaxy\}$$

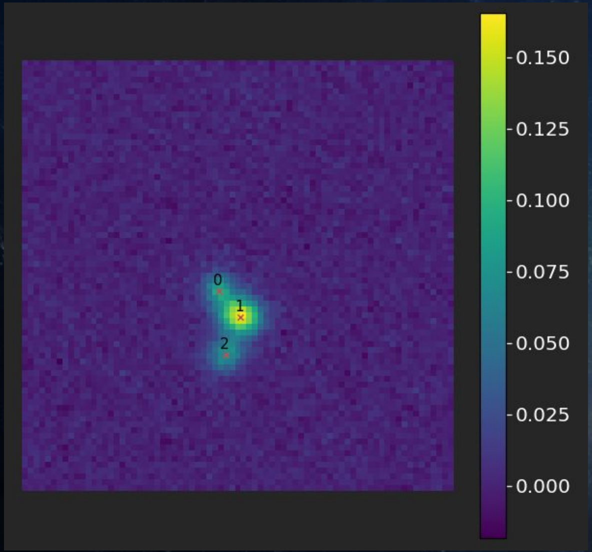
$$Z^* = \underset{Z}{\arg\min} \; -\log p(y|Z) - \log p(Z)$$

Reconstructed field

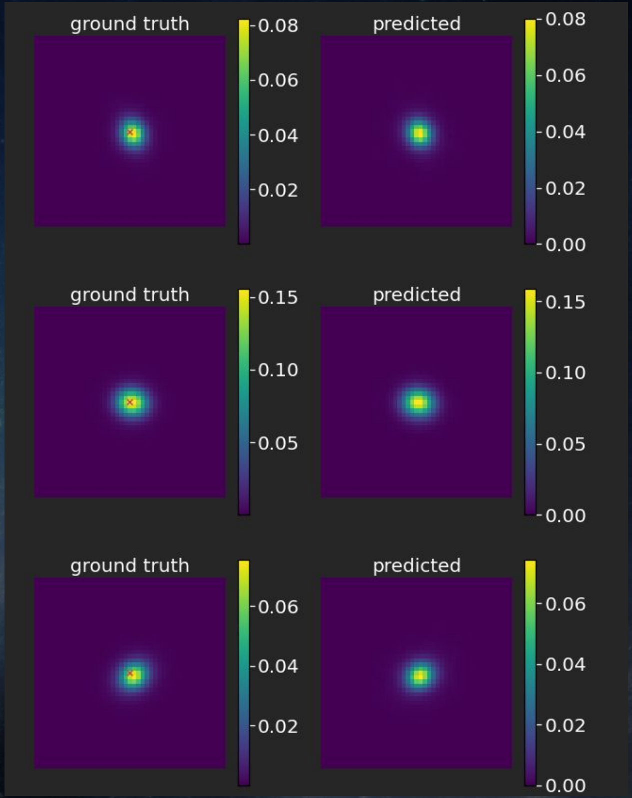
Probability that predictions are galaxies!

$$Z^* = \underset{Z}{\arg\min} \; \frac{|| y - \sum_i f_\theta(z_i) ||^2}{2\sigma^2_{noise}} - \sum_i \log p(z_i)$$

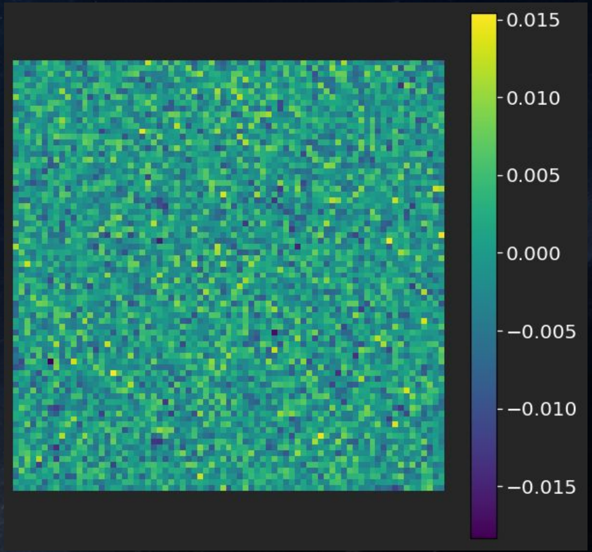
Deblending Example



Input image

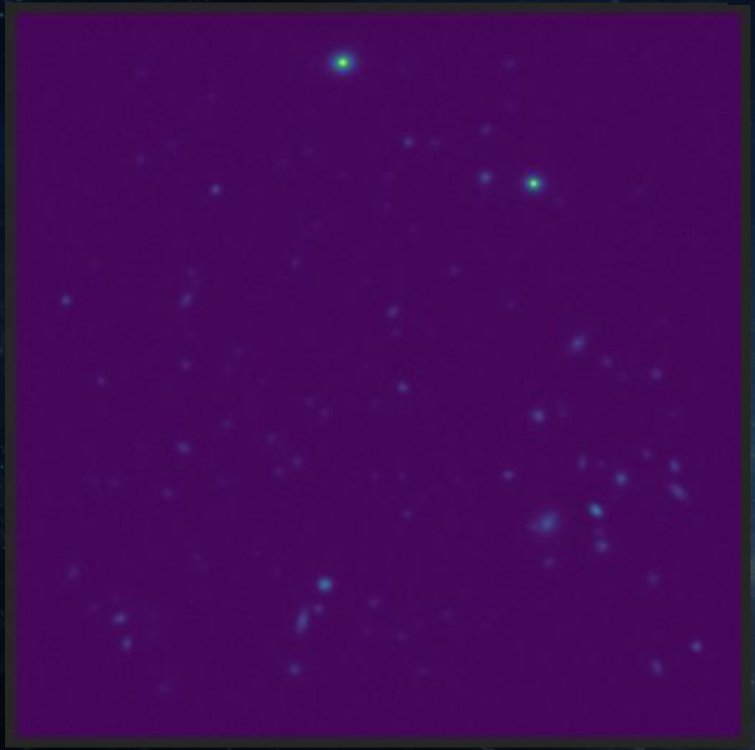


Predictions

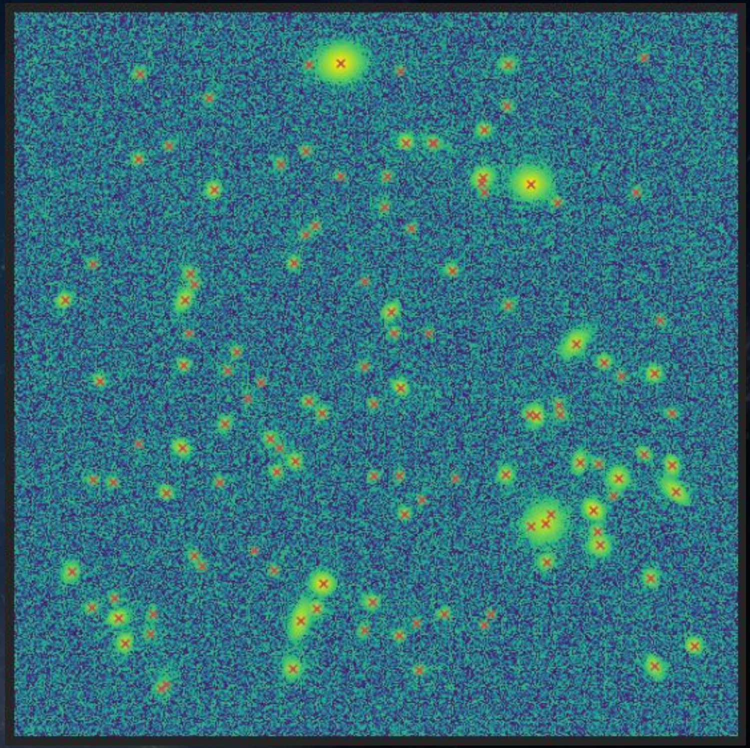


Residual image
(input - predictions)

Moving to a larger field...

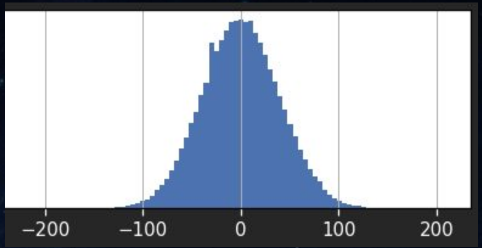


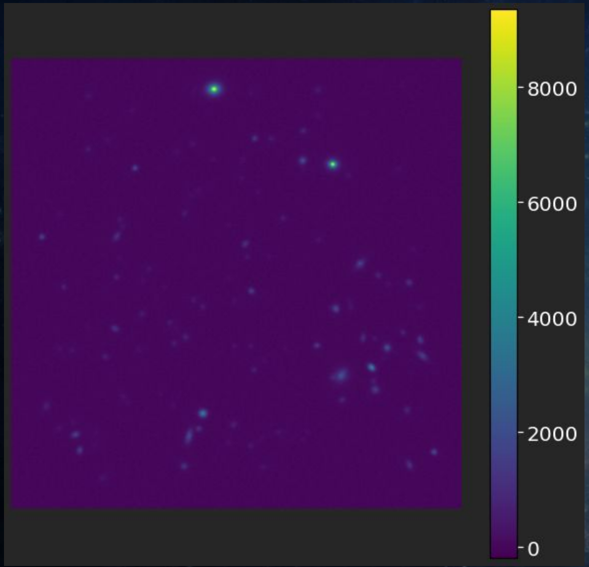
Input field (501 x 501)



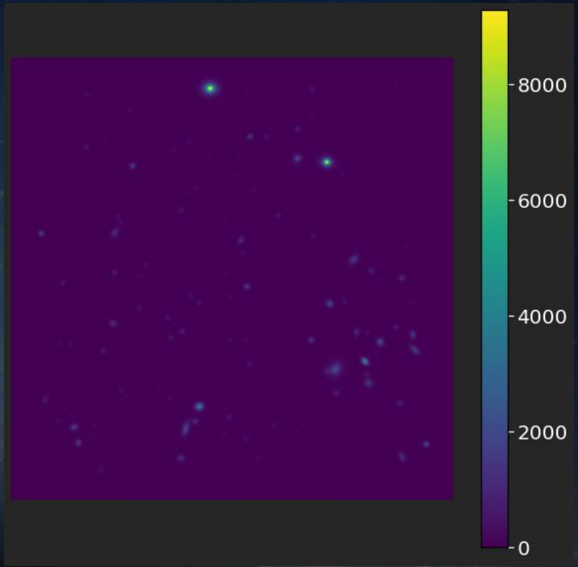
$\sinh^{-1}$(Input field)

Moving to a larger field...

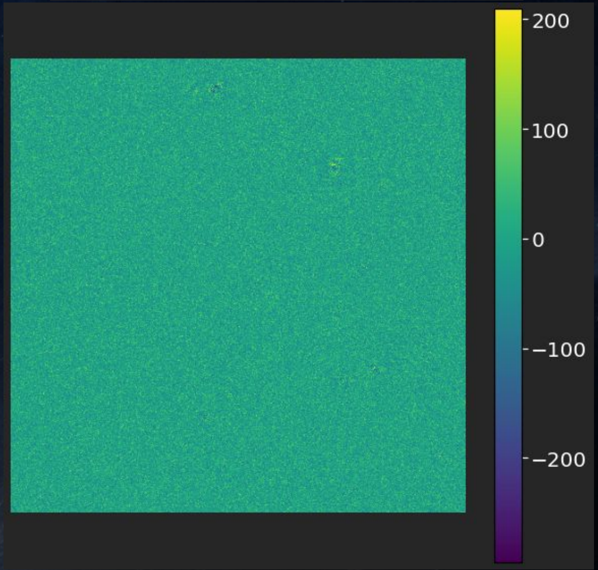




Input field



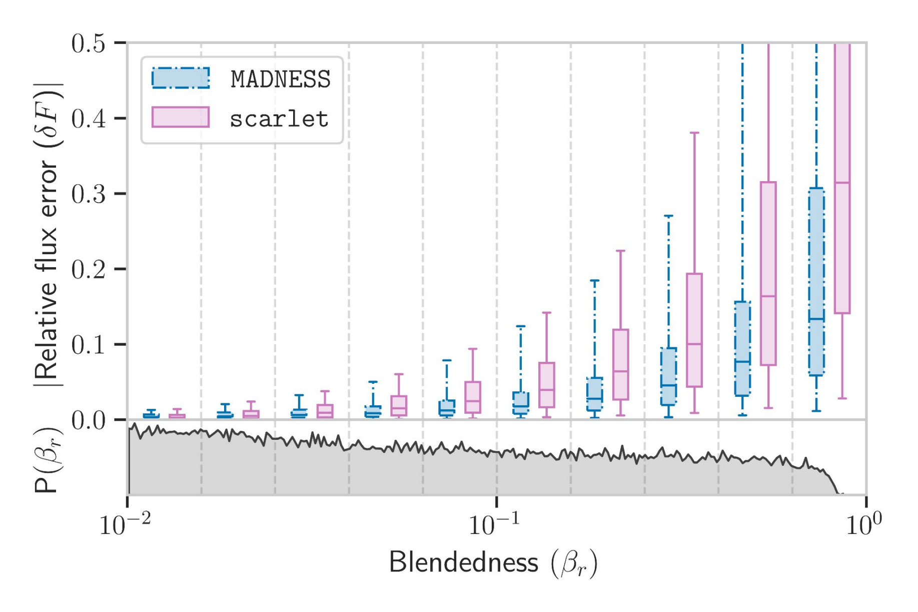
predicted field

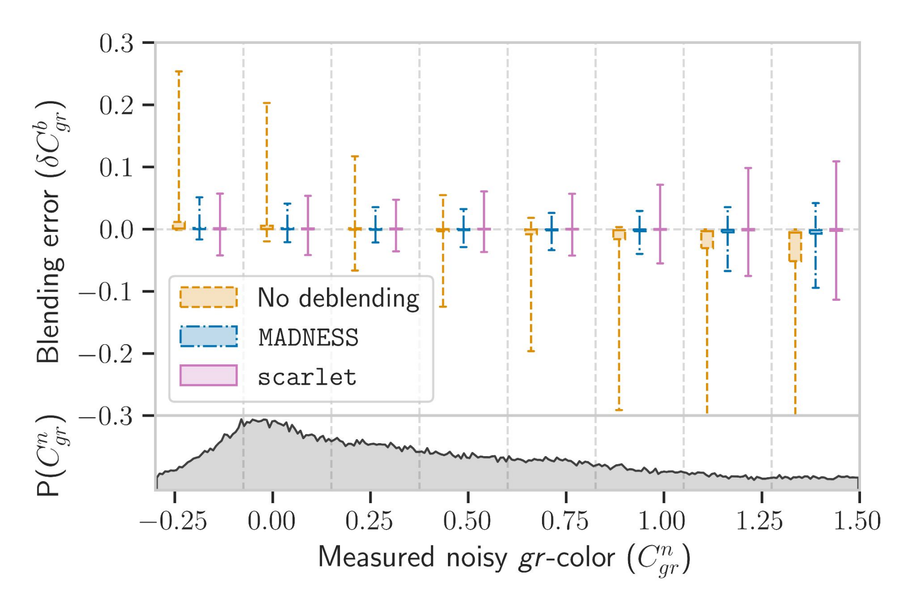


residual field
(Input - predicted)

Preliminary results*

Compare with SOTA





Conclusion and Future work

- Developed MAP estimate with generative models
- Performance close to SOTA!
- Benchmark speed
- metrics
- Real data!

Thank you!