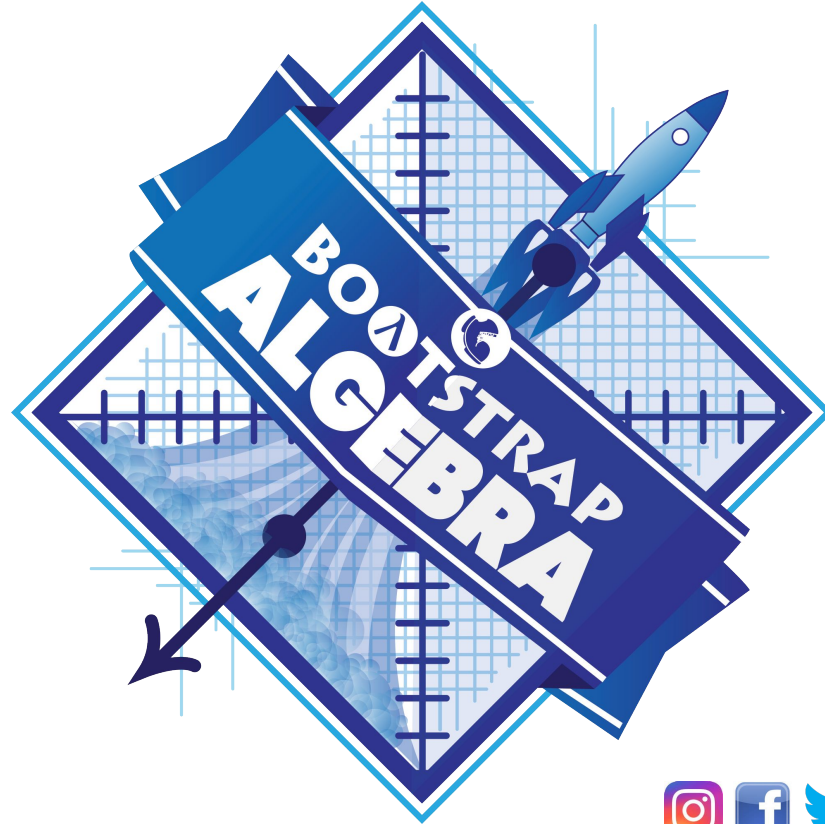


# Function Composition



# Composing Functions



For this activity we will be working in groups of 3-4 students.

Each group has a set of "Function Cards", each of which takes an input and produces an output.

# Composing Functions



Each **function card** has a Contract (Name, Domain, Range), and a description of what it does.

Starting with 4,

- you could play the `add 1` card to turn it into 5.
- you could play `add 6` and turn it into 10.

What other cards could you play to get from 4 to 10?

# Composing Functions



Select the cards you would play with to get from the starting number to the ending number.

- Start at 4, end at 26
- Start at -22, end at 13
- Start at 64, end at 0

Let's try some more numbers from this [random integer generator](#).

You will need to use some functions more than once, and that's ok! If you're ready for a challenge, try to find the *shortest path* from start to end, using the smallest number of compositions.



# Diagramming Function Composition

Three of the function cards we just used were for the functions  $f$ ,  $g$  and  $h$ :

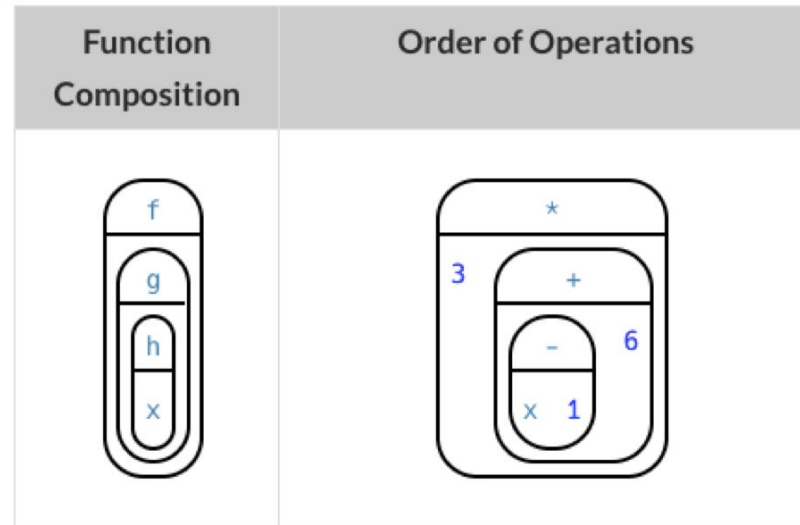
- $f$  multiplies its input by 3
- $g$  adds six to its input
- $h$  subtracts one from its input

We can compose those functions in any order. If we composed them as  $f(g(h(x)))$  and evaluated them for  $x = 4$  what would happen?



# Diagramming Function Composition

The circles of evaluation for  $f(g(h(4)))$  would look like this:





# Diagramming Function Composition

Complete [Diagramming Function Composition](#) with your partner.



# Diagramming Function Composition

Do  $f(g(h(x)))$  and  $g(h(f(x)))$  evaluate to the same thing?



# Composing Functions in Code



- Log into [WeScheme](#), and open a new program.
- Save the file as "Function Composition", and click "Run".
- Complete the following [Function Composition -- Green Star](#).  
When you're done, change the color of all the stars in the file to gold.
- Then try [Function Composition -- Your Name](#).
- If you have time, work with [Function Composition -- scale-xy](#) and/or [Function Composition Matching Activity](#)





# Composing Functions in Code

- What do all of these functions have in common?
- Does using one of these functions change the original image?
- What does the number in `scale` represent?
- What does the number in `rotate` represent?
- The Domain and Range for `flip-horizontal` is `Image -> Image`. Why can we use the output of the `text` function as an *input* for `flip-horizontal`?

# Composing Multiple Ways



As is often true with solving math problems, there is more than one way to get the same composed image.

Suppose I wrote the code:

```
(scale 3 (circle 50 "solid" "red"))
```

What's another line of code I could write that would produce the exact same image?

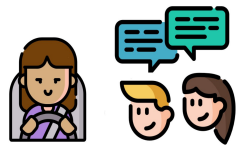
# Composing Multiple Ways



Complete [More than one way to Compose an Image!](#).

There is a special function in WeScheme that lets us test whether or not two images are equal.

```
image=? :: Image, Image -> Boolean
```



Use it to test whether all of the expressions you wrote successfully build the same images.



# Composing Multiple Ways



- Could we have written more expressions to create the same images?
- Are all of the ways to write the code equally efficient?