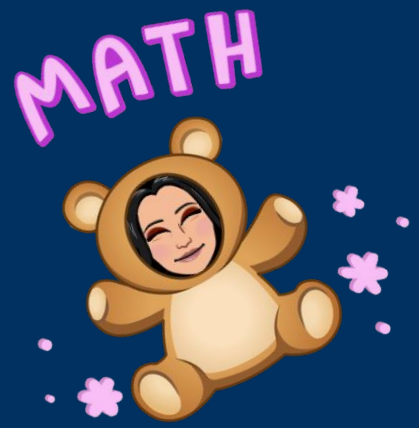
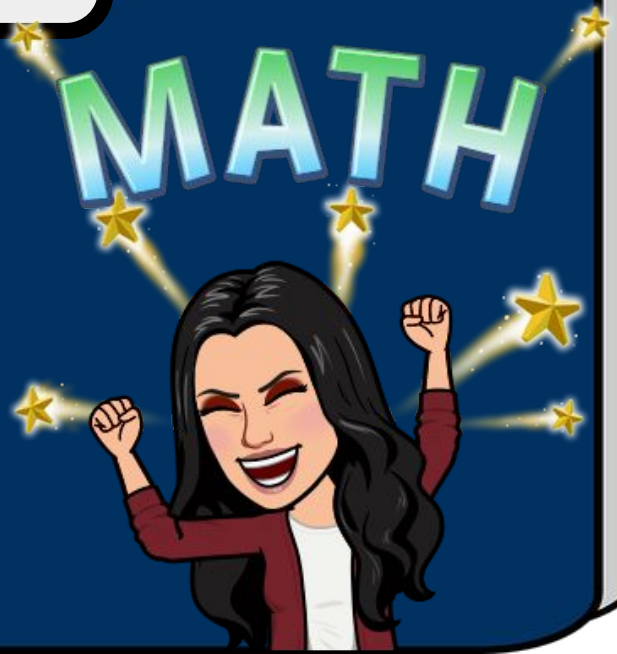


Digital Math Notebook



Math Key Terms

Addition

* Sum
* Total
* Increased by
* More
* Addend
* Together
* Combined
* Perimeter
* Deposit
* In all
* And
* Plus

Multiplication

* Product
* Rows of
* Factors
* Product of
* Double
* Triple
* Multiple
* Area
* Volume
* Each
* Twice
* Groups of

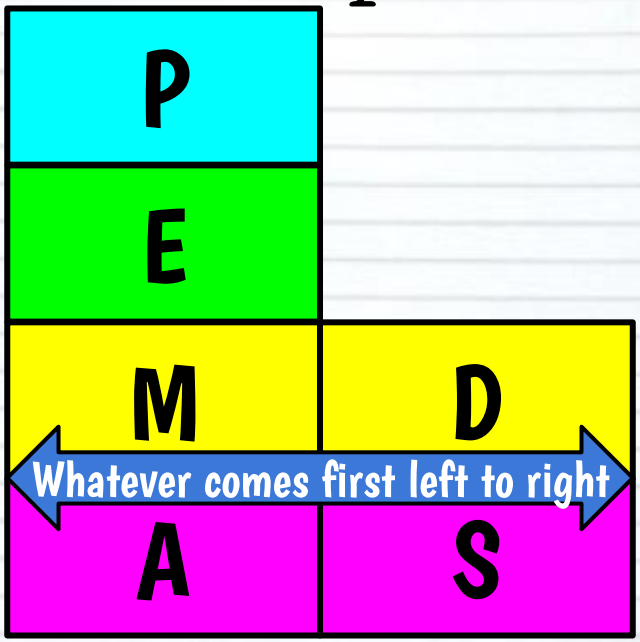
Subtraction

* Fewer
* Remain
* Reduced by
* Difference
* How many More
* Greater than
* Less than
* Withdrawal
* Minus
* Left
* Farther
* Take away

Division

* Divisor
* Equal Pieces
* Dividend
* Divided up
* Distribute Equally
* Equal Pieces
* Quotient
* In each
* Average
* Each
* Cut up
* Groups of

Order of Operations



P - Parenthesis { }, [ ], or ( )

E - Exponents 10^4

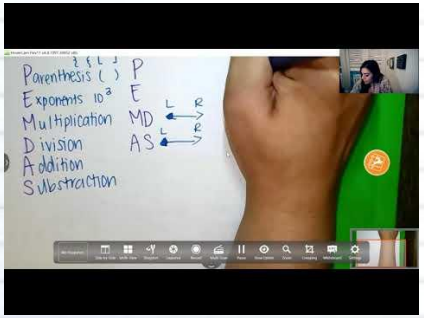
M - Multiplication x, *, or 5(6)

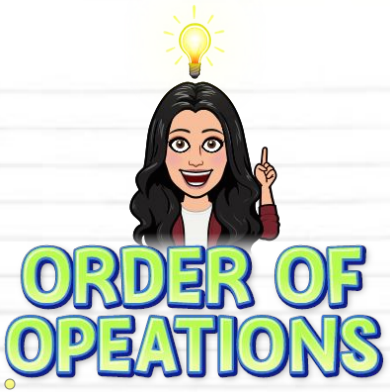
D - Division /, ⌜, ¼, or ➗

A - Addition +

S - Subtraction -

Check out a video here!





Remember to do what is inside the grouping symbols first

$(2 + 2) \times 7$

4×7

$= 28$

$(2 \times 6) \div 3 \times 6$

$12 \div 3 \times 6$

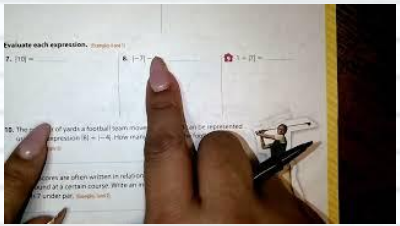
4×6

$= 24$

Chapter 3 Notes

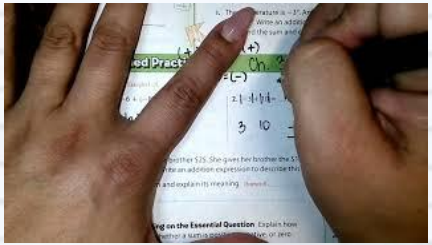
Ch. 3 Lesson 1: Integers and Absolute Value

Check out a video here!



Ch. 3 Lesson 2: Adding Integers

Check out a video here!



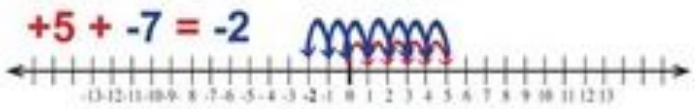
HANDOUT FOR INTERACTIVE NOTEBOOKS OR FOR TEACHING

Adding + & - Integers

Number Line Method

Start by counting to the right the number of + numbers starting at '0' then go left if the number is negative. Red indicates + hops, Blue indicates - hops.

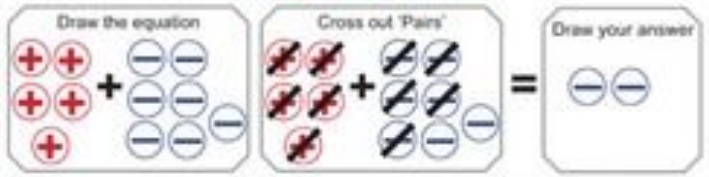
+5 + -7 = -2



Visual Method

Draw circles to model how many + and how many -. Cross out one + to one -. What amount is left is the answer. Remember: It 's like a pair of socks ~ one + and one - cancel each other or make a 'pair' like a pair of socks!

+5 + -7 = -2



Algorithm Method

Look at the numbers. If both numbers are +(positive) then just add. If both numbers are negative then just add the value of the numbers and keep the sign as - for the answer. Is one number in the equation + and one -?.... then....Which one is larger? Has the greatest 'absolute value'? Take the sign of the largest number and take the difference to get your answer.

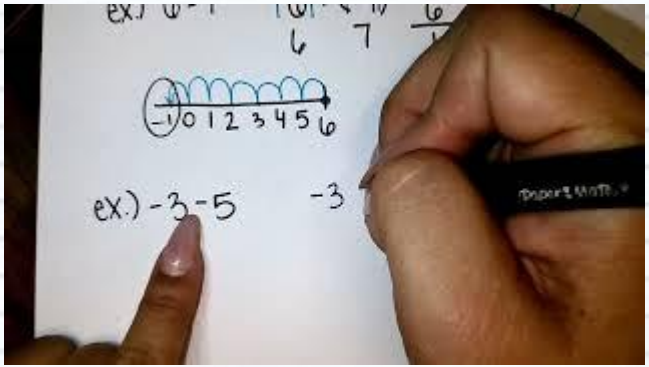
+5 + -7 = -2
7 is larger than 5 so the answer will be - (negative), the difference is 2, so the answer is -2

+9 + -7 = +2
9 is larger than 7 so the answer will be + (positive), the difference is 2, so the answer is +2

-2 + -7 = -9
Both integers are negative (-) so the answer will be -. Then just add the numbers and keep the sign

Ch. 3 Lesson 2: Subtracting Integers

Check out a video here!



Keep the first number the same

12 – (-6) =

12 + 6 = 18

Change the sign of the second number to its' opposite. (In this case, a negative to a positive)

Change the subtraction sign to an addition sign.

So… 12 – (-6) = 18

Subtraction of Integers on a Number Line

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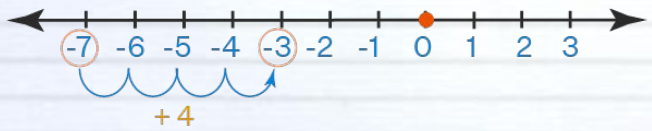
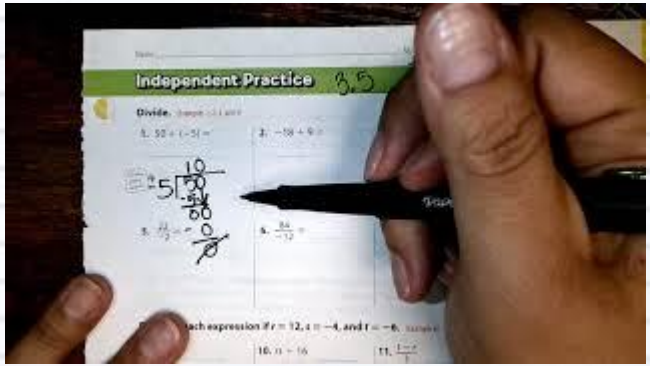


-7 - (-4) = -7 + 4
= -3

Ch. 3 Lesson 4 and 5: Multiplying and Dividing Integers

Check out a video here!



Multiplying & Dividing Integers

1) Signs the same: answer is positive

(+)(+) = (+) (+) ÷ (+) = (+)
(-)(-) = (+) (-) ÷ (-) = (+)

2) Signs different: answer is negative

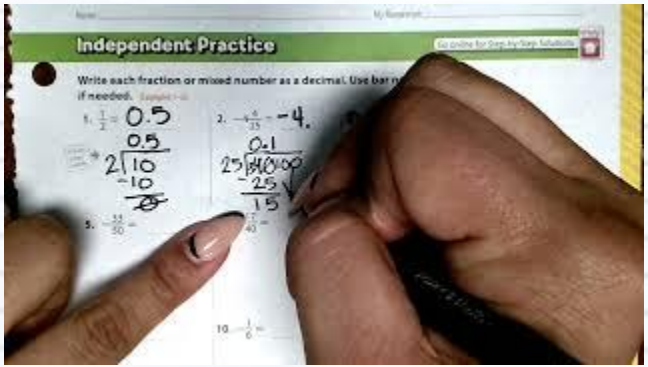
(+)(-) = (-) (+) ÷ (-) = (-)
(-)(+) = (-) (-) ÷ (+) = (-)

* Remember to work 2 numbers at a time *

Chapter 4 Notes

Ch. 4 Lesson 1: Repeating and Terminating Decimals

Check out a video here!



Types of Decimals

FRACTIONS TO DECIMALS

Take the numerator and divide it by the denominator by using _____

$\frac{3}{4}$ ➡ $4\overline{)3}$ ➡ .75

REPEATING

A decimal number that has digits that _____ go on forever.

$\frac{2}{3}$ ➡ .333... $\overline{.3}$

THE DECIMAL _____

TERMINATING

A decimal number that has digits that _____ go on forever.

$\frac{3}{10}$ ➡ .3

THE DECIMAL _____

Percentage to Decimal Conversion

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2.5%

00.02.5 Shift the decimal point to two places towards left

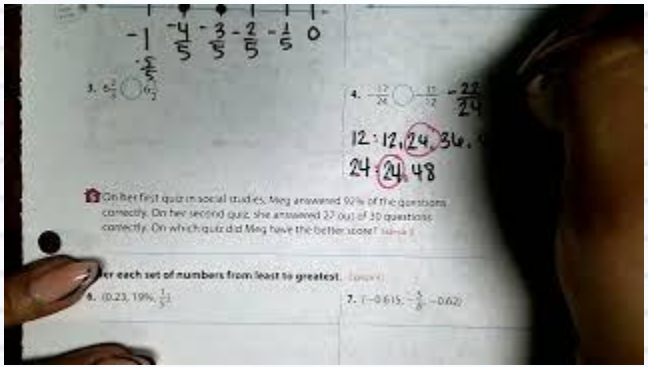
= 0.025

2.5% = 0.025

(In Percent) (In Decimal)

Ch. 4 Lesson :2 Compare and Order Rational Numbers

Check out a video here!



Percentage to Decimal Conversion

cuemath THE MATH EXPERT

2.5%

00.02.5 Shift the decimal point to two places towards left

= 0.025

2.5% = 0.025

(In Percent) (In Decimal)

If you **cannot** convert the denominator into a **power of 10**, divide the numerator with the denominator to get your answer.

$\frac{3}{8}$

$$
\begin{array}{r}
0.375 \\
8\overline{)3.000} \\
\underline{24} \\
60 \\
\underline{56} \\
40 \\
\underline{40} \\
0
\end{array}
$$

Ch. 4 Lesson :3 Adding and Subtracting Fractions with Like Denominators

Check out a video here!

Ch. 4 Lesson 4: Adding and Subtracting Fractions with Unlike Denominators

Check out a video here!

2.1 and 2.3: ADDING AND SUBTRACTING FRACTIONS

STEPS TO SUCCESSFUL ADDING AND SUBTRACTING FRACTIONS:

Fractions need a COMMON DENOMINATOR to be added or subtracted!!!

1. Change all mixed fractions to improper fractions.
2. Create a common denominator.
3. Follow same steps of adding and subtracting integers.

Example 3:

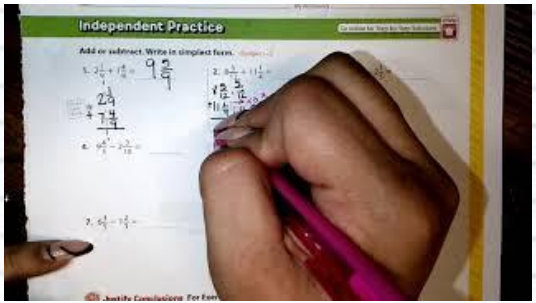
1. $-\frac{4}{7}+\left(-\frac{1}{7}\right)=-\frac{4}{7}-\frac{1}{7}$
$=\frac{-4-1}{7}=\mathbf{-\frac{5}{7}}$

2. $\frac{2}{6}+\frac{1}{3}=\frac{2}{6}+\frac{2}{6}=\frac{2+2}{6}$
$=\frac{4}{6}=\mathbf{\frac{2}{3}}$

3. $-\frac{4}{15}+\frac{2}{5}=-\frac{4}{15}+\frac{6}{15}$
$=-\frac{-4+6}{15}=\mathbf{\frac{2}{15}}$

Ch. 4 Lesson 5: Adding and Subtracting Mixed Numbers

Check out a video here!



Adding and subtracting / mixed numbers.

1. Convert mixed numbers to fractions

$$3\frac{1}{4} - 1\frac{3}{5} = \frac{13}{4} - \frac{8}{5} =$$

2. Find the LCM and subtract

$$\frac{65}{20} - \frac{32}{20} = \frac{33}{20} =$$

3. Convert back to a mixed number

$$1\frac{13}{20}$$

Subtracting Mixed Numbers (with Regrouping)

$$\begin{array}{r} {\scriptstyle 11} \\ 12\tfrac{2}{11} + \tfrac{11}{11} = \tfrac{13}{11} \\ -\ 4\tfrac{9}{11} \\ \hline 7\tfrac{4}{11} \end{array}$$

1. ALWAYS subtract fractions first: But I can't subtract 9 from 2!

$$\frac{2}{11} - \frac{9}{11}$$

2. Borrow 1 from the whole number and add it to your first fraction.

$$12\tfrac{2}{11} + \tfrac{11}{11} = \tfrac{13}{11}$$

3. Subtract the fractions

$$\begin{array}{r} \tfrac{13}{11} \\ -\ \tfrac{9}{11} \\ \hline \tfrac{4}{11} \end{array}$$

4. Subtract the whole numbers

$$\begin{array}{r} 11 \\ -\ 4 \\ \hline 7 \end{array}$$

Answer: $7\frac{4}{11}$

Regroup the whole as a fraction with the same denominator. Since the denominator is ninths 1 whole = $\frac{9}{9}$

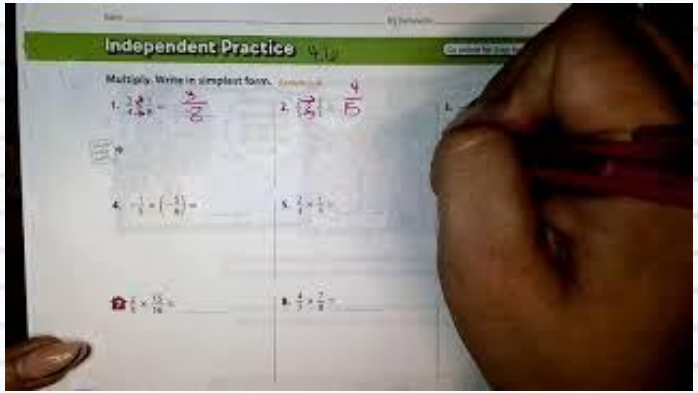
Regrouping $\frac{9}{9}$ plus the $\frac{3}{9}$ you started with gives you $\frac{12}{9}$

$$2\tfrac{3}{9} + \tfrac{9}{9} = 2\tfrac{12}{9}$$

$$\begin{array}{r} 2\tfrac{3}{9} \\ -\ 1\tfrac{5}{9} \\ \hline \end{array} = \begin{array}{r} 2\tfrac{3}{9} \\ -\ 1\tfrac{5}{9} \\ \hline 1\tfrac{7}{9} \end{array}$$

Ch. 4 Lesson 6
Multiply Fractions

Check out a video here!



Multiply the numerators $\frac{2}{5} \times \frac{3}{4} = \frac{6}{\ }$

Multiply the denominators $\frac{2}{5} \times \frac{3}{4} = \frac{6}{20}$

Reduce the fraction if necessary $\frac{6}{20} = \frac{3}{10}$

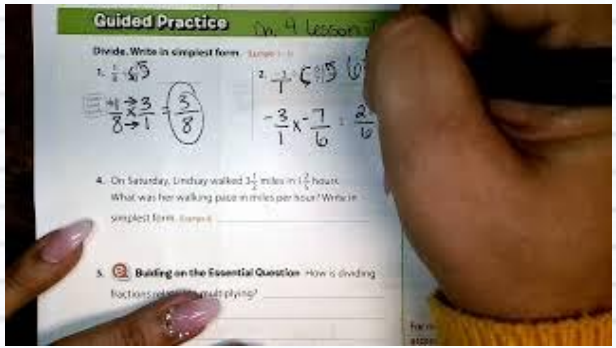
MULTIPLYING FRACTIONS

Remember! 1.Multiply 2.Multiply 3.Simplify

	Fraction multiplied by a fraction	Whole number multiplied by a fraction	Fraction multiplied by a mixed number
Step 1: Write whole number as fraction; write mixed number as improper fraction.	$\frac{2}{3} \times \frac{3}{4}$	$9 \times \frac{2}{5}$ → $\frac{9}{1} \times \frac{2}{5}$	$2\frac{1}{3} \times \frac{2}{3}$ → $\frac{7}{3} \times \frac{2}{3}$
Step 2: Multiply the numerators	$\frac{2}{3} \times \frac{3}{4} = \frac{6}{\ }$	$\frac{9}{1} \times \frac{2}{5} = \frac{18}{\ }$	$\frac{7}{3} \times \frac{2}{3} = \frac{14}{\ }$
Step 3: Multiply the denominators	$\frac{2}{3} \times \frac{3}{4} = \frac{6}{12}$	$\frac{9}{1} \times \frac{2}{5} = \frac{18}{5}$	$\frac{7}{3} \times \frac{2}{3} = \frac{14}{9}$
Step 4: Write answer in simplest terms	$\frac{6}{12} = \frac{1}{2}$	$\frac{18}{5} = 3\frac{3}{5}$	$\frac{14}{9} = 1\frac{5}{9}$

Ch. 4 Lesson 8
Dividing Fractions

Check out a video here!



Dividing fractions

Multiply by the reciprocal of the divisor.

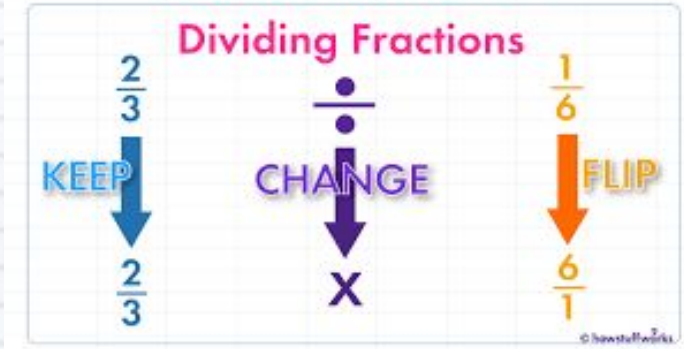
$$\frac{3}{4} \div \frac{1}{8}$$

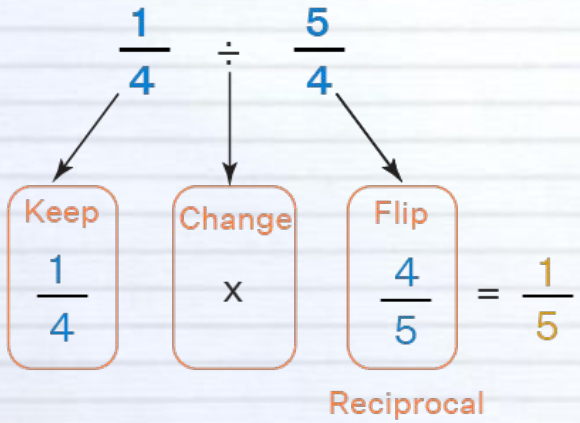
$$\frac{3}{4} \times \frac{8}{1}$$

Find the product and simplify

$$\frac{3}{4} \times \frac{8}{1} = \frac{24}{4}$$

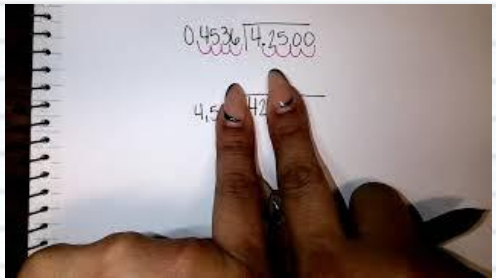
$$= 6$$





Ch. 4 Lesson : 7 Customary & Metric Conversions

Check out a video here!



Customary to Metric Conversion		
Length	**Weight/Mass**	**Capacity**
1 inch = 2.54 centimeters 1 foot ≈ 0.305 meter 1 yard ≈ 0.914 meter 1 mile ≈ 1.61 kilometers	1 ounce ≈ 28.3 grams 1 pound ≈ 0.454 kilogram	1 fluid ounce ≈ 29.6 milliliters 1 quart ≈ 0.946 liter 1 gallon ≈ 3.79 liters

Metric to Customary Conversion		
Length	**Weight/Mass**	**Capacity**
1 centimeter ≈ 0.39 inch 1 meter ≈ 3.28 feet 1 meter ≈ 1.09 yards 1 kilometer ≈ 0.621 mile	1 gram ≈ 0.035 ounce 1 kilogram ≈ 2.20 pounds	1 milliliter ≈ 0.034 fluid ounce 1 liter ≈ 1.06 quarts 1 liter ≈ 0.264 gallon

Chapter 1 Notes

Ch. 1 Lesson : 1 Rates

Check out a video here!

Convert to Unit Rates:

$\frac{6 \text{ miles}}{3 \text{ hours}}$

$\frac{6 \div 3}{3 \div 3}$

$= \frac{2 \text{ mi.}}{1 \text{ hr.}}$

=2 mi./hr.

$\frac{40 \text{ words}}{2 \text{ min.}}$

$\frac{40 \div 2}{2 \div 2}$

$= \frac{20 \text{ words}}{1 \text{ min.}}$

=20 words/min.

$\frac{5 \text{ miles}}{2 \text{ hours}}$

$\frac{5 \div 2}{2 \div 2}$

=2.5 mi./hr.

Unit Rates:

ratios that compare
✕ units of one quantity to
1 unit of another quantity

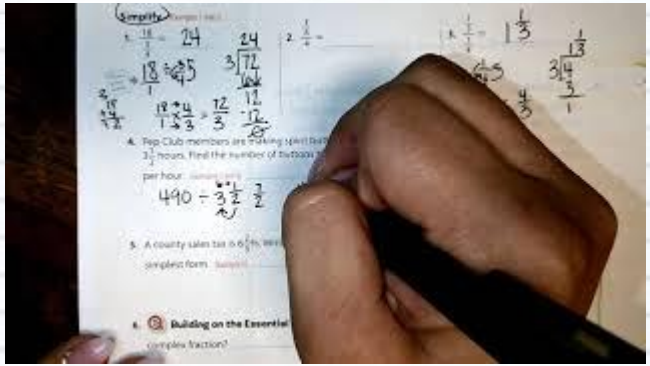
Examples:

2 cats : 1 dog → "2 cats for every dog"

37 jelly beans : 1 bag → "37 jelly beans per bag"

Ch. 1 Lesson : 2 Complex Fractions and Rates

Check out a video here!



$$\frac{1}{9} \text{ numerator}$$

$$\frac{\quad}{\quad} \leftarrow \text{main division}$$

$$\frac{2}{7} \text{ denominator}$$

Complex Fractions -

a fraction whose numerator, denominator or both are fractions.

We want to get a unit rate, which means we want a denominator of 1.

Normally that means dividing by the denominator, but since its a fraction, we multiply by its reciprocal instead.

$\frac{\frac{1}{4}}{2}$ $\quad \frac{1}{4} \div \frac{2}{1}$ $\quad \frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$

$\frac{1}{\frac{2}{7}}$ $\quad \frac{1}{2} \cdot \frac{7}{2}$ $\quad \frac{7}{14}$

$\frac{3}{\frac{3}{5}}$ $\quad \frac{3}{1} \div \frac{3}{5}$ $\quad \frac{3}{1} \times \frac{5}{3} = \frac{5}{1} = 5$

Simplifying a complex fraction means making both the numerator and denominator into integers.

Ch. 1 Lesson : 3
Convert Unit Rates

Check out a video here!

Convert 5 *gallons* to *cups*.

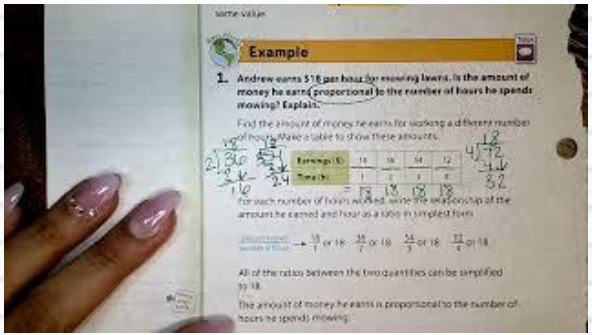
$$\frac{5\ \cancel{gallons}}{1} \times \frac{16\ cups}{1\ \cancel{gallon}} =$$

Customary Units of Measure	
Smaller	**Larger**
12 inches	1 foot
16 ounces	1 pound
8 pints	1 gallon
3 feet	1 yard
5,280 feet	1 mile

Metric Units of Measure	
Smaller	**Larger**
100 centimeters	1 meter
1,000 grams	1 kilogram
1,000 milliliters	1 liter
10 millimeters	1 centimeter
1,000 milligrams	1 gram

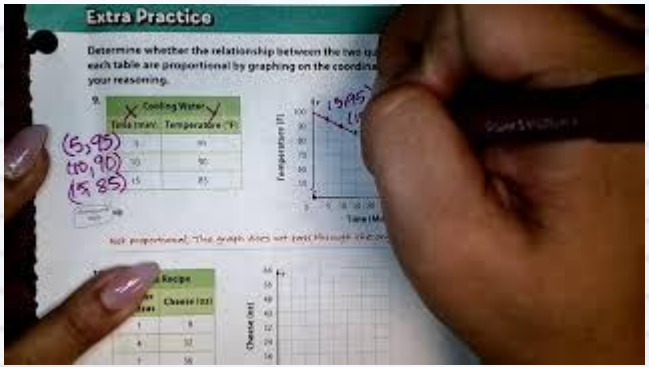
Ch. 1 Lesson : 4
Proportional Vs. Not Proportional

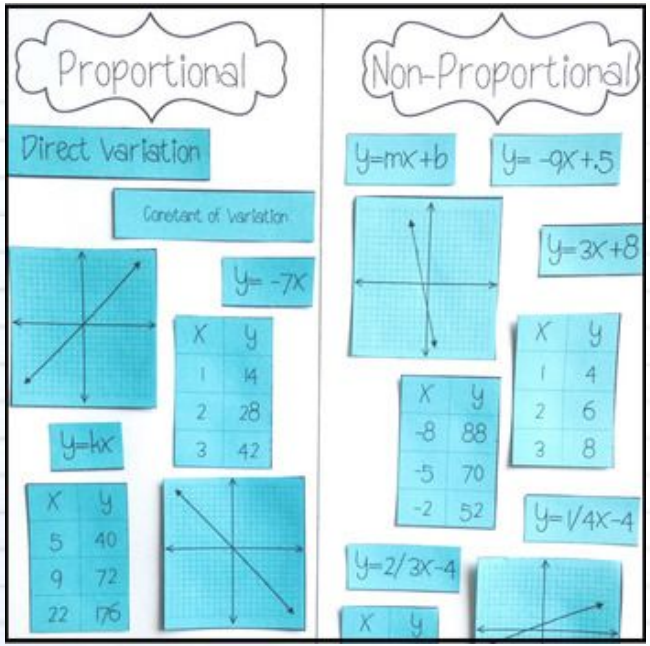
Check out a video here!



Ch. 1 Lesson : 5
Graph Proportional Relationships

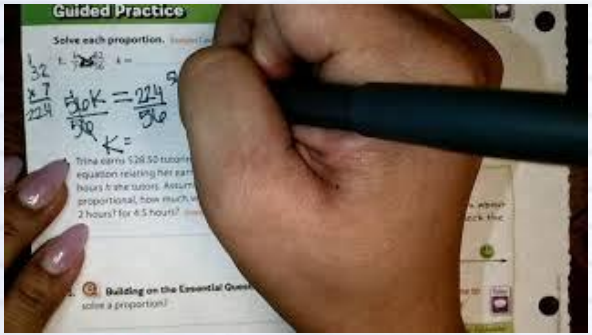
Check out a video here!





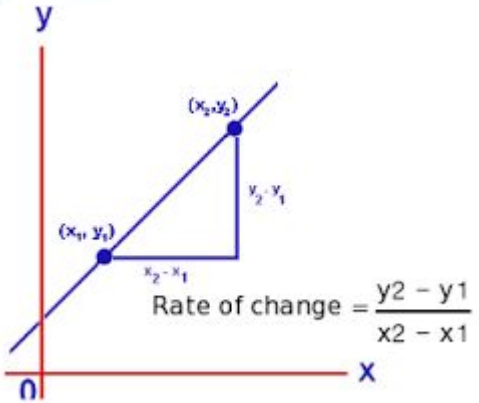
Ch. 1 Lesson : 6
Solve Proportional Equations

Check out a video here!



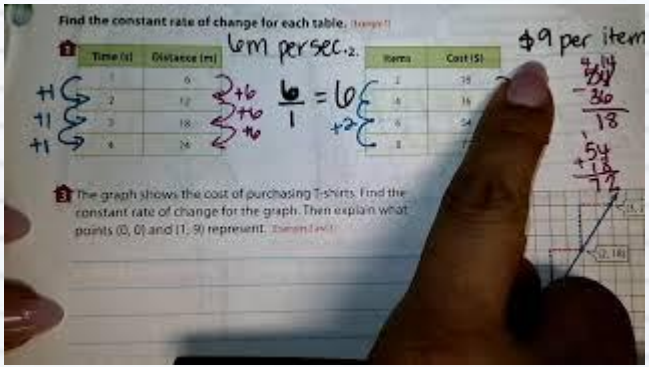
Ch. 1 Lesson : 7
Constant Rate of Change

Check out a video here!



Ch. 1 Lesson : 8
Slope

Check out a video here!



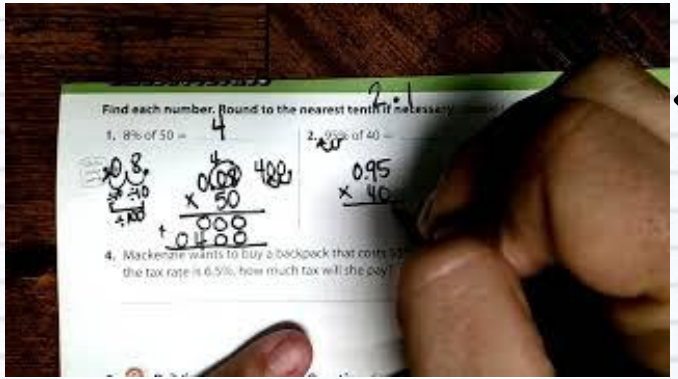
Ch. 1 Lesson : 9
Direct Variation

Check out a video here!

Chapter 2 Notes

Ch. 2 Lesson : 1
Find the Percent of a Number

Check out a video here!



$50 ; 15% off

15% = 0.15

$50 × 0.15 = $7.50

$50 − $7.50 = $42.50

3 ways to solve Percent of a Number Problems

Multiply by a Decimal

Find 5% of 180

5% = 0.05

0.05 x 180 = 9

Use Proportional Reasoning

Find 30% of 400

30% = 30/100

$\frac{30}{100} \overset{\times 4}{} = \frac{?}{400}$

? = 120

Multiply by a fraction

Find 135% of 60

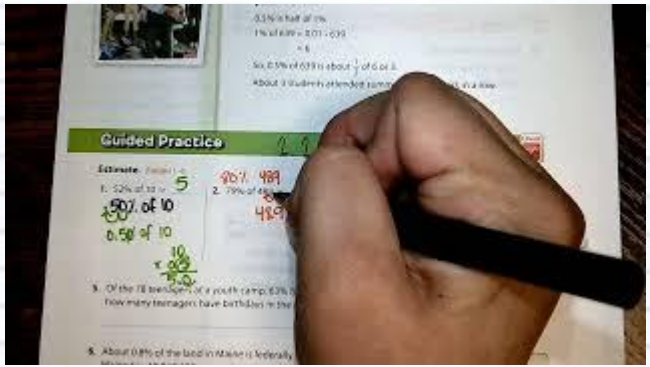
135% = 135/100

60 = 60/1

$\frac{135}{100} \times \frac{60}{1} = \frac{810}{10} = 81$

Ch. 2 Lesson 2 :
Estimate the Percent of a Number

Check out a video here!



Estimate Using Compatible Numbers

8% of 868

↓ ↓

10% of 870

87.0

3 ways to solve Percent of a Number Problems

Multiply by a Decimal

Find 5% of 180

5% = 0.05

0.05 x 180 = 9

Use Proportional Reasoning

Find 30% of 400

30% = 30/100

$\frac{30}{100} \overset{\times 4}{=} \frac{?}{400}$

? = 120

Multiply by a fraction

Find 135% of 60

135% = 135/100

60 = 60/1

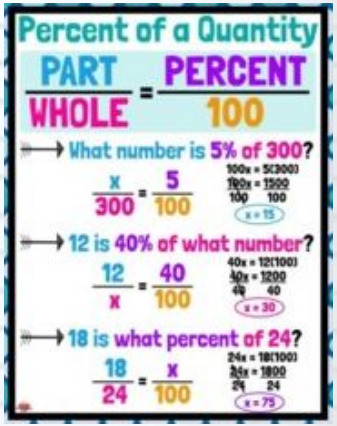
$\frac{135}{100_{10}} \times \frac{60^{6}}{1} = \frac{810}{10} = 81$

Ch. 2 Lesson 3 and 4 : Percent of a Number

Check out a video here!

$$\frac{\text{part}}{\text{whole}} = \frac{\%}{100}$$

$$\frac{\text{is}}{\text{of}} = \frac{\%}{100}$$



Solving Word Problems with Percents

Taylor gave Tobin 35% of the rings in her jewelry collection for Christmas. If Taylor started with 20 rings, how many did she give Tobin?

Step 1: Identify KNOWNS and UNKNOWN

Taylor gave Tobin 35% of the rings in her jewelry collection for Christmas. If Taylor started with 20 rings, how many did she give Tobin?

Step 2: Plug values into proportion

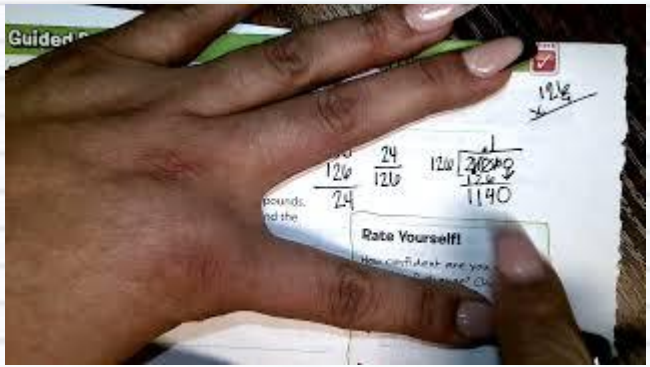
$$\frac{\text{PART}}{\text{TOTAL}} = \frac{\text{PERCENT}}{100} \rightarrow \frac{x}{20} = \frac{35}{100}$$

Step 3: Solve proportion

$$\frac{x}{20} = \frac{35}{100} \rightarrow 100x = 700 \rightarrow x = 7 \text{ rings}$$

Ch. 2 Lesson 5 : Percent of Change

Check out a video here!



Calculating Percent Change

Calculate the percent change:

107 ← Starting Value

86 ← Final Value

STEP 1: Find the absolute value of the difference

Starting Final

$|107 - 86| = |21| = 21$

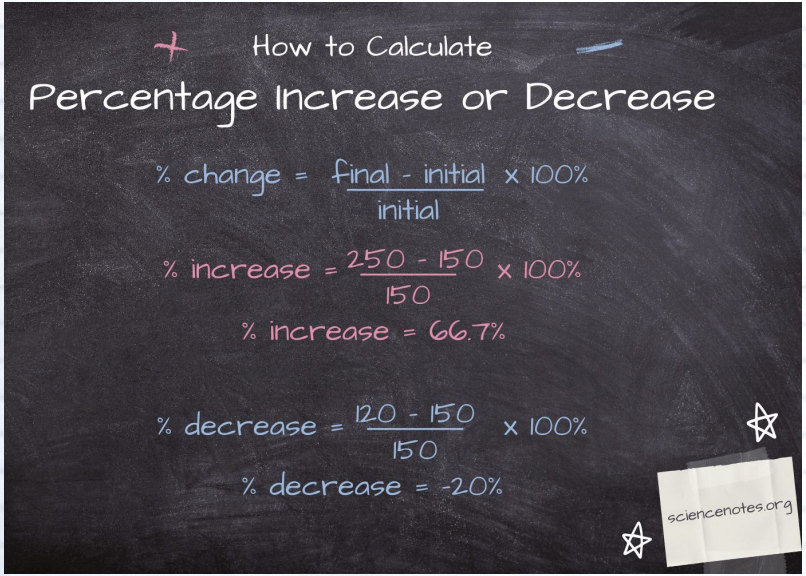
STEP 2: Divide by the starting value.

Starting

$21 \div 107 = 0.196$ ← Express as a decimal

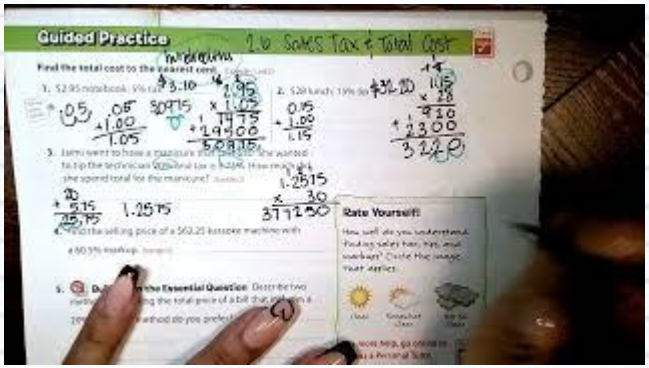
STEP 3: Multiply by 100

$0.196 \times 100 = 19.6\%$ change



Ch. 2 Lesson 6 : Sales Tax & Total Cost

Check out a video here!



HOW MUCH DID JASMINE PAY IN TOTAL?

a = total cost

$a = 54 + (0.08 \cdot 54)$

cost of jeans | sales tax

$a = 54 + 4.32$

$a = \$58.32$

Calculate 20% Tip

Before Tip	
SUBTOTAL	12.74
TAX 7%	0.89
TOTAL	13.63
TIP	____
TOTAL	____

After Tip	
SUBTOTAL	12.74
TAX 7%	0.89
TOTAL	13.63
TIP	2.73
TOTAL	$16.36

Step 1: Find 10%

13.63 TOTAL

13.63 MOVE DECIMAL

1.363 10% OF TOTAL

Step 2: Double it

$1.363 \times 2 = 2.726$

Step 3: Round

$2.726 \approx 2.73$

CALCULATING SALES TAX

Shirt $15.99 × Sales Tax 7% = $1.12

Shirt $15.99 + Sales Tax $1.12 = Total Cost $17.11

Ch. 2 Lesson 7 : Discounts

Check out a video here!

$$\begin{array}{r} 7.99 \\ \times \quad .2 \\ \hline 1.598 \end{array}$$ Girls Shirt — Extra 20% discount

$$\begin{array}{r} 7.99 \\ - \quad 1.59 \\ \hline 6.40 \end{array}$$ Subtract 20% discount from the sale price

$6.40 — New price with 20% discount

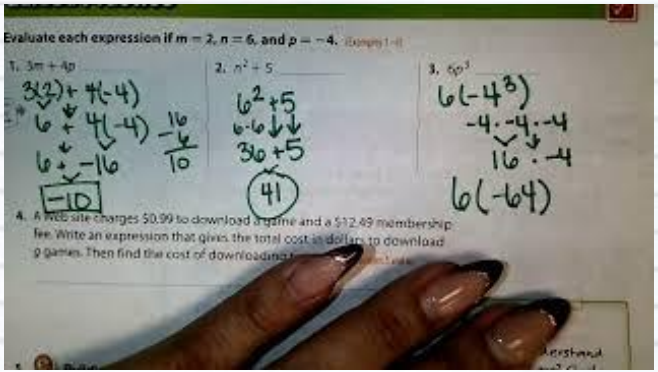
$$\begin{array}{r} 6.4 \\ \times \quad .07 \\ \hline \$0.448 \end{array}$$ Find the Sales Tax — Sales Tax

$$\begin{array}{r} 6.40 \\ + \quad 0.45 \\ \hline \$6.85 \end{array}$$ Add Sales Tax — Final price

Chapter 5 Notes

Ch. 5 Lesson : 1
Evaluate Expressions

Check out a video here!



Numerical Expression	Word Expression
8 x 43 – 13	Eight times 43 minus 13.
8 x (43 – 13)	8 times the difference of 43 and 13.
12 × (5 + 25)	12 times the sum of 5 and 25.
(20 × 3) + (5 × 3)	The sum of 3 twenties and 3 fives.

evaluate an algebraic expression

To evaluate an algebraic expression means to find a numerical value for it, given particular values.

evaluating expressions … given z = 10

$6 + z$

$6 + z = 6 + 10$
$= 16$

$5z$

$5z = 5 \times 10$
$= 50$

$20 - z$

$20 - z = 20 - 10$
$= 10$

z^2

$z^2 = 10 \times 10$
$= 100$

evaluating expressions … given a = 2

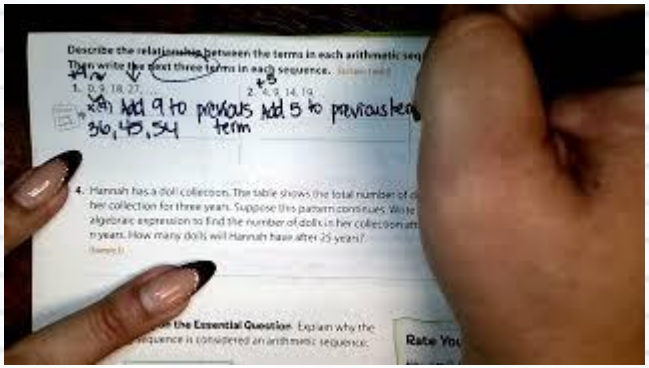
$4(a + 4)$

If a = 2:
$4(a + 4)$
$= 4(2 + 4)$
$= 8 + 16$
$= 24$

$a^2 + 2ab + b^2$

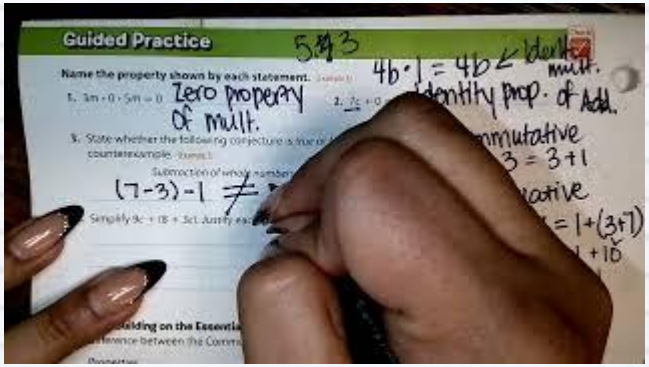
If a = 1, b = 2:
$a^2 + 2ab + b^2$
$= 1^2 + (2 \times 1 \times 2) + 2^2$
$= 1 + 4 + 4$
$= 9$

Ch. 5 Lesson : 2
Find a Pattern in a Sequence
Check out a video here!

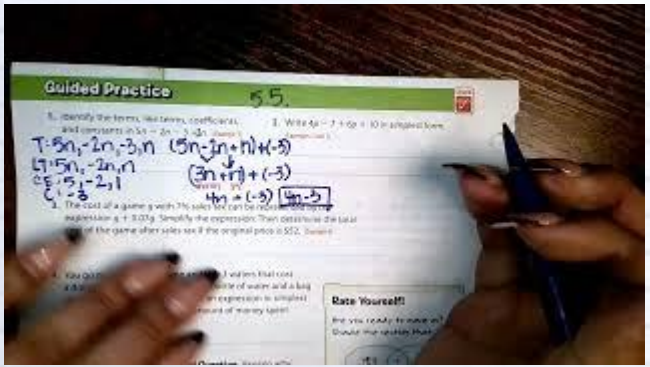


Ch. 5 Lesson : 4
Distributive Property
Check out a video here!

Ch. 5 Lesson : 3
Properties & Operations
Check out a video here!



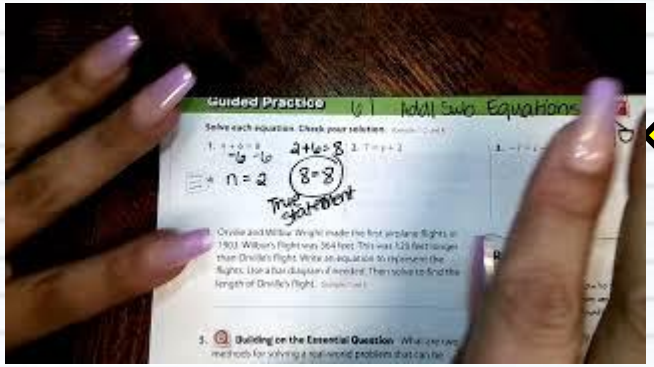
Ch. 5 Lesson : 5
Parts of an Expression
Check out a video here!



Chapter 6 Notes

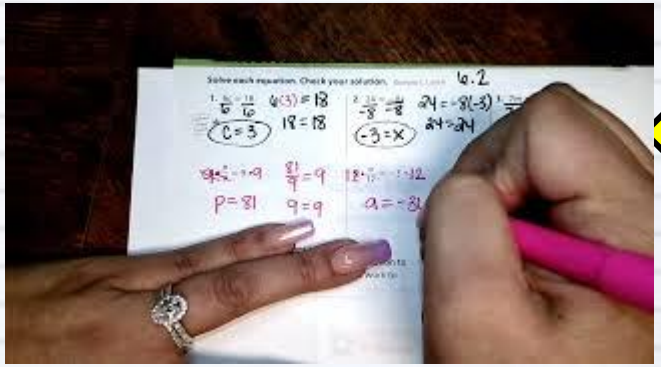
Ch. 6 Lesson : 1
Add and Subtract Equations

Check out a video here!



Ch. 6 Lesson : 2
Multiply and Divide Equations

Check out a video here!



SOLVING ONE STEP EQUATIONS

+

$5 + x = -10$

$-5 \quad -5$

$x = -15$

$5 + -15 = 10$ ✓

−

$x - 7 = -10$

$+7 \quad +7$

$x = -3$

$-3 - 7 = -10$ ✓

×

$-5x = 10$

$\div -5 \quad \div -5$

$x = -2$

$5 \times 2 = 10$ ✓

÷

$\frac{x}{-5} = 10$

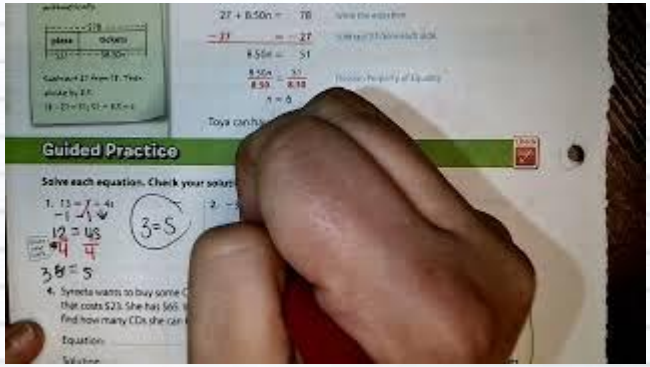
$\times \frac{-5}{1} \quad \times \frac{-5}{1}$

$x = -50$

$-50 \div 5 = 10$ ✓

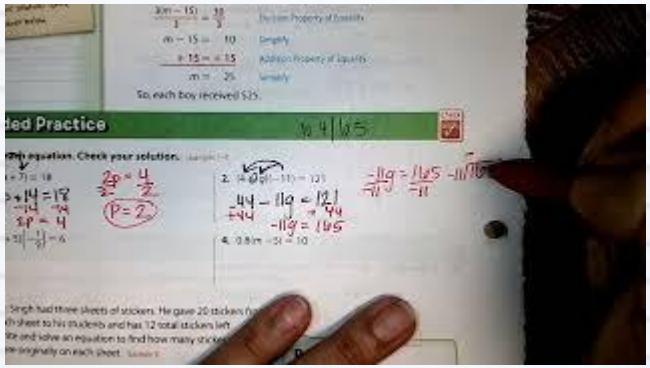
Ch. 6 Lesson : 5

Check out a video here!



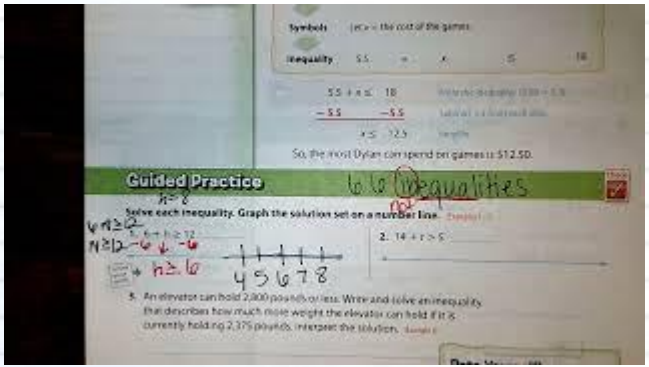
Ch. 6 Lesson : 6

Check out a video here!



Ch. 6 Lesson : 7

Check out a video here!



Ch. 6 Lesson : 8

Check out a video here!

Chapter 7 Notes

Ch. 7 Lesson : 1
Classify Angles

Check out a video here!

Angle Pair Relationships

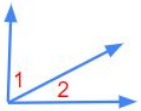
Adjacent Angles

Angles 1 and 2 are adjacent angles.
They share a common side.

Vertical Angles

Angles 1 and 2 are vertical angles.
They are congruent (equal in size).
Angles 3 and 4 are also vertical angles.

Complementary Angles



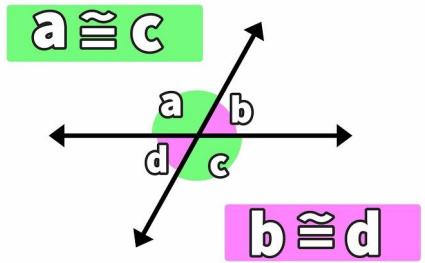
Angles 1 and 2 are complementary angles.
They have a sum of 90°.

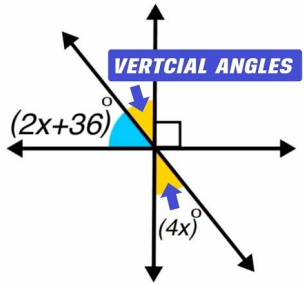
Supplementary Angles

Angles 1 and 2 are supplementary angles.
They have a sum of 180°.

Acute angle:	Obtuse angle:	Right angle:	Straight angle:
less than 90° and greater than 0°	less than 180° and greater than 90°	equal to 90°	equal to 180°
			

Vertical Angles

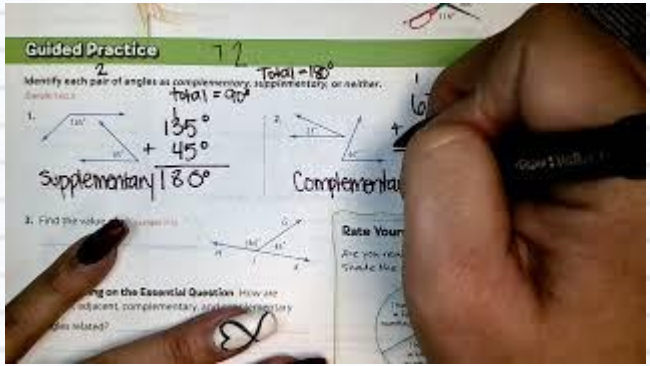




mashupmath

Ch. 7 Lesson : 2
Complementary and Supplementary Angles

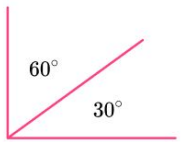
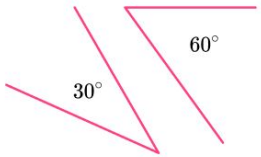
Check out a video here!



Complementary Angles

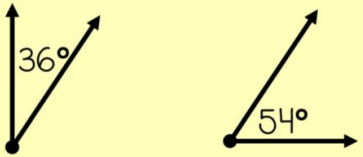
Complementary angles are two angles that add up to 90 degrees.
They can be adjacent or not adjacent.

Example

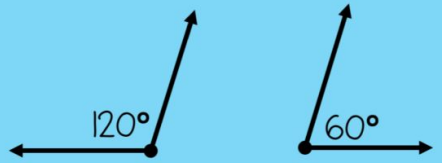
Adjacent complementary angles	Non-adjacent complementary angles
	

COMPLEMENTARY & SUPPLEMENTARY ANGLES

Complementary Angles: Two angles that add to equal 90°



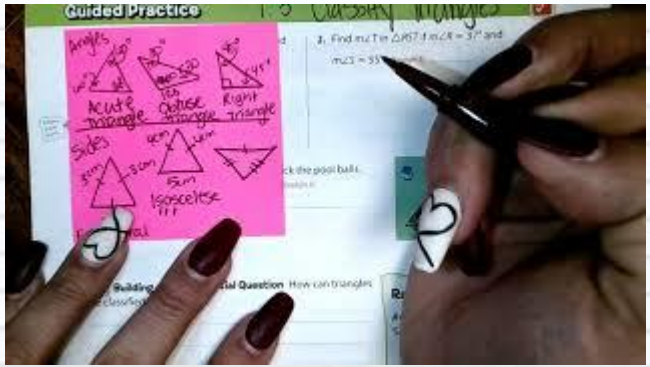
Supplementary Angles: Two angles that add to equal 180°



Lindsay Bowden

Ch. 7 Lesson : 3
Classify Triangles

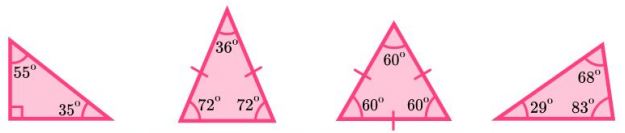
Check out a video here!



Angles in a Triangle

Angles in a triangle refers to the sum (total) of the angles at each vertex in a triangle. The sum of the interior angles of a triangle is **180°.**

E.g.



Right angled triangle	**Isosceles triangle**	**Equilateral triangle**	**Scalene triangle**
One right angle	Two equal sides & angles	Three equal sides & angles	All sides & angles different
90+55+35 = 180°	72+72+36 = 180°	60+60+60 = 180°	83+68+29 = 180°

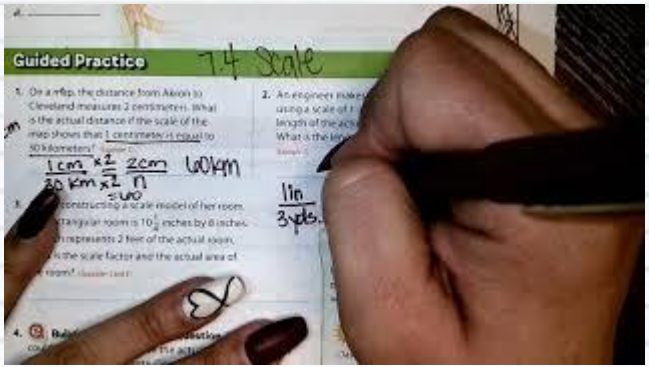
THIRD SPACE LEARNING

TYPES OF TRIANGLES

by angles:	by sides:
acute	**equilateral**
A triangle with three acute angles (<90°).	A triangle with three equal length sides.
right	**isosceles**
A triangle with one right angle (exactly 90°).	A triangle with two equal length sides.
obtuse	**scalene**
A triangle with one obtuse angle (> 90°)	A triangle with all different length sides.

Ch. 7 Lesson : 4
Scale

Check out a video here!



Scale Drawing

scale: 2 in to 5 ft

$$\frac{2\text{ in}}{5\text{ ft}} = \frac{8.5\text{ in}}{}$$

Scale = 1:5

Real Giraffe
150 inches high

Drawn Giraffe
30 inches high

Ch. 7 Lesson : 5
Draw 3d Figures

Check out a video here!