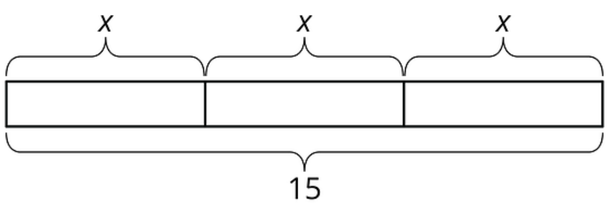
Equations in One Variable

Grade6-6-Unit-family-support-materials.pdf

Grade 6, Unit 6 Expressions and Equations

a **variable** is a letter to represent a number whose value is unknown. Diagrams can help us make sense of how quantities are related. Here is an example of such a diagram:



Since 3 pieces are labeled with the same variable x, we know that each of the three pieces represents the same number. Some equations that match this diagram are $x + x + x = 15$ and $15 = 3x$.

A **solution** to an equation is a number used in place of the variable that makes the equation true. In the previous example, the solution is 5. Think about substituting 5 for x in either equation: $5 + 5 + 5 = 15$ and $15 = 3 \cdot 5$ are both true. We can tell that, for example, 4 is *not* a solution, because $4 + 4 + 4$ does not equal 15.

Solving an equation is a process of finding a solution. Your student will learn that an equation $15 = 3x$ can be solved by dividing each side by 3. Notice that if you divide each side by 3, $15 \div 3 = 3x \div 3$, you are left with $5 = x$, the solution to the equation.

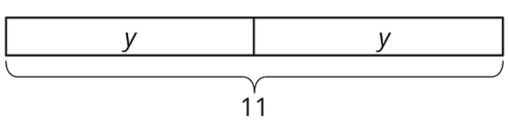
Practice Problems:

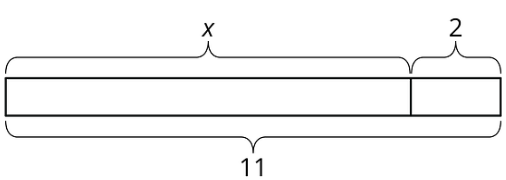
Draw a diagram to represent each equation. Then, solve each equation.

1. $2y = 11$

2. $11 = x + 2$

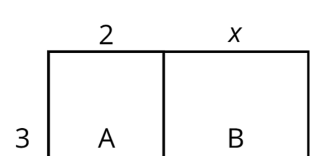
Solution:





1. $y = 5.5 \ or \ y = \frac{11}{2}$
2. $x = 9$

Equal and Equivalent



This week your student is writing mathematical expressions, especially expressions using the distributive property.

In this diagram, we can say one side length of the large rectangle is 3 units and the other is $x + 2$ units. So, the area of the large rectangle is $3(x + 2)$. The large rectangle can be partitioned into two smaller rectangles, A and B, with no overlap. The area of A is 6 and the area of B is $3x$. So, the area of the large rectangle can also be written as $3x + 6$. In other words,

$$3(x + 2) = 3x + 3 \cdot 2$$

This is an example of the distributive property.

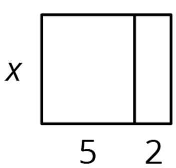
Practice Problems

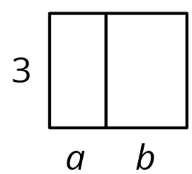
Draw and label a partitioned rectangle to show that each of these equations is always true, no matter the value of the letters.

1. $5x + 2x = (5 + 2)x$
2. $3(a + b) = 3a + 3b$

Solution:

Answers vary. Sample responses:





Relationships Between Quantities

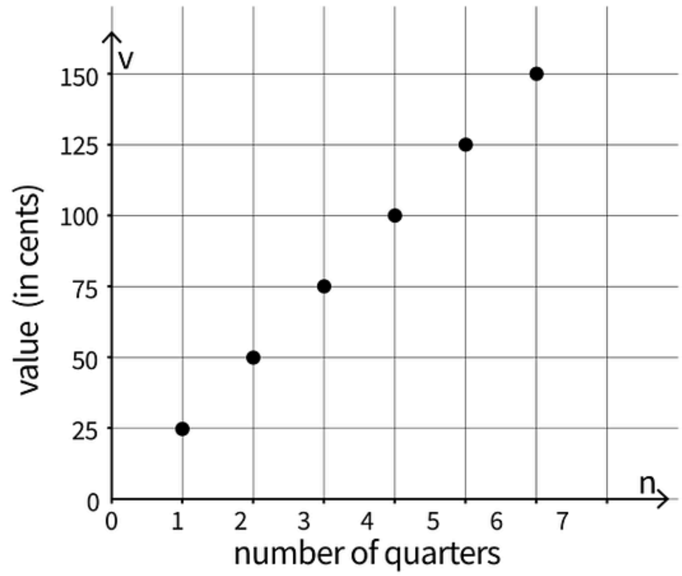
For example, since a quarter is worth 25¢, we can represent the relationship between the number of quarters, n, and their value v in cents like this:

$$v = 25n$$

We can also use a table to represent the situation.

n	v
1	25
2	50
3	75

Or we can draw a graph to represent the relationship between the two quantities:



The independent variable is used to calculate the value of another variable.

The dependent variable is the result of a calculation.

The dependent variable is the value *v* in cents because it is the result of multiplying 25 by *n*, the number of quarters.

Practice Problems:

A shopper is buying granola bars. The cost of each granola bar is $0.75.

1. Write an equation that shows the cost of the granola bars, c, in terms of the number of bars purchased, n.
2. Create a graph representing associated values of c and n.
3. What are the coordinates of some points on your graph? What do they represent?

Solutions

1. $c = 0.75n$. Every granola bar costs $0.75 and the shopper is buying n of them, so the cost is $0.75n$.
2. Answers vary. One way to create a graph is to label the horizontal axis with the "number of bars" with intervals, 0, 1, 2, 3, etc, and label the vertical axis with "total cost in dollars" with intervals 0, 0.25, 0.50, 0.75, etc.
3. If the graph is created as described in this solution, the first coordinate is the number of granola bars and the second is the cost in dollars for that number of granola bars. Some points on such a graph are $(2, 1.50)$ and $(10, 7.50)$