

Name: \_\_\_\_\_

Date: \_\_\_\_\_

Block: \_\_\_\_\_

# Measurement and Uncertainty

Differentiated worksheet

Learning objectives:

I can use different mathematical skills to find the accuracy and precision in measurements

Success Criteria:

- Differentiate between accuracy and precision
- Apply the significant figures rules
- Develop a method to deal with scientific notation formula
- Solve mathematical equations
- Use the unit conversion method

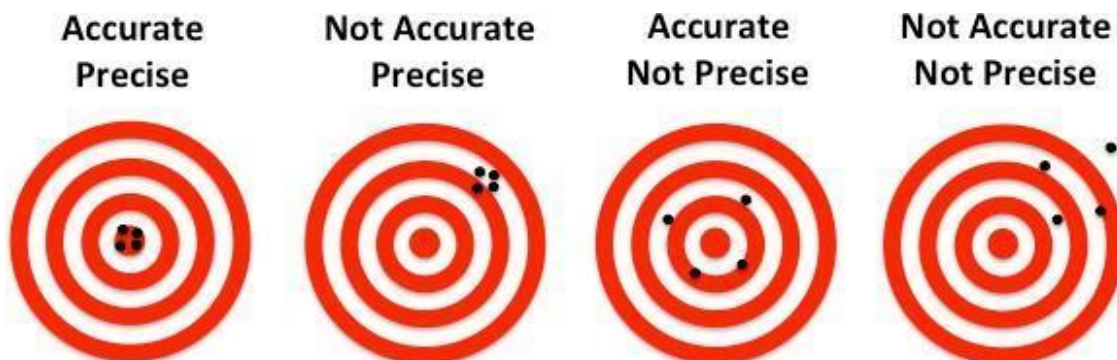
## Moderate achievers, High achievers, Gifted and talented

There is uncertainty in every measurement due to \_\_\_\_\_ of accuracy and precision.

Accuracy: how close the instrument measures to an accepted \_\_\_\_\_.

Precision: how closely two or more measurements of the same thing agree when \_\_\_\_\_

\_\_\_\_\_ care by the same instrument.



Each instrument has its own actual uncertainty that can only be obtained by experiment (i.e. finding the variation in values from repeated measurements).



# Summary

- Accuracy of a measured value refers to how close a measurement is to the correct value. The uncertainty in a measurement is an estimate of the amount by which the measurement result may differ from this value.
- Precision of measured values refers to how close the agreement is between repeated measurements.
- The precision of a *measuring tool* is related to the size of its measurement increments. The smaller the measurement increment, the more precise the tool.
- Significant figures express the precision of a measuring tool.
- When multiplying or dividing measured values, the final answer can contain only as many significant figures as the least precise value.
- When adding or subtracting measured values, the final answer cannot contain more decimal places than the least precise value.

# SIGNIFICANT FIGURES

All Measurements have some degree of uncertainty to them (due to the instrument used.)

To indicate the degree of certainty in a measurement (or a number derived from a measurement), scientists use significant figures. Or numbers they know to be 100% accurate.

**\*\* Significant figures are important in the way we report different kinds of data!**

A significant figure is a **measured** or **meaningful digit**

## A. What is Not Significant?

Defined or counting numbers: A number which involves things which cannot realistically be subdivided.

Example:

1 book; 4 students (cannot have 1.5 books or 4.78 students)

Conversion factors are assumed to be an exact relationship (cannot have 1 kg = 1000.5 kg)

## Rules for identifying # of sig figs:

- a) An exact number (e.g. 25 students) has an infinite number of significant figures because the number was not rounded off. Exact numbers are not used to determine the significant digits.
- b) For all measurements, the following rules apply to count the number of significant figures a number has.

1. Any digit between 1-9 is significant.

e.g. 234.566 has 6 sig figs  
7.4586 has 5 sig figs

2. A '0' at the beginning of a number is **not significant** because it only holds the decimal place. **Leading zeros are NOT significant**

e.g. 0.00045 has 2 sig figs  
0.02333 has 4 sig figs

3. A '0' between two other sig figs is significant.

e.g. 50034.03 has 7 sig figs  
e.g. 534.034201 has 9 sig figs

4. A '0' at the end of a number is only significant IF a decimal point occurs in the number otherwise it is not significant. **Be careful with this one!**

e.g. 750000 has 2 sig figs  
20000000 has 1 sig fig  
e.g. 750.000 has 6 sig figs

Example:

If a balance gives a reading of 97.53 g when a beaker is placed on it, the reading is considered to have 4 significant figures. If the beaker is then put on a different balance and gives a reading of 97.5295 g, there are more significant figures to the measurement (6 significant figures).

How many significant figures do each of the following measurements have?

1. 1.25 kg \_\_\_\_\_

2. 1255 kg \_\_\_\_\_

3. 11s \_\_\_\_\_

4. 150 m \_\_\_\_\_

5. 1.283 cm \_\_\_\_\_

6. 365.249 days \_\_\_\_\_

7. 2 000 000 years \_\_\_\_\_

8. 17.25 L \_\_\_\_\_

## B. Scientific Notation

Scientific Notation is a way of writing numbers for values too large or small to be conveniently written in standard decimal notation.

Example:

$$10 = 1.0 \times 10^1$$

$$25 = 2.5 \times 10^1$$

$$250 = 2.5 \times 10^2$$

$$0.000\,0350\,000 = 3.5000 \times 10^{-5}$$

Write the following numbers in scientific notation: 1.

3570 \_\_\_\_\_

2. 41.400 \_\_\_\_\_

3. 0.000 572 \_\_\_\_\_

4.  $41.50 \times 10^{-4}$  \_\_\_\_\_

5.  $0.000\,410 \times 10^7$  \_\_\_\_\_

### C. Adding or Subtracting Significant Figures

When adding or subtracting significant figures, round off the answer to the least number of decimal places contained in the calculation.

Example:

$$12.56 \text{ cm (2 SF after decimal)} + 125.8 \text{ cm (1 SF after decimal)} = 138.36 \text{ cm} \approx 138.4 \text{ cm (1 SF after decimal)}$$

Exercise:

1.  $15.1 + 75.32$

2.  $178.904\ 56 - 125.8055$

3.  $4.55 \times 10^{-5} + 3.1 \times 10^{-5}$

4.  $1.805 \times 10^4 + 5.89 \times 10^2$

### Multiplying or Dividing Significant Figure

When multiplying or dividing significant figures, round off the answer to the least number of significant figures contained in the calculation.

Example:

$$2.00 \text{ (3 SF)} \times 3.000\ 00 \text{ (6 SF)} = 6.00 \text{ (3 SF)}$$

Exercise:

1.  $12.5 \times 0.50$

2.  $0.15 \times 0.0016$

3.  $40.0 / 30.000$

4.  $2.5 \times 7.500 / 0.150$

5.  $(6.40 \times 10^8) \times (5 \times 10^5)$

6.  $4.37 \times 10^3 / 0.008\ 560\ 0$

7.  $0.51 \times 10^{-4} / 6 \times 10^{-7}$

8.  $0.000\ 01 / 0.1000$

**Summary Practice Exercises:**

In the following mixed calculations, perform multiplications and divisions before doing the additions and subtractions. Keep track of the number of significant figures at each stage of a calculation.

1.  $25.00 \times 0.100 - 15.87 \times 0.1036$

2.  $35.0 \times 1.525 + 50.0 \times 0.975$

3.  $(0.865 - 0.800) \times (1.593 + 9.04)$

4.  $(0.3812 - 0.4176) / (0.0159 - 0.0146)$

5.  $9.34 \times 0.07146 - 6.88 \times 0.08115$

## Significant Figures Worksheet

# Significant Figures

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1. Indicate how many significant figures there are in each of the following measured values.

|         |       |         |       |         |       |
|---------|-------|---------|-------|---------|-------|
| 246.32  | _____ | 1.008   | _____ | 700000  | _____ |
| 107.854 | _____ | 0.00340 | _____ | 350.670 | _____ |
| 100.3   | _____ | 14.600  | _____ | 1.0000  | _____ |
| 0.678   | _____ | 0.0001  | _____ | 320001  | _____ |

2. Calculate the answers to the appropriate number of significant figures.

$$\begin{array}{r} 32.567 \\ 135.0 \\ + 1.4567 \\ \hline \end{array}$$

$$\begin{array}{r} 246.24 \\ 238.278 \\ + 98.3 \\ \hline \end{array}$$

$$\begin{array}{r} 658.0 \\ 23.5478 \\ + 1345.29 \\ \hline \end{array}$$

3. Calculate the answers to the appropriate number of significant figures.

$$\text{a) } 23.7 \times 3.8 = \underline{\hspace{2cm}} \qquad \text{f) } 1.678 / 0.42 = \underline{\hspace{2cm}}$$

$$\text{b) } 45.76 \times 0.25 = \underline{\hspace{2cm}} \qquad \text{g) } 28.367 / 3.74 = \underline{\hspace{2cm}}$$

$$\text{c) } 81.04 \text{ g} \times 0.010 = \underline{\hspace{2cm}} \qquad \text{h) } 4278 / 1.006 = \underline{\hspace{2cm}}$$

$$\text{d) } 6.47 \times 64.5 = \underline{\hspace{2cm}} \qquad \text{i) } (6.8 + 4.7) \times 17.44 = \underline{\hspace{2cm}}$$

$$\text{e) } 43.678 \times 64.1 = \underline{\hspace{2cm}} \qquad \text{j) } (320. - 22.7) \times 3.8 = \underline{\hspace{2cm}}$$

$$\text{k) } \frac{(14.86 + 13.7) \times (65.346 - 4.10)}{(43.888 - 32.888)} = \underline{\hspace{2cm}}$$



**Sig Figs & Units Worksheet**

1. How many significant figures are there in each of the following?

a. 273.16 \_\_\_\_\_

e. 2,000,000 \_\_\_\_\_

i. 5280. \_\_\_\_\_

b. 186,000 \_\_\_\_\_

f. 13.8 \_\_\_\_\_

j. 708.003 \_\_\_\_\_

c. 505 \_\_\_\_\_

g. 0.00928 \_\_\_\_\_

k. 0.0652 \_\_\_\_\_

d. 1000 \_\_\_\_\_

h. 60.080 \_\_\_\_\_

l.  $3.040 \times 10^5$  - \_\_\_\_\_

2. In the following, convert numbers in common notation to scientific notation, or vice versa.

a. 93,000,000 \_\_\_\_\_

d.  $2.997 \times 10^{10}$  - \_\_\_\_\_

b. 0.000019 \_\_\_\_\_

e.  $6.02 \times 10^{-5}$  - \_\_\_\_\_

c. 606.39 \_\_\_\_\_

f.  $2.5359 \times 10^2$  - \_\_\_\_\_

3. In the following, how many decimal places will the solution have? DO NOT SOLVE.

a.  $6.0 \text{ m} + 10.73 \text{ m} + 111.250 \text{ m}$  \_\_\_\_\_d.  $93.4 \text{ cm} + 10.975 \text{ cm}$  \_\_\_\_\_b.  $4050 \text{ L} - 2.06 \text{ L}$  \_\_\_\_\_e.  $0.005070 \text{ cm} + 6.90 \text{ cm} + 2000.860 \text{ cm}$  \_\_\_\_\_c.  $96.75 \text{ km} + 108.43 \text{ km} + 77 \text{ km}$  \_\_\_\_\_f.  $10.970 \text{ mL} - 5.0 \text{ mL}$  \_\_\_\_\_

4. In the following, how many digits should be in the solution to have the proper number of sig figs? DO NOT SOLVE.

a.  $(797.6 \text{ m})(54 \text{ m})$  \_\_\_\_\_d.  $93.4 \text{ m} \div 10.975 \text{ m}$  \_\_\_\_\_b.  $(851 \text{ cm})(24.3 \text{ cm})$  \_\_\_\_\_e.  $(6.02 \times 10^{23} \text{ m})(12.00 \text{ m})(1.660 \times 10^{-24} \text{ m})$  \_\_\_\_\_c.  $1075 \text{ kg} \div 15 \text{ L}$  \_\_\_\_\_f.  $(453.6 \text{ m})(9.050 \times 10^4 \text{ m})(239.1 \text{ m})$  \_\_\_\_\_

Solve the following problems, expressing the answer in the proper number of sig figs.

5. Express the sum of 20.6 mm, 49.5 cm and 5.03 m in meters

6. If 22.5 L of gasoline is drawn from a tank originally containing 65 L of gasoline, what volume of gasoline remains in the tank?

7. What is the area of the bottom of a tank 30.0 cm long and 15.0 cm wide?

8. If the tank in Problem 7 has a volume of  $2.25 \times 10^4 \text{ cm}^3$ , what is its height?

9. How many centimeters are there in 35.0 inches?

10. What is the distance, in kilometers, of a 2.5 mile cross-country course?

## Math Review

Fill in the following table for the following quantities and their symbols:

| Quantity  | Unit   | Symbol |
|-----------|--------|--------|
| length    | meters | m      |
| mass      |        |        |
| time      |        |        |
| force     |        |        |
| energy    |        |        |
| power     |        |        |
| speed     |        |        |
| frequency |        |        |

Complete the following conversions

1. 4 km = m
2. 54 mm = m
3. 0.394 Mg = g
4. 4000 ms = s
5. 4 dl = l
6. 70 dam (deka meters) = m
7. 4 Gg = cg
8. 9 000 000  $\mu\text{m}$  = km
9. 4000 s = h
10. 67 m<sup>2</sup> = cm<sup>2</sup>

**Example 1:**

$$3000 \text{ cm} = \text{ km}$$

$$3000 \text{ cm} \times \left( \frac{1 \text{ m}}{100 \text{ cm}} \right) \times \left( \frac{1 \text{ km}}{1000 \text{ m}} \right)$$

$$= 0.03 \text{ km} (100 \text{ cm}) (1000 \text{ m})$$

**Example 2:**

$$3 \text{ m}^3 = \text{ cm}^3$$

$$3 \text{ m}^3 \times (100 \text{ cm})^3 = 3 \text{ m}^3 \times (1\,000\,000 \text{ cm}^3) = 3\,000\,000 \text{ cm}^3$$

$$(1 \text{ m})^3 \quad (1 \text{ m}^3)$$

### Rounding:

5 and up  $\square$  round up                      4.55  $\square$  4.6  
 4 and down  $\square$  round down              4.54  $\square$  4.5

### Significant Figures:

All non-zero numbers count. Zeros to the left never count. Zeros in the middle always count.  
 Zeros to the right count only if there is a decimal in the number.

**Example:**        0.00050600        This number has 5 sig figs because the four zeros to the left of the 5 don't count. The 5 and 6 count. The 0 in the middle counts. The two zeros to the right of the 6 count because there is a decimal in the number.

**Example:**        567, 000        This number has 3 sig figs because the 5,6,and 7 count, but the zeros to the right do not count since there is no decimal in the number.

Round the following numbers to 2 sig figs:

- |                                             |                           |
|---------------------------------------------|---------------------------|
| 1. 35.67 $\square$ _____                    | 6. 0.0102 $\square$ _____ |
| 2. 0.0004567 $\square$ _____                | 7. 99536 $\square$ _____  |
| 3. 2.34 x 10 <sup>4</sup> $\square$ _____   | 8. 1.0326 $\square$ _____ |
| 4. 4.777 x 10 <sup>-6</sup> $\square$ _____ | 9. 156.21 $\square$ _____ |
| 5. 23.333 $\square$ _____                   | 10. 9.75 $\square$ _____  |

**Multiplication / Division:** This is the most common rule for sig figs we will be using. Use this for all multiplication or multifunction equations. Use the **lowest number of total sig figs** in your equation for your answer.

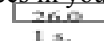
Example:  $6.5 \text{ m} \times 687.3 \text{ m} = 4467.645 \text{ m}$ , but because of sig figs, your answer will be



(2)      (4)      (7)      (2)

**Addition / Subtraction:** If you have a situation where you are only using addition and / or subtraction you should use this rule for sig figs. Look at the number of **decimal places** and use the smallest number of decimal places in your answer.

Example:  $3.456 \text{ s} + 22.55 \text{ s} = 26.006 \text{ s}$ , but because of sig figs, your answer will be



(3)      (2)      (3)      (2)

Solve the following equations and leave the answers with the correct number of sig figs:

1.  $23 + 4.8 =$  \_\_\_\_\_
2.  $234.67 \times 34 =$  \_\_\_\_\_
3.  $4567 / 2.45 =$  \_\_\_\_\_
4.  $2.56 + 0.89 =$  \_\_\_\_\_
5.  $2345.8 \times 23.2 =$  \_\_\_\_\_

### Percent Uncertainty:

If something is measured to be  $12.3 \text{ cm} \pm 0.5 \text{ cm}$ . What is its percent uncertainty?

$$\frac{0.5 \text{ cm}}{12.3 \text{ cm}} \times 100\% = 4\% \text{ uncertainty}$$

It is important to know how big the uncertainty is compared to the actual measurement.  $0.5 \text{ cm}$  error would be a lot if your measurement was only  $2.1 \text{ cm}$ ! That would amount to an error of  $24\%$  instead of only  $4\%$

$$(0.5 / 2.1) \times 100\% = 24\%$$

To emphasize this point, consider this;  $1 \text{ cm}$  error when you are measuring  $100\,000 \text{ cm}$  isn't much, therefore almost negligible. Your calculated % error would be low.  $1 \text{ cm}$  error when you are measuring only  $10 \text{ cm}$  is a concern. Your % error would be much higher.

### Entering very big and very small numbers into your calculator.

Say this... “...times ten to the...”.

Pressing on your calculator is the equivalent of saying “times ten to the”.

So, how do you enter  $4 \times 10^5$  into your calculator.

You would say this in the following way “4 times ten to the 5”.

You would enter into your calculator the following....



Enter these problems into your calculator...

$$(3.9 \times 10^7) \times (2 \times 10^2)$$



Your answer should be....?

$$(3.9 \times 10^{-7}) \times (2 \times 10^2)$$

|   |   |   |     |    |   |   |   |   |     |    |   |       |
|---|---|---|-----|----|---|---|---|---|-----|----|---|-------|
| 3 | . | 9 | 2nd | EE | ( | 7 | x | 2 | 2nd | EE | 2 | enter |
|---|---|---|-----|----|---|---|---|---|-----|----|---|-------|

Your answer should be....?

$$(-3.9 \times 10^{-7}) \times (2 \times 10^2)$$

|   |   |   |   |     |    |   |   |   |   |     |    |   |       |
|---|---|---|---|-----|----|---|---|---|---|-----|----|---|-------|
| ( | 3 | . | 9 | 2nd | EE | ( | 7 | x | 2 | 2nd | EE | 2 | enter |
|---|---|---|---|-----|----|---|---|---|---|-----|----|---|-------|

Your answer should be....?

Use your calculator to answer the following....

$$(3 \times 10^3) \times (2 \times 10^2) =$$

$$(3 \times 10^3) + (2 \times 10^{-2}) =$$

$$(-3 \times 10^{-3}) / (2 \times 10^2) =$$

$$(3 \times 10^3) - (2 \times 10^2) =$$

$$(3 \times 10^3) \times (2 \times 10^{-2}) =$$

$$(-3 \times 10^{-3}) \times (2 \times 10^2) =$$

+

## 1. Conversion

Science uses the **KMS** system (**SI**: System Internationale). **KMS** stands for kilogram, meter, second. These are the units of choice of physics. The equations in physics depend on unit agreement. So you must convert to **KMS** in most problems to arrive at the correct answer.

kilometers ( $km$ ) to meters ( $m$ ) and meters to kilometers  
centimeters ( $cm$ ) to meters ( $m$ ) and meters to centimeters  
millimeters ( $mm$ ) to meters ( $m$ ) and meters to millimeters  
nanometers ( $nm$ ) to meters ( $m$ ) and meters to nanometers  
micrometers ( $\mu m$ ) to meters ( $m$ )

gram ( $g$ ) to kilogram ( $kg$ )

Celsius ( $^{\circ}C$ ) to Kelvin ( $K$ )

atmospheres ( $atm$ ) to Pascals ( $Pa$ )

liters ( $L$ ) to cubic meters ( $m^3$ )

Other conversions will be taught as they become necessary.

What if you don't know the conversion factors? Colleges want students who can find their own information (so do employers). Hint: Try a good dictionary and look under "measure" or "measurement". Or the Internet? Enjoy.

a.  $4008\text{ g}$  = \_\_\_\_\_  $kg$

b.  $1.2\text{ km}$  = \_\_\_\_\_  $m$

c.  $823\text{ nm}$  = \_\_\_\_\_  $m$

d.  $298\text{ K}$  = \_\_\_\_\_  $^{\circ}C$

e.  $0.77\text{ m}$  = \_\_\_\_\_  $cm$

f.  $8.8 \times 10^{-8}\text{ m}$  = \_\_\_\_\_  $mm$

g.  $1.2\text{ atm}$  = \_\_\_\_\_  $Pa$

h.  $25.0\text{ }\mu m$  = \_\_\_\_\_  $m$

i.  $2.65\text{ mm}$  = \_\_\_\_\_  $m$

j.  $8.23\text{ m}$  = \_\_\_\_\_  $km$

k.  $40.0\text{ cm}$  = \_\_\_\_\_  $m$

l.  $6.23 \times 10^{-7}\text{ m}$  = \_\_\_\_\_  $nm$

m.  $1.5 \times 10^{11}\text{ m}$  = \_\_\_\_\_  $km$

## 2. Geometry

Solve the following geometric problems.

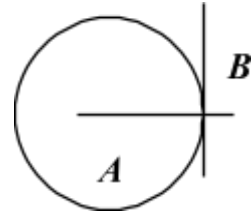
- a. Line **B** touches the circle at a single point. Line **A** extends through the center of the circle.

- i. What is line **B** in reference to the circle?

\_\_\_\_\_

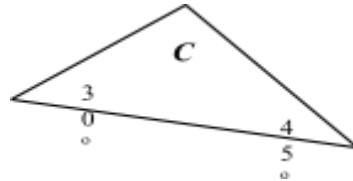
- ii. How large is the angle between lines **A** and **B**?

\_\_\_\_\_



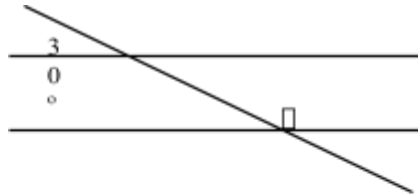
- b. What is angle **C**?

\_\_\_\_\_



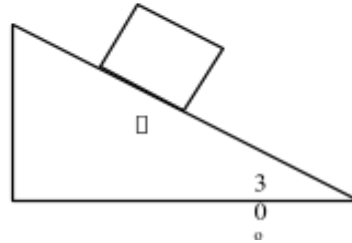
- c. What is angle  $\theta$ ?

\_\_\_\_\_



- d. How large is  $\theta$ ?

\_\_\_\_\_



- e. The radius of a circle is 5.5 cm,

- i. What is the circumference in meters?

\_\_\_\_\_

- ii. What is its area in square meters?

\_\_\_\_\_

- f. What is the area under the curve at the right?

\_\_\_\_\_

