

1.

|  |  |                      |   |  |
|--|--|----------------------|---|--|
|  | $3x^2$ or $-40$  |                      | 5 | M1 for differentiating one of the first two terms correctly  |
|  | $3x^2 - 40$  |                      |   | A1 for both terms correct and no additions   |
|  | $"3x^2 - 40" = 8$  |                      |   | M1ft dep on M1 for equating their quadratic derivative with 8<br><br>(Derivative must be in the form $ax^2 - 40$ or $3x^2 - b$ where $a \neq 0$ and $b \neq 0$ )               |
|  | $(y = )x^4 - 40x^3 + 1 (= -95)$ or<br>$y = (x - 4)^3 - 40x^3 - 4x + 1 (= 97)$                            |                      |   | M1ft dep on previous M1 for substituting at least one $x$ value into $y$<br><br>NB Following through from $ax^2 - 40 = 8$ or $3x^2 - b = 8$ , their $x$ values must be correct |
|  | <i>Working not required, so correct answer scores full marks (unless from obvious incorrect working)</i> | $(4, -95), (-4, 97)$ |   | A1 both coordinates must be paired correctly   |
|  |  |                      |   | <b>Total 5 marks</b>   |

2.

|      |  |            |   |                      |
|------|--|------------|---|----------------------|
| (i)  |  | $(-2, -4)$ | 1 | B1                   |
| (ii) |  | $(5, -10)$ | 1 | B1                   |
|      |  |            |   | <b>Total 2 marks</b> |

3. ,

|  |  |                   |   |  |
|--|--|-------------------|---|--|
|  | $\pm 3(x^2 \pm 4x) \dots \dots$ or $\pm 3(x^2 \pm 4x \dots \dots)$<br>or<br>$b = 3$                                      |                   | 4 | M1 for factorising $-3x^2 + 12x$<br>or<br>stating the correct value of $b$ or $b = 3$ embedded in an incorrect final answer in the form $a - 3(x - c)^2$ |
|  | $-3[(x - 2)^2 \dots \dots]$ or $-3(x - 2)^2 \dots \dots$   |                   |   | M1 for a <b>correct</b> first step to complete the square  |
|  | $-3[(x - 2)^2 - (2)^2] \dots \dots$ oe or<br>$-3(x - 2)^2 + 12 \dots \dots$ or<br>$-3[(x - 2)^2 - (2)^2 \dots \dots]$ oe |                   |   | M1 for a <b>correct</b> second step to complete the square   |
|  | <i>Working not required, so correct answer scores full marks (unless from obvious incorrect working)</i>                 | $29 - 3(x - 2)^2$ |   | A1 oe eg $-3(x - 2)^2 + 29$  |
|  |  |                   |   | <b>Total 4 marks</b>   |

4.

|                      |   |           |   |      |   |
|----------------------|---|-----------|---|------|---|
|                      | $\left(\frac{dy}{dx}\right) = 3x^2 - 16x - 12$  |           | 5 | M1   | for differentiation with at least 2 terms correct   |
|                      | $"3x^2 - 16x - 12" = 0$   |           |   | M1ft | (dep on previous M1) for their $\frac{dy}{dx} = 0$  |
|                      | eg $(3x+2)(x-6) (= 0)$<br>or $(x =) \frac{-(-16) \pm \sqrt{(-16)^2 - 4 \times 3 \times (-12)}}{2 \times 3}$<br>or $3 \left[ \left(x - \frac{8}{3}\right)^2 - \frac{64}{9} \right] - 12 (= 0)$ |           |   | M1ft | (dep on 1 <sup>st</sup> M1)<br><br>for the correct x value (of 6) – ignore other x value<br><b>OR</b><br>for solving <b>their</b> 3 term quadratic equation using any correct method<br>(if factorising, allow brackets which expanded give 2 out of 3 terms correct)<br>(if using formula allow one sign error and some simplification – allow as far as $\frac{16 \pm \sqrt{256 + 144}}{6}$ )<br>(if completing the square then as far as shown on LHS)<br><br>The award of this mark implies the previous M mark |
|                      | eg $6^3 - 8 \times 6^2 - 12 \times 6 + 5 (= -139)$  |           |   | M1ft | (dep on 1 <sup>st</sup> M1) for $x = 6$ substituted into correct equation for curve C<br><b>OR</b><br>(dep on 1 <sup>st</sup> M1 and 2 values for x) for <b>their</b> greatest x value substituted into correct equation for curve C (ignore any attempt to substitute their least x value)   |
|                      | <i>Working required</i>   | (6, -139) |   | A1   | (dep on M2) cao   |
| <b>Total 5 marks</b> |   |           |   |      |   |

5.

|                      |   |   |   |       |   |
|----------------------|---|---|---|-------|---|
| (a)                  | $2\left(x^2 - \frac{11}{2}x\right) + \dots$ or $2\left(x^2 - \frac{11}{2}x + \dots\right)$ oe   |   | 3 | M1    | for taking out a factor of 2  |
|                      | $2\left[\left(x - \frac{11}{4}\right)^2 - \frac{11^2}{4^2}\right] + \dots$ or $2\left[\left(x - \frac{11}{4}\right)^2 - \frac{11^2}{4^2} + \dots\right]$ oe |   |   | M1    | for correctly completing square   |
|                      | <i>Correct answer scores full marks (unless from obvious incorrect working)</i>   | $2\left(x - \frac{11}{4}\right)^2 - \frac{49}{8}$ |   | A1    | oe, eg $2(x - 2.75)^2 - 6.125$<br>allow $a = 2$ , $b = \frac{11}{4}$ oe, $c = \frac{49}{8}$ oe<br>if no other marks awarded,<br>award SCB1 for $2\left(x - \frac{11}{4}\right)^2 + \dots$ |
| <b>ALTERNATIVE</b>   |   |   |   |       |   |
| Γ (a)                | $ax^2 - 2bax + b^2a - c$  |   | 3 | M1    | for correctly expanding $a(x - b)^2 - c$ to give $ax^2 - 2bax + b^2a - c$   |
|                      | $-2ba = -11$ or $2ba = 11$ and $b^2a - c = 9$   |   |   | M1    | for setting up 2 equations using the coefficient of x and the numerical term  |
|                      | <i>Correct answer scores full marks (unless from obvious incorrect working)</i>   | $2\left(x - \frac{11}{4}\right)^2 - \frac{49}{8}$ |   | A1    | oe, eg $2(x - 2.75)^2 - 6.125$<br>allow $a = 2$ , $b = \frac{11}{4}$ oe, $c = \frac{49}{8}$ oe<br>if no other marks awarded,<br>award SCB1 for $2\left(x - \frac{11}{4}\right)^2 + \dots$ |
| (b)                  |   | $\left(\frac{23}{4}, -\frac{49}{8}\right)$        | 2 | B2ft  | oe, eg (5.75, -6.125)   |
|                      |   |   |   | (B1ft | for one correct coordinate)   |
| <b>Total 5 marks</b> |   |   |   |       |   |

6.

|  |   |                    |   |  |
|--|---|--------------------|---|--|
| eg $2(5-y)^2 + 3y^2 = 210$<br>$\sqrt{\frac{210-3y^2}{2}} = 5-y$ oe   | Eg $2x^2 + 3(5-x)^2 = 210$<br>$\sqrt{\frac{210-2x^2}{3}} = 5-x$ oe  |                    | 5 | M1 substitution of $x = \pm 5 \pm y$ or $y = \pm 5 \pm x$ into $2x^2 + 3y^2 = 210$ or a correct equation formed by using $x = \pm 5 \pm y$ or $y = \pm 5 \pm x$ to obtain an equation in $x$ only or $y$ only  |
| eg $5y^2 - 20y - 160 (= 0)$<br>or<br>$y^2 - 4y - 32 (= 0)$   | eg $5x^2 - 30x - 135 (= 0)$<br>or<br>$x^2 - 6x - 27 (= 0)$  |                    |   | M1 dep on previous M1 for multiplying out and collecting terms, forming a three term quadratic in any form of $ax^2 + bx + c (= 0)$ where <b>at least 2</b> coefficients ( $a$ or $b$ or $c$ ) are correct   |
| eg $(y-8)(y+4) (= 0)$<br>$y = \frac{-4 \pm \sqrt{(-4)^2 - 4 \times 1 \times -32}}{2 \times 1}$<br><br>eg<br>$(y-2)^2 - 2^2 = -32$<br>(allow incorrect labels for $x/y$ ) | eg $(x-9)(x+3) (= 0)$<br>$x = \frac{-6 \pm \sqrt{(-6)^2 - 4 \times 1 \times -27}}{2 \times 1}$<br><br>eg<br>$(x-3)^2 - 3^2 - 27 = 0$<br>(allow incorrect labels for $x/y$ ) |                    |   | M1 (dep on first M1) for a complete method to solve their 3-term quadratic equation ( $ax^2 + bx + c = 0$ ); correct factorisation or substitution into formula (allow one sign error and some simplification – allow as far as $\frac{4 \pm \sqrt{16+128}}{2}$ or $\frac{6 \pm \sqrt{36+108}}{2}$ ) or completing the square or for seeing $x = 9, x = -3$ or $y = 8, y = -4$ |
| eg $x + 8 = 5$ and $x + -4 = 5$<br>(correct labels for $x/y$ )   | eg $y = 5 - 9$ and $y = 5 - -3$<br>(correct labels for $x/y$ )  |                    |   | M1ft dep on previous M1 for substituting <b>their</b> 2 found values of $x$ or $y$ in a suitable equation (allow use of quadratic equation) or fully correct values for the other variable must see substitution for incorrect $x/y$ values  |
| working required   |   | (9, -4)<br>(-3, 8) |   | A1 (dep on M2)   |
|  |   |                    |   | <b>Total 5 marks</b>   |

7.

|      |  |          |   |                      |     |
|------|--|----------|---|----------------------|-----|
| (i)  |  | (30, 2)  | 1 | B1                   | cao |
| (ii) |  | (300, 0) | 1 | B1                   | cao |
|      |  |          |   | <b>Total 2 marks</b> |     |

8.

|  |   |               |   |  |
|--|---|---------------|---|--|
|  | $(fg(k)) = \frac{3k+1}{2(3k+1)-4}$ oe or $\frac{3k+1}{2(3k+1)-4} = 2$ oe or<br>$(fg(k)) = \frac{3k+1}{6k-2}$ oe or $\frac{3k+1}{6k-2} = 2$ oe or<br>$x = 2(2x-4)$ or $x = 4x-8$ or $x = \frac{8}{3}$ oe |               | 3 | M1 for a correct expression for $fg(k)$ or $fg(x)$ or for $f(x) = 2$<br><br>Allow $x$ instead of $k$ for all marks   |
|  | $3k+1 = 2(6k-2)$ oe or<br>$3k+1 = 2(2(3k+1)-4)$ oe or<br>$3k+1 = 12k-4$ oe or<br>$3k+1 = \frac{8}{3}$ oe  |               |   | M1 dep on M1 for <b>correctly</b> removing the denominator to form a correct equation or<br>for $g(k) = \frac{8}{3}$ |
|  | Working not required, so correct answer scores full marks (unless from obvious incorrect working)   | $\frac{5}{9}$ |   | A1 oe eg 0.55(555...) rounded or truncated or 0.5 (must show recurring)  |
|  |   |               |   | <b>Total 3 marks</b>   |

9.

|               |  |         |   |    |
|---------------|--|---------|---|----|
| (i)           |  | (6, 7)  | 1 | B1 |
| (ii)          |  | (2, -3) | 1 | B1 |
| Total 2 marks |  |         |   |    |

10.

|               |  |                   |   |  |
|---------------|--|-------------------|---|--|
|               | $\left(\frac{dy}{dx} = \right) 3 \times 4x^2 - 8 (= 12x^2 - 8)$  |                   | 4 | B2 for $3 \times 4x^2 - 8$ or $12x^2 - 8$ (with no other terms)<br><br>(B1 for one term, ie $3 \times 4x^2$ or $12x^2$ or $-8$ ) |
|               | $"12x^2 - 8" = \frac{1}{3}$  |                   |   | M1 for equating their initial derivative with the given gradient.<br>Derivative must be a <b>quadratic</b> (dep on B1)           |
|               | <i>Working not required, so correct answer scores full marks (unless from obvious incorrect working)</i> | $\pm \frac{5}{6}$ |   | A1oe Ignore y values<br>Allow $\pm 0.83(333\dots)$ or $\pm \sqrt{\frac{25}{36}}$ oe  |
| Total 4 marks |  |                   |   |  |

11.

|               |  |                         |   |                                       |
|---------------|--|-------------------------|---|---------------------------------------|
| (a)           |  | $(a =) -4$<br>$(b =) 6$ | 2 | B1 for $(a =) -4$<br>B1 for $(b =) 6$ |
| (b)           |  | $(p =) 3$<br>$(q =) 45$ | 2 | B1 for $(p =) 3$<br>B1 for $(q =) 45$ |
| Total 4 marks |  |                         |   |                                       |

12.

|               |  |      |   |                                    |
|---------------|--|------|---|------------------------------------|
| i             | $\left(\frac{ds}{dt} = \right) 6t^2 - 10t + 6$   |      | 4 | M1 at least 2 terms correct        |
|               | $\left(\frac{dv}{dt} = \right) 12t - 10$   |      |   | M1ft ft from a 3 term quadratic    |
|               | $"12t - 10" = 5$   |      |   | M1ft ft dep on previous M1 awarded |
|               | <i>Working not required, so correct answer scores full marks (unless from obvious incorrect working)</i> | 1.25 |   | A1oe                               |
| Total 4 marks |  |      |   |                                    |

13.

|   |  |                              |   |  |
|---|--|------------------------------|---|--|
| (a)   |  | 4.5                          | 1 | B1oe 4.5, $x = 4.5$ , $x \neq 4.5$<br>Allow anything with 4.5, $\frac{9}{2}$ or $4\frac{1}{2}$ apart<br>from $x < 4.5$ , $x > 4.5$ , $x \leq 4.5$ , $x \geq 4.5$ |
| (b)   | $(g(4)) = \frac{5}{2 \times 4 - 9} (= -5)$ or $5\left(\frac{5}{2 \times 4 - 9}\right) + 7$ oe            |                              | 2 | M1   |
|   | <i>Working not required, so correct answer scores full marks (unless from obvious incorrect working)</i> | -18                          |   | A1   |
| (c)   | $(y =) 3(x^2 - 4x) + \dots$ or $y = 3(x^2 - 4x + \dots)$<br>where $\dots$ can be number(s) or nothing    |                              | 4 | M1 or $3x^2 - 12x + (8 - y) = 0$ oe  |
|   | $(y =) 3(x - 2)^2 \dots$ or $y = 3[(x - 2)^2 \dots]$<br>could have: $y - 8 = 3[(x - 2)^2 \dots]$ oe      |                              |   | M1<br>or $(x =) \frac{12 \pm \sqrt{144 - 12(8 - y)}}{6}$ may have +<br>rather than $\pm$   |
|   | $(x - 2)^2 = \frac{y + 4}{3}$ oe or an answer of $2 \pm \sqrt{\frac{4 + y}{3}}$                          |                              |   | M1<br>or $(x =) 2 \pm \sqrt{\frac{4 + y}{3}}$ may have + rather than<br>$\pm$  |
|   | <i>Working not required, so correct answer scores full marks (unless from obvious incorrect working)</i> | $2 + \sqrt{\frac{x + 4}{3}}$ |   | A1<br>oe eg $2 + \frac{\sqrt{12 + 3x}}{3}$   |
| : Allow candidates to swap x and y (or other letter) at any stage when finding the inverse – but the answer must be in terms of x |  |                              |   |  |
|   |  |                              |   | <b>Total 7 marks</b>   |

14.

|     |  |                             |   |  |
|-----|--|-----------------------------|---|--|
| (a) |  | $12x^2 + 2x - 20$           | 2 | M1 for at least 2 of $12x^2$ , $2x$ , $-20$<br>A1  |
| (b) | $12x^2 + 2x - 20 = 4$ oe   |                             | 4 | M1 ft, for equating their dy/dx to 4   |
|     | $12x^2 + 2x - 24 (= 0)$ or $6x^2 + x - 12 (= 0)$   |                             |   | M1 (dep on M1) ft their dy/dx in the<br>form $ax^2 + bx (+ c)$   |
|     | eg $(6x - 8)(2x + 3) (= 0)$<br>or $(3x - 4)(2x + 3) (= 0)$<br>or<br>$x = \frac{-2 \pm \sqrt{(2)^2 - (4 \times 12 \times -24)}}{2 \times 12}$ |                             |   | M1 for solving their three-term quadratic<br>equation using any correct method - if<br>factorising, allow brackets which expanded<br>give 2 out of 3 terms correct (if using<br>formula or completing the square allow one<br>sign error and some simplification – allow<br>as far as eg $\frac{-2 \pm \sqrt{4 + 1152}}{24}$ oe) |
|     | <i>Working required</i>  | $\frac{4}{3}, -\frac{3}{2}$ |   | A1<br>(dep on M2) oe, allow 1.33(3...) for $\frac{4}{3}$ ,<br>both values – isw any attempt to find y<br>coordinates   |
|     |  |                             |   | <b>Total 6 marks</b>   |

15.

|                      |   |     |   |  |
|----------------------|---|-----|---|--|
| (a)                  |   | 2.5 | 1 | B1 oe  |
| (b)                  | $(gh(x)) = \frac{11}{2(x^2+4)-5} (=1)$  |     | 3 | M1   |
|                      | $11 - 3 = 2x^2$ oe eg $x^2 = 4$<br>or $2x^2 - 8 = 0$ or $x^2 - 4 = 0$           |     |   | M1 correct expansion and rearrangement with $x$ term on one side and number terms the other side or all terms on one side in an equation |
|                      | <i>Correct answer scores full marks (unless from obvious incorrect working)</i> | 2   |   | A1<br>cao, an answer of $\pm 2$ gains M2 only<br><br>If no other marks awarded,<br>award SCB1 for answer of 2.2 oe                       |
| <b>Total 4 marks</b> |   |     |   |  |

16.

|                      |  |         |   |        |
|----------------------|--|---------|---|--------|
| (a)                  |  | (10, 5) | 1 | B1 cao |
| (b)                  |  | (2, 5)  | 1 | B1 cao |
| <b>Total 2 marks</b> |  |         |   |        |

17.

|                      |   |  |   |  |
|----------------------|---|--|---|--|
| (a)(i)               |   | (3, 10)  | 1 | B1   |
| (ii)                 |   | (3, -2)  | 1 | B1   |
| (iii)                |   | (-3, 5)  | 1 | B1   |
| (b)                  | $(x \pm 2)$   | $(x + 3.5 \pm 2)$ ..... or<br>$\left(x + \frac{7}{2} \pm 2\right)$ ... | 4 | M1 for sight or use of $(x \pm 2)$ or $(x + 1.5)$ or $(x + 5.5)$       |
|                      | $(x - 2)^2 + 7(x - 2) + 20$   | $(x + 3.5 - 2)^2 - 3.5^2 + 20$ or<br>$(x + 1.5)^2 + 7.75$              |   | M1 for correct substitution or correct use of $(x - 2)$ for $x$ into L |
|                      | $x^2 - 4x + 4 + 7x - 14 + 20$   | $x^2 + 3x + 2.25 - 12.25 + 20$ or<br>$x^2 + 3x + 2.25 + 7.75$          |   | M1 dep on M2<br>for expanding brackets <b>correctly</b>                |
|                      | <i>Correct answer scores full marks (unless from obvious incorrect working)</i> | $x^2 + 3x + 10$  |   | A1   |
| <b>Total 7 marks</b> |   |  |   |  |

18.

|               |   |                 |   |  |
|---------------|---|-----------------|---|--|
| (a)           | $3x^2$ or $-2 \times 2x$ or $-4x$ or $-9$ oe  |                 | 2 | M1 for differentiating one term correctly  |
|               |   | $3x^2 - 4x - 9$ |   | A1 for a correct expression<br>Allow $3x^2 - 2 \times 2x - 9$  |
| (b)           | $(x =) \frac{4 \pm \sqrt{(-4)^2 - (4 \times 3 \times -9)}}{2 \times 3}$ or $3 \left[ \left( x - \frac{2}{3} \right)^2 - \left( \frac{2}{3} \right)^2 \right] - 9 (= 0)$ |                 | 4 | M1 for finding the critical values for a 3-term quadratic using any correct method - if using formula or completing the square allow one sign error and some simplification<br>- allow as far as eg $\frac{4 \pm \sqrt{16 + 108}}{6}$<br>oe<br>or eg $3 \left( x - \frac{2}{3} \right)^2 - 10 \frac{1}{3}$ oe) |
|               |   | -1.19 and 2.52  |   | A1 for critical values of -1.19 and 2.52 or better (for this A1 mark allow -1.2 or -1.18 and 2.5<br>or $\frac{2 \pm \sqrt{31}}{3}$ oe)   |
|               |   | $x < -1.19$     |   | A1 awrt -1.19  |
|               |   | $x > 2.52$      |   | A1 awrt 2.52   |
| Total 6 marks |   |                 |   |  |

19.

|  |   |  |   |  |
|--|---|--|---|--|
| Eg<br>$(2x+1)^2 + x(2x+1) = 7$   | eg<br>$y^2 + \left( \frac{y-1}{2} \right) y = 7$  |  | 5 | M1 for substitution of $y = \pm 2x \pm 1$ (or $x = \frac{\pm y \pm 1}{2}$ ) into $y^2 + xy = 7$ to obtain an equation in $x$ only (or $y$ only)  |
| E.g.<br>$6x^2 + 5x - 6 (= 0)$<br>$6x^2 + 5x = 6$   | E.g.<br>$3y^2 - y - 14 (= 0)$<br>$3y^2 - y = 14$  |  |   | M1ft dep on previous M1 for multiplying out and collecting terms, forming a three term quadratic in any form of $ax^2 + bx + c (= 0)$ where at least 2 coefficients ( $a$ or $b$ or $c$ ) are correct  |
| E.g.<br>$(2x+3)(3x-2) (= 0)$<br>or<br>$x = \frac{-5 \pm \sqrt{5^2 - 4 \times 6 \times -6}}{2 \times 6}$<br>or<br>$\left( x + \frac{5}{12} \right)^2 - \left( \frac{5}{12} \right)^2 = 1$<br>$\left( x = -\frac{3}{2} \text{ and } x = \frac{2}{3} \right)$ | E.g.<br>$(y+2)(3y-7) (= 0)$<br>or<br>$y = \frac{-(-1) \pm \sqrt{(-1)^2 - 4 \times 3 \times -14}}{2 \times 3}$<br>or<br>$\left( y - \frac{1}{6} \right)^2 - \left( \frac{1}{6} \right)^2 = \frac{14}{3}$<br>$\left( y = -2 \text{ and } y = \frac{7}{3} \right)$ |  |   | M1ft dep on first M1 method to solve <b>their</b> 3 term quadratic using any correct method (allow one sign error and some simplification - allow as far as eg $\frac{-5 \pm \sqrt{25 + 144}}{12}$ or $\frac{1 \pm \sqrt{1 + 168}}{6}$ or if factorising allow brackets which expanded give 2 out of 3 terms correct)<br>or correct values for $x$ or correct values for $y$<br>Accept $(x =) 0.6(66...)$ rounded or truncated or $(y =) 2.3(33...)$ |
| $y = 2 \left( -\frac{3}{2} \right) + 1 (= -2)$<br>and<br>$y = 2 \left( \frac{2}{3} \right) + 1 \left( = \frac{7}{3} \right)$   | $-2 = 2x + 1$ or $x = -\frac{3}{2}$<br>and<br>$\frac{7}{3} = 2x + 1$ or $x = \frac{2}{3}$   |  |   | M1ft dep on previous M1 for substituting <b>their</b> 2 found values of $x$ or $y$ into one of the two given equations<br>or fully correct values for the other variable (correct labels for $x / y$ )   |

20.

|                      |  |                      |   |                                 |
|----------------------|--|----------------------|---|---------------------------------|
| (a)                  |  | $\frac{k}{x}$        | 1 | B1 allow $kx^{-1}$              |
| (b)(i)               |  | -46                  | 1 | B1 cao                          |
| (ii)                 | $\frac{3(2-3x^4)}{2-(2-3x^4)}$ or $\frac{6-9x^4}{2-2+3x^4}$ oe or $\frac{6-9x^4}{3x^4}$ oe |                      | 2 | M1                              |
|                      | <i>Correct answer scores full marks (unless from obvious incorrect working)</i>            | $\frac{2-3x^4}{x^4}$ |   | A1 allow $\frac{2}{x^4} - 3$ oe |
| <b>Total 4 marks</b> |  |                      |   |                                 |

21.

|                      |   |                   |   |  |
|----------------------|---|-------------------|---|--|
| (a)                  |   | -0.5              | 1 | B1<br>oe eg $-\frac{1}{2}, \frac{-1}{2}, \frac{1}{-2}, -1/2$                                       |
| (b)                  | $(3x-5)y=2$ or $(3y-5)x=2$ or<br>$3xy-5y=2$ or $3xy-5x=2$ oe or<br>$3y-5=\frac{2}{x}$ or $3x-5=\frac{2}{y}$ oe      |                   | 2 | M1<br>remove denominator or get to the stage<br>$3y-5=\frac{2}{x}$ or $3x-5=\frac{2}{y}$           |
|                      | <i>Correct answer scores full marks (unless from obvious incorrect working)</i>                                     | $\frac{2+5x}{3x}$ |   | A1 oe<br>eg $\frac{2}{3x} + \frac{5}{3}$ or $\frac{\frac{2}{x}+5}{3}$ <b>must be in terms of x</b> |
| (c)                  | $5(x^2-4x)$ .....or $5(x^2-4x)$ .....) or $5(x-2)^2 \dots$  |                   | 3 | M1   |
|                      | $5[(x-2)^2 - (-2)^2]$ .....or $5[(x-2)^2 - (-2)^2]$ .....<br>or $5(x-2)^2 - 20$ ..... or $5[(x-2)^2 + \frac{3}{5}]$ |                   |   | M1<br>$(-2)^2$ can be $2^2$ or $4$ or $(\pm \frac{4}{2})^2$  |
|                      | <i>Correct answer scores full marks (unless from obvious incorrect working)</i>                                     | $5(x-2)^2 + 3$    |   | A1   |
| <b>Total 6 marks</b> |   |                   |   |  |

22.

|          |  |                            |          |  |
|----------|--|----------------------------|----------|--|
|          | $y = 3(x^2 - 4x) + 7$ or $y = 3\left(x^2 - 4x + \frac{7}{3}\right)$ or $\frac{y-7}{3} = x^2 - 4x$<br>or $y = 3(x-2)^2 \dots$ | 4                          | M1       | for a correct equation for a first step to complete the square                             |
|          | eg $y = 3((x-2)^2 - 2^2) + 7$ or $y = 3((x-2)^2 - 2^2 + \frac{7}{3})$ or<br>$y = 3(x-2)^2 - 5$ oe or                         |                            | M1       |  |
|          | $(x-2)^2 = \frac{y+5}{3}$ oe eg $(x-2)^2 = \frac{y-7}{3} + 4$ or<br>$x-2 = (\pm)\sqrt{\frac{y+5}{3}}$ oe                     |                            | M1       |  |
|          | <i>Correct answer scores full marks (unless from obvious incorrect working)</i>  | $2 - \sqrt{\frac{x+5}{3}}$ | A1<br>oe | NB: note only negative square root.<br>Must be in terms of x<br><b>any equivalent form</b> |
|          | <b>Note: Allow candidates to swap x and y when finding the inverse</b>   |                            |          | <b>Total 4 marks</b>   |
| <b>f</b> | $3x^2 - 12x + (7 - y) = 0$   | 4                          | M1       | for a correct first step   |
|          | $(x =) \frac{12 \pm \sqrt{144 - 12(7 - y)}}{6}$  |                            | M1       |  |
|          | $(x =) 2 \pm \sqrt{\frac{60 + 12y}{36}}$ oe  |                            | M1       |  |
|          | <i>Correct answer scores full marks (unless from obvious incorrect working)</i>  | $2 - \sqrt{\frac{x+5}{3}}$ | A1<br>oe | NB: note only negative square root.<br>Must be in terms of x<br><b>any equivalent form</b> |
|          |  |                            |          | <b>Total 4 marks</b>   |

23.

|      |  |         |   |                      |
|------|--|---------|---|----------------------|
| (i)  |  | (-4, 7) | 1 | B1                   |
| (ii) |  | (5, 10) | 1 | B1                   |
|      |  |         |   | <b>Total 2 marks</b> |

24.

|        |                          |                     |   |  |
|--------|--------------------------|---------------------|---|--|
| (a)(i) |                          | (-6, 1)             | 2 | B1   |
| (ii)   |                          | (-2, -4)            |   | B1   |
| (b)    | (-1, 6), (3, -2), (7, 6) | Fully correct graph | 2 | B2 for a fully correct graph<br>(B1 for a V shape with least value at (3, -2)) |
| (c)    |                          | -3, 4               | 2 | B2 for 2 correct values in any order<br>(B1 for 1 correct value)               |
|        |                          |                     |   | <b>Total 6 marks</b>   |

25.

|               |  |                   |   |  |
|---------------|--|-------------------|---|--|
| (a)           | $(x-3)^2$ or $(3-x)^2$ or $(y-3)^2$ or $(3-y)^2$                                 |                   | 4 | M1   |
|               | 14 or -14  |                   |   | M1 As part of an expression in $x$ or $y$ or an equation in $x$ and $y$  |
|               | $3 \pm \sqrt{14-x}$ or $3 \pm \sqrt{4-y}$  |                   |   | M1 Can be $\pm$ or $-$ or $+$  |
|               |  | $3 + \sqrt{14-x}$ |   | A1 oe must be in $x$   |
| alt (a)       | Alternative method:<br>$x^2 - 6x + (y-5) = 0$ oe or<br>$y^2 - 6y + (x-5) = 0$ oe |                   | 4 | M1 rearrange to form a quadratic in $x$ or $y$<br><br>terms can be in any order but must be in an equation equal to zero |
|               | $y = \frac{6 \pm \sqrt{36-4(x-5)}}{2}$ or $x = \frac{6 \pm \sqrt{36-4(y-5)}}{2}$ |                   |   | M1 correct substitution into quadratic formula   |
|               | $3 \pm \sqrt{14-x}$ or $3 \pm \sqrt{4-y}$  |                   |   | M1 Can be $\pm$ or $-$ or $+$  |
|               |  | $3 + \sqrt{14-x}$ |   | A1 oe must be in $x$   |
| (b)           |  | $x \leq 14$       | 1 | B1 oe <b>must</b> fit from part (a) dep on an answer in correct form   |
| Total 5 marks |  |                   |   |  |

26.

|               |   |          |   |  |
|---------------|---|----------|---|--|
|               | Line drawn at (2, 1) with a positive gradient that does not intersect the curve at any other point. |          | 3 | M1 for a tangent drawn at $x = 2$  |
|               |   |          |   | M1 (dep M1) for a correct method to work out the gradient of the tangent.                              |
|               |   | 1.5 to 3 |   | A1 for 1.5 to 3<br>accept answers in the range 1.5 – 3 so long as a tangent at $x = 2$ has been drawn. |
| Total 3 marks |   |          |   |  |

27.

|               |   |                  |   |  |
|---------------|---|------------------|---|--|
|               | $x^2 - 12x + 25$<br>$(x-6)^2 - 6^2 + 25$ or $(x-6)^2 - 11$<br><b>or</b><br>$x^2 - 12x + (25-y) = 0$ oe <b>or</b><br>$y^2 - 12y + (25-x) = 0$ oe |                  | 4 | M1 for substituting $g(x)$ into $f(x)$<br><br>M1 ft (dep on M1) for a correct first step in order to complete the square. Allow $y$ in place of $x$ .<br><br><b>or</b><br>Correctly setting up an equation = 0   |
|               | $(x-6)^2 = y + 11$ or $(y-6)^2 = x + 11$<br><b>or</b><br>$x = \frac{12 \pm \sqrt{44-4(25-y)}}{2}$ oe<br>or $x = 6 \pm \sqrt{1+y}$               |                  |   | M1 ft (dep on M2) for a correct rearrangement for their completed the square quadratic<br><br><b>or</b><br>correctly substituting into the quadratic formula (allow just $+$ or just $-$ instead of $\pm$ )<br><br>Allow same equations with $x$ and $y$ swapped |
|               |   | $6 - \sqrt{1+x}$ |   | A1 oe must be in terms of $x$ and have minus only before the square root.  |
| Total 4 marks |   |                  |   |  |

28.

|     |                                    |                                    |                  |   |  |
|-----|------------------------------------|------------------------------------|------------------|---|--|
| (a) |                                    |                                    | 5                | 1 | B1 cao   |
| (b) | $y(x-6) = 2x$ or<br>$yx - 6y = 2x$ | $x(y-6) = 2y$ or<br>$xy - 6x = 2y$ |                  | 3 | M1 for multiplying the denominator                           |
|     | $x(y-2) = 6y$                      | $y(x-2) = 6x$                      |                  |   | M1 for isolating the $x$ or $y$ terms <b>and</b> factorising |
|     |                                    |                                    | $\frac{6x}{x-2}$ |   | A1 accept $\frac{-6x}{2-x}$ (must be a function of $x$ )     |
|     |                                    |                                    |                  |   | <b>Total 4 marks</b>   |

29.

|      |  |            |   |  |
|------|--|------------|---|--|
| (i)  |  | $(s+2, t)$ | 1 | B1oe accept $(2+s, t)$                             |
| (ii) |  | $(s, 3t)$  | 1 | B1oe accept $(s, 3 \times t)$ or $(s, t \times 3)$ |
|      |  |            |   | <b>Total 2 marks</b>                               |