



# Indraprastha College for Women

## University of Delhi

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|--------------------|----------------------|
| Course Name:       | B.Sc.(H) Mathematics |
| Paper Title:       | Mathematical Finance |
| Unique Paper Code: | 32357614             |
| Semester:          | VI                   |
| Faculty(s):        | Ritika Gulati        |
| Year:              | 2024                 |

| Work Plan |                                                                   |             |                                                              |
|-----------|-------------------------------------------------------------------|-------------|--------------------------------------------------------------|
| Unit No.  | Learning Objective                                                | Lecture No. | Topics to be Covered                                         |
| 1         | Introduction to the application of mathematics in financial world | 1           | Interest rates, Types of rates, Measuring interest rates,    |
|           |                                                                   | 2           | Interest rates, Types of rates, Measuring interest rates,    |
|           |                                                                   | 3           | Interest rates, Types of rates, Measuring interest rates,    |
|           |                                                                   | 4           | Zero rates, Bond pricing, Forward rate, Duration, Convexity, |
|           |                                                                   | 5           | Zero rates, Bond pricing, Forward rate, Duration, Convexity, |
|           |                                                                   | 6           | Zero rates, Bond pricing, Forward rate, Duration, Convexity, |
|           |                                                                   | 7           | Exchange traded markets and OTC markets,                     |
|           |                                                                   | 8           | Exchange traded markets and OTC markets,                     |
|           |                                                                   | 9           | Exchange traded markets and OTC markets,                     |
|           |                                                                   | 10          | Derivatives--forward contracts, Futures contract,            |
|           |                                                                   | 11          | Derivatives--forward contracts, Futures contract,            |

|   |                                                                                                            |    |                                                                                  |
|---|------------------------------------------------------------------------------------------------------------|----|----------------------------------------------------------------------------------|
|   |                                                                                                            | 12 | Options, Types of traders, Hedging, Speculation, Arbitrage.                      |
|   |                                                                                                            | 13 | Options, Types of traders, Hedging, Speculation, Arbitrage.                      |
|   |                                                                                                            | 14 | Options, Types of traders, Hedging, Speculation, Arbitrage.                      |
|   |                                                                                                            | 15 | Options, Types of traders, Hedging, Speculation, Arbitrage.                      |
| 2 | To understand some computational and quantitative techniques required for working in the financial markets | 16 | No Arbitrage principle, Short selling, Forward price for an investment asset,    |
|   |                                                                                                            | 17 | No Arbitrage principle, Short selling, Forward price for an investment asset,    |
|   |                                                                                                            | 18 | No Arbitrage principle, Short selling, Forward price for an investment asset,    |
|   |                                                                                                            | 19 | Types of options, Option positions,                                              |
|   |                                                                                                            | 20 | Types of options, Option positions,                                              |
|   |                                                                                                            | 21 | Underlying assets, Factors affecting option prices,                              |
|   |                                                                                                            | 22 | Underlying assets, Factors affecting option prices,                              |
|   |                                                                                                            | 23 | Bounds on option prices, Put-call parity,                                        |
|   |                                                                                                            | 24 | Bounds on option prices, Put-call parity,                                        |
|   |                                                                                                            | 25 | Bounds on option prices, Put-call parity,                                        |
|   |                                                                                                            | 26 | Early exercise, Effect of dividends.                                             |
|   |                                                                                                            | 27 | Early exercise, Effect of dividends.                                             |
|   |                                                                                                            | 28 | Early exercise, Effect of dividends.                                             |
|   |                                                                                                            | 29 | Early exercise, Effect of dividends.                                             |
|   |                                                                                                            | 30 | Early exercise, Effect of dividends.                                             |
| 3 | To understand some computational and quantitative techniques required for working in actuarial mathematics | 31 | Binomial option pricing model, Risk neutral valuation (for European and American |

|   |                                                                                                            |    |                                                                                                                                    |
|---|------------------------------------------------------------------------------------------------------------|----|------------------------------------------------------------------------------------------------------------------------------------|
|   |                                                                                                            |    | options on assets following binomial tree model),                                                                                  |
|   |                                                                                                            | 32 | Binomial option pricing model, Risk neutral valuation (for European and American options on assets following binomial tree model), |
|   |                                                                                                            | 33 | Binomial option pricing model, Risk neutral valuation (for European and American options on assets following binomial tree model), |
|   |                                                                                                            | 34 | Binomial option pricing model, Risk neutral valuation (for European and American options on assets following binomial tree model), |
|   |                                                                                                            | 35 | Lognormal property of stock prices, Distribution of rate of return,                                                                |
|   |                                                                                                            | 36 | Lognormal property of stock prices, Distribution of rate of return,                                                                |
|   |                                                                                                            | 37 | Lognormal property of stock prices, Distribution of rate of return,                                                                |
|   |                                                                                                            | 38 | Lognormal property of stock prices, Distribution of rate of return,                                                                |
|   |                                                                                                            | 39 | expected return, Volatility,                                                                                                       |
|   |                                                                                                            | 40 | expected return, Volatility,                                                                                                       |
|   |                                                                                                            | 41 | expected return, Volatility,                                                                                                       |
|   |                                                                                                            | 42 | estimating volatility from historical data, Extension of risk neutral valuation to assets following GBM                            |
|   |                                                                                                            | 43 | estimating volatility from historical data, Extension of risk neutral valuation to assets following GBM                            |
|   |                                                                                                            | 44 | Black-Scholes formula for European options.                                                                                        |
|   |                                                                                                            | 45 | Black-Scholes formula for European options.                                                                                        |
| 4 | To understand some computational and quantitative techniques required for working in actuarial mathematics | 46 | Hedging parameters (the Greeks: Delta, Gamma, Theta, Rho and Vega),                                                                |

|  |  |    |                                                                     |
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|  |  | 47 | Hedging parameters (the Greeks: Delta, Gamma, Theta, Rho and Vega), |
|  |  | 48 | Hedging parameters (the Greeks: Delta, Gamma, Theta, Rho and Vega), |
|  |  | 49 | Trading strategies involving options,                               |
|  |  | 50 | Trading strategies involving options,                               |
|  |  | 51 | Swaps, Mechanics of interest rate swaps,                            |
|  |  | 52 | Swaps, Mechanics of interest rate swaps,                            |
|  |  | 53 | Comparative advantage argument,                                     |
|  |  | 54 | Comparative advantage argument,                                     |
|  |  | 55 | Valuation of interest rate swaps, Currency swaps,                   |
|  |  | 56 | Valuation of interest rate swaps, Currency swaps,                   |
|  |  | 57 | Valuation of currency swaps.                                        |
|  |  | 58 | Valuation of currency swaps.                                        |
|  |  | 59 | Valuation of currency swaps.                                        |
|  |  | 60 | Valuation of currency swaps.                                        |

| Syllabus |                                                                                                                                                                                                                                                                                                                                                                                          |               |
|----------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------|
| Unit     | Contents                                                                                                                                                                                                                                                                                                                                                                                 | Contact Hours |
| I        | Interest rates, Types of rates, Measuring interest rates, Zero rates, Bond pricing, Forward rate, Duration, Convexity, Exchange traded markets and OTC markets, Derivatives--forward contracts, Futures contract, Options, Types of traders, Hedging, Speculation, Arbitrage.                                                                                                            | 15            |
| II       | No Arbitrage principle, Short selling, Forward price for an investment asset, Types of options, Option positions, Underlying assets, Factors affecting option prices, Bounds on option prices, Put-call parity, Early exercise, Effect of dividends.                                                                                                                                     | 15            |
| III      | Binomial option pricing model, Risk neutral valuation (for European and American options on assets following binomial tree model), Lognormal property of stock prices, Distribution of rate of return, expected return, Volatility, estimating volatility from historical data, Extension of risk neutral valuation to assets following GBM, Black-Scholes formula for European options. | 15            |

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|---------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------|
| IV                                    | Hedging parameters (the Greeks: Delta, Gamma, Theta, Rho and Vega), Trading strategies involving options, Swaps, Mechanics of interest rate swaps, Comparative advantage argument, Valuation of interest rate swaps, Currency swaps, Valuation of currency swaps. | 15                                       |
|                                       | <b>Total</b>                                                                                                                                                                                                                                                      | <b>60</b>                                |
| <b>Text Books/Suggested Readings:</b> |                                                                                                                                                                                                                                                                   |                                          |
| <b>S. No.</b>                         | <b>Name of Authors/Books/Publishers</b>                                                                                                                                                                                                                           | <b>Year of Publication/<br/>Repr int</b> |
| 1.                                    | Hull, J. C., & Basu, S. (2010). Options, Futures and Other Derivatives (7th ed.). Pearson Education. New Delhi.                                                                                                                                                   | 2010                                     |
| 2.                                    |                                                                                                                                                                                                                                                                   |                                          |
| 3.                                    |                                                                                                                                                                                                                                                                   |                                          |
| 4.                                    |                                                                                                                                                                                                                                                                   |                                          |

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|--------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------|----------------------|
|                          | <b>Paper Components</b>                                                                                                                             |                       |                      |
| <b>Credits</b>           | <b>Lecture (L)</b>                                                                                                                                  | <b>Tutorial (T)</b>   | <b>Practical (P)</b> |
| <b>5+1</b>               | <b>5</b>                                                                                                                                            | <b>1</b>              | <b>0</b>             |
| <b>Assessment Scheme</b> |                                                                                                                                                     |                       |                      |
| <b>S.No.</b>             | <b>Component</b>                                                                                                                                    | <b>Marking Scheme</b> | <b>Total Marks</b>   |
| 1                        | Internal Assessment <ul style="list-style-type: none"> <li>Assignment/Quiz/Project/ Presentation</li> <li>Class Test</li> <li>Attendance</li> </ul> | <b>10</b>             | <b>25</b>            |
|                          |                                                                                                                                                     | 10                    |                      |
|                          |                                                                                                                                                     | 5                     |                      |
|                          |                                                                                                                                                     |                       |                      |
| 3.                       | Practical <ul style="list-style-type: none"> <li>Continuous Assessment</li> <li>End Term Written/Practical Exam</li> <li>Viva</li> </ul>            | <b>0</b>              | <b>0</b>             |
|                          |                                                                                                                                                     |                       |                      |
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| 4. | End Semester Examination | 75 | 75 |
|----|--------------------------|----|----|