

PDM: Chapter 3; Section 8: Graphs, Translations, and Solutions

Consider the following general equations:

$$y_1 = f(x)$$

$$y_2 = a \cdot f(bx - h) + k$$

y_2 is the image of y_1 after some combination of translations (slides/shifts) $T_{x,y}$ and scale changes (stretch/shrink) $S_{a,b}$.

Vertical Scale Change: a

Vertical Shift: k

Horizontal Scale Change: $\frac{1}{b}$

Horizontal Shift: Solve $bx - h = 0$ for x

Describe the transformation made to the function f in order to get the function g .

1. $f(x) = \sin(x)$

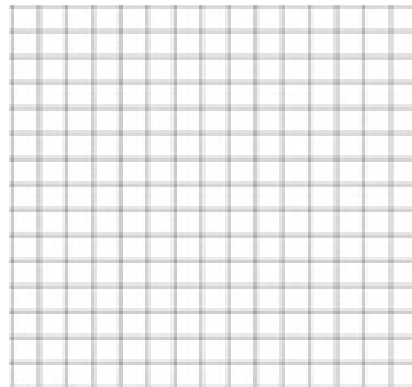
$$g(x) = \frac{3}{4} \sin\left(2x - \frac{\pi}{2}\right)$$

2. $f(x) = x^4$

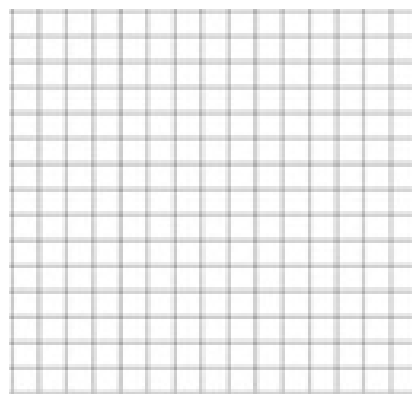
$$g(x) = 8(4x + 3)^4 - 3$$

Sketch the graphs of each of the following using known parent functions.

3. $f(x) = (x - 2)^2 - 6$

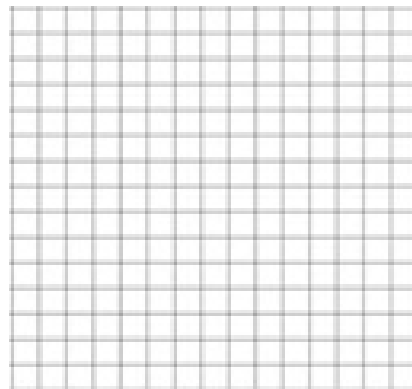


4. $f(x) = 2|x - 5| + 2$



5. Given that $x^2 + y^2 = r^2$ represents the graph of a circle centered at the origin with a radius of r , sketch the following graph.

$$\left(\frac{x-2}{4}\right)^2 + \left(\frac{y+6}{5}\right)^2 = 1$$

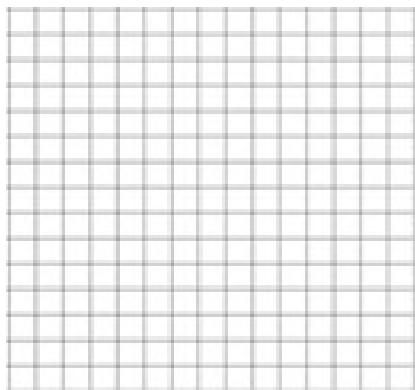


Homework

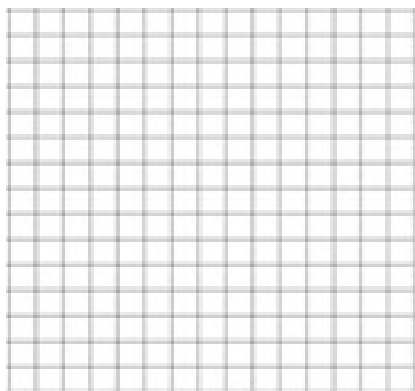
1. Describe the transformation made to the function
- f
- in order to get the function
- g
- .

a) $f(x) = x $ $g(x) = 2 x - 3 - 1$	b) $f(x) = x^3$ $g(x) = (3x + 6)^3 + 1$
c) $f(x) = \sin(x)$ $g(x) = \frac{1}{2}\sin(\pi x - \frac{\pi}{2})$	d) $f(x) = 2^x$ $g(x) = 5 + 3 \cdot 2^{2x+8}$

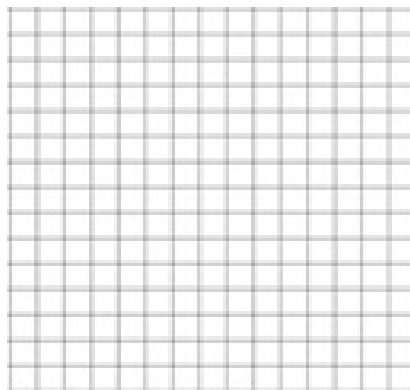
2. Sketch the graphs of each of the following, using known parent functions.



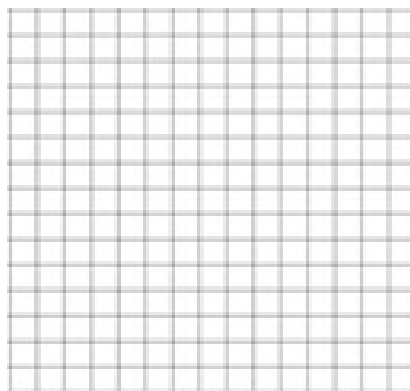
a) $y = (x - 2)^2 - 3$



c) $y = |2x + 6| - 1$



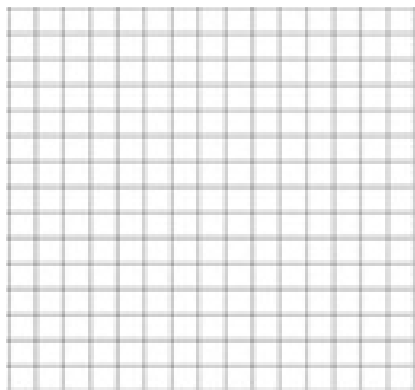
b) $y = \frac{1}{2}x^2 - 1$



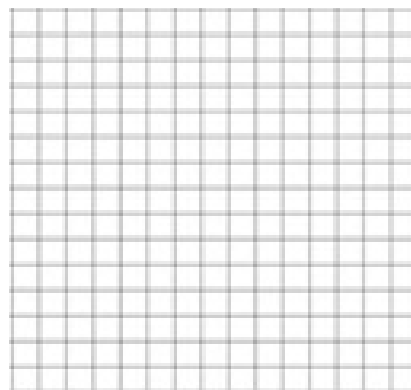
d) $y = -3 + 2\sqrt{x + 1}$

3. Given that $x^2 + y^2 = r^2$ represents the graph of a circle centered at the origin with a radius of r , sketch the following graphs

a) $\left(\frac{x-1}{2}\right)^2 + \left(\frac{y+2}{3}\right)^2 = 1$



b) $\left(\frac{x}{3}\right)^2 + (y - 4)^2 = 1$



4. Give an equation for the circle with center $(50, 30)$ and radius 25

5. Explain how the graph of the ellipse $\frac{x^2}{9} + \frac{y^2}{16} = 1$ is related to the graph of the unit circle

6. Give the equation of the function graphed using your knowledge of transformations of circles. Assume that the circle has a radius of 1.

