Systems of Linear Equations

Notes	Video Links & Practice Space
Welcome to your Toolbox	How to use the toolbox
Vocabulary	Vocabulary (0:56)
Linear Equation: a polynomial equation that contains a of 1, but no term of higher degree	
Parallel Lines: lines on the same coordinate plane that are at distance from each other and intersect	
Solution (of a system): a point or set of points that the equations of the system	
Determining the Solution Type of a Linear System	10 *
A linear system, as shown below, consists of two equations.	6-
y = x + 3	2
$y = -\frac{1}{3}x + 3$	10 -8 -6 -1 -2 2 4 6 8 10
Each equation will have an x-variable, a y-variable, and a constant (a number not attached to a variable). If there is no constant shown we can infer the constant is 0.	-2 + -4 + -6 +
The solution to a graphed system is the point (or points) where the lines intersect. A system can have one solution, infinite solutions, or no solutions.	-8 - -10 ¥

Types of Solutions One Solution (1:07) _____Solution _____ Slope _____ y-intercepts No Solution (1:23) y_____ Solution _____ Slope _____ y-intercepts **Infinite Solutions (1:22)** _____ Solutions _____ Slope _____ y-intercept

Verifying a Systems Solution Algebraically

If we graph the system below:

$$y = 2x + 4$$

$$y = -3x - 6$$

The point of intersection is (-2, 0)

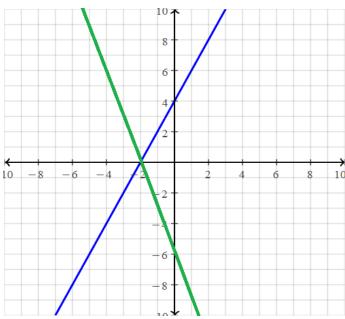
How can we verify algebraically that this solution is, in fact, correct?

We can _____ our solution into BOTH of the original equations.

If we obtain a _____ statement the solution is correct.

What is a true statement?

<u>Verifying Solutions</u> (3:16)



Solving Systems by Graphing

You've already learned how to graph linear equations in slope intercept form.

Graphing a linear system is no different except now we will be graphing two equations instead of one.

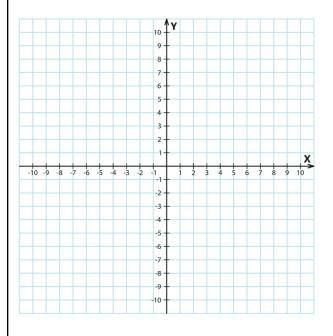
Once graphed we can identify the solution by looking for the point of intersection.

Let's graph the system below and identify the solution:

$$y = \frac{2}{3}x + 4$$

$$4x = y + 6$$

Solving Systems by Graphing (5:32)



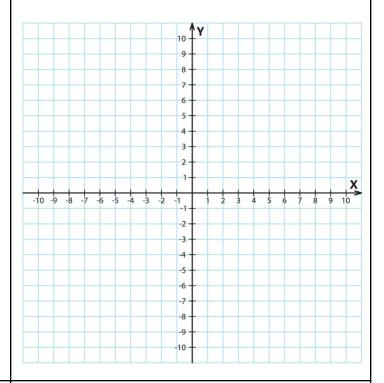
Practice

1. Solve this system of equations by graphing.

$$y = -\frac{1}{3}x - 2$$

$$6 = y + 3x$$

Solving Systems by Graphing Practice (5:20)



Determining Solution Types Without a Graph

To determine the number of solutions a system has without graphing it the system must be written in slope intercept form, y = mx + b

For the system:

$$y = 3x + 2$$
 $y = 3x + 3$

The system is already written in slope intercept form.

We can now look at slope and y-intercept to determine the solution type.

For this system the equations have the _____ slope and _____ y-intercepts.

This means that there would be

<u>Determining Solution Types</u> Without a <u>Graph</u> (1:42)

Practice	Identifying Solutions 2 (3:20)
What is the solution type for this system?	
6x = 3y + 9	
y = 2x + 3	
What is the solution type for this system?	Identifying Solutions 3 (3:38)
3x = 3y + 6	
y = 1/2x + 3	
What is the solution type for this system?	Identifying Solutions 4 (2:08)
y = 4x + 2	
$\begin{vmatrix} 2y &= 8x &+ & 4 \end{vmatrix}$	

Solving A Real-World System of Two Equations by Graphing

You have learned about using linear equations to represent real-world problems and how their graphs can help to make predictions and better understand the situation.

Similarly, we can use systems of linear equations to help find a solution to real-world problems.

The next set of steps can be useful in finding and interpreting the solution to a real-world problem.

Step 1: Define and assign variables

Step 2: Write two equations to represent the information given in the problem

Step 3: Solve the system of linear equations by graphing, and check the solution

Step 4: Interpret the solution

A teacher can purchase packs of dry erase markers at a local store for \$4 each. He can also buy them from an online retailer for \$3 each and \$5 shipping and handling.

How many packs of dry erase markers would the teacher need to purchase for the cost from the local store to be the same as the cost from the online retailer?

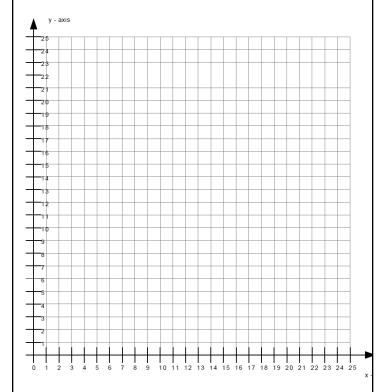
Solving A Real-World System of Equations by Graphing (4:40)

Let x = _____

Let y = _____

Equation for local store:

Equation for online retailer:



Practice

5. Johnny's parents are planning a party for him at the local trampoline park. There are two types of party planner options.

Option 1: They can pay \$60 for the room and cake, and then \$3 per guest.

Option 2: Pay for an all-inclusive party package (room, cake and unlimited guests) for \$120.

If we have y represent the cost for the party and x represent the number of guests. Option 2 can be represented by y = 120.

- What is the equation for option 1?
- How many guests have to come to make it the same price for both options?

