

Important Formulae TIME,SPEED,DISTANCE

i) $\text{Speed} = \text{Distance} / \text{Time}$

ii) $\text{Time} = \text{Distance} / \text{speed}$

iii) $\text{Distance} = \text{speed} \times \text{time}$

iv) $1 \text{ km/hr} = 5/18 \text{ m/s}$

v) $1 \text{ m/s} = 18/5 \text{ km/hr}$

vi) If the ratio of the speed of A and B is $a:b$, then the ratio of the time taken by them to cover the same distance is $1/a : 1/b$ or $b:a$

vii) Suppose a man covers a distance at x kmph and an equal distance at y kmph, then the **AVERAGE SPEED** during the whole journey is $2xy/x+y$ kmph

Out of time, speed and distance we can compute any one of the quantities when we happen to know the other two. For example, suppose we drive for 2 hours at 30 miles per hour, for a total of 60 miles.

If we know the time and the speed, we can find the **distance**

$$2 \text{ hour} \times 30 \text{ miles/hour} = 60 \text{ miles}$$

If we know the time and the distance, we

can find the **speed**

$$60 \text{ miles} / 2 \text{ hours} = 30 \text{ miles/hour}$$

Example:

A train meets with an accident and moves at $(3/4)^{\text{th}}$ its original speed. Due to this, it is 20 min late. Find the original time for the journey beyond the point of accident?

Method 1:

Think about 2 diff. situations, 1st with accident and another w/o accident. As distance in both the cases is constant

$$\text{So } V_1 V_2 = T_2 T_1$$

$$\Rightarrow V_1 [(3/4) \times V_1] = T_1 + 20 T_1$$

$$\Rightarrow 43 = T_1 + 20 T_1$$

$$\Rightarrow T_1 = 60$$

Method 2:

Velocity decreases by 25% ($3/4$ of original speed $\Rightarrow$ decrement by $1/4$) so time will increase by 33.3% ($4/3$ of original time $\Rightarrow$ increment by $1/3$)

$$\text{now, } 33.3\% = 20 \text{ min}$$

=>100%=60 min

3. Relative Speed

Case 1:

Two bodies *are moving in opposite directions* at speed V_1 & V_2 respectively. The relative speed is defined as $V_r = V_1 + V_2$

Case 2:

Two bodies are moving *in same directions* at speed V_1 & V_2 respectively. The relative speed is defined as $V_r = |V_1 - V_2|$

4. Train Problems

The basic equation in train problem is the same $\text{Speed} = \frac{\text{Distance}}{\text{Time}}$
The following things need to be kept in mind while solving the train related problems.

- When the train is crossing a moving object, the speed has to be taken as the relative speed of the train with respect to the object.
- The *distance to be covered when crossing an object*, whenever trains crosses an object will be equal to: *Length of the train + Length of the object*

5. Boats and Streams

Let,

$U =$ Velocity of the boat in still water

$V =$ Velocity of the stream.

Upstream:

While moving in **upstream**, distance covered, distance covered, $S = (U - V)T$

Downstream:

In case of **downstream**, distance covered, distance covered, $S = (U + V)T$

6. Clock

For clock problems consider the clock as a circular track of 60km.

Min. hand moves at the speed of 60km/hr (think min. hand as a point on the track) and hour hand moves at 5km/hr and second hand at the speed of 3600 km/hr.

Relative speed between HOUR hand and MINUTE hand = 55

