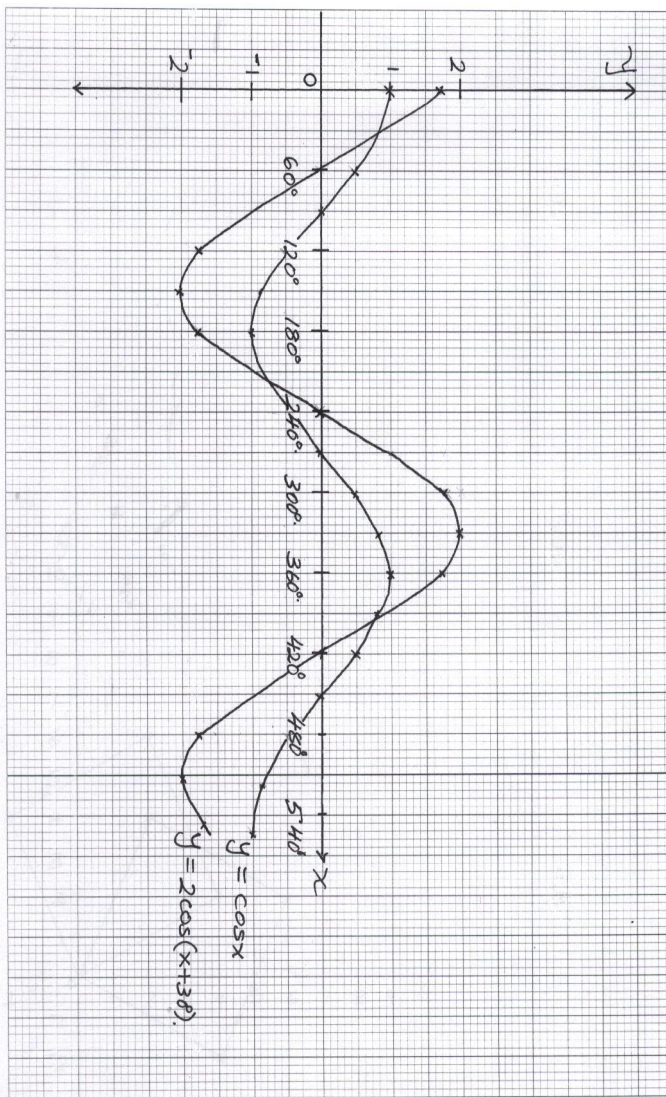


2. Trigonometry 2

1	$\sin \frac{5}{2}x = -\frac{1}{2}$ $\frac{5}{2}x = 210^{\circ}, 330^{\circ}, 390^{\circ}$ $x = 84^{\circ}, 132^{\circ}, 156^{\circ}$	B ₁ B ₁	Allow for any 2 ✓ angles																														
2	a) <table border="1"><thead><tr><th>X⁰</th><th>60⁰</th><th>120⁰</th><th>180⁰</th><th>240⁰</th><th>300⁰</th><th>360⁰</th><th>420⁰</th><th>480⁰</th><th>540⁰</th></tr></thead><tbody><tr><td>cosX</td><td>0.50</td><td>-0.5 0</td><td></td><td>-0.5</td><td></td><td>1.00</td><td>0.50</td><td>-0.5</td><td>-1.0</td></tr><tr><td>2cos(x+30)</td><td>0.00</td><td></td><td>-1.7 3</td><td></td><td>1.73</td><td>1.73</td><td>0.00</td><td>-1.7 3</td><td>-1.7 3</td></tr></tbody></table> b) i) Period = 3600 ii) Phase angle = 300	X ⁰	60 ⁰	120 ⁰	180 ⁰	240 ⁰	300 ⁰	360 ⁰	420 ⁰	480 ⁰	540 ⁰	cosX	0.50	-0.5 0		-0.5		1.00	0.50	-0.5	-1.0	2cos(x+30)	0.00		-1.7 3		1.73	1.73	0.00	-1.7 3	-1.7 3	B2 B1 B1	allow B1 for 7✓ values ✓ values to 2 d.p. apply ow-1 if given to other d.p
X ⁰	60 ⁰	120 ⁰	180 ⁰	240 ⁰	300 ⁰	360 ⁰	420 ⁰	480 ⁰	540 ⁰																								
cosX	0.50	-0.5 0		-0.5		1.00	0.50	-0.5	-1.0																								
2cos(x+30)	0.00		-1.7 3		1.73	1.73	0.00	-1.7 3	-1.7 3																								



S_1

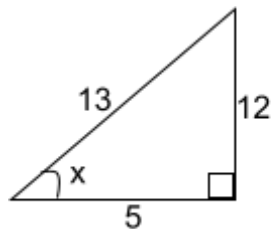
P_1 for all values by
Plotted

C_1 smooth curve
 $y = \cos x$

C_1 smooth curve
 $y = 2\cos(x+30^\circ)$

c)	$37.5^\circ \leq x \leq 217.5^\circ$ $397.5^\circ \leq x \leq 540^\circ$	B_1 B_1	Allow ± 0.5
		10	

$$\begin{aligned}
 1. \quad & 5 \sin x + \cos x \\
 &= 5 \left[\frac{-5}{13} \right] \\
 &= \frac{60}{13} - \frac{5}{13} = \frac{55}{13} \\
 &= \frac{1}{13}
 \end{aligned}$$



$$\begin{aligned}
 2. \quad & \frac{2 \cos 3\theta}{2} = \frac{1}{2} \\
 & \cos 3\theta = 0.5 \\
 & 3\theta = \cos^{-1} 0.5 \\
 & 3\theta = 60^\circ, 300^\circ, 420^\circ, 66^\circ, 78^\circ, 102^\circ
 \end{aligned}$$

✓ Identification of exact number of
quadrants to satisfy the equation.
✓ Values of at least 4 soln. of θ

$$\therefore \theta = 20^\circ, 100^\circ, 140^\circ, 220^\circ, 260^\circ, 340^\circ$$

$$3.. \quad \frac{\frac{1}{2} X^{\frac{\sqrt{3}}{2}}}{\sqrt{3/2} X^{1/\sqrt{2}}}$$

$$\frac{\frac{\sqrt{3}}{4}}{\sqrt{3/2} - 1/\sqrt{2}} X^{\frac{\sqrt{3}}{2} - \frac{1}{\sqrt{2}}}$$

$$\frac{\frac{3}{4} - \frac{\sqrt{3}}{4\sqrt{2}}}{\frac{3}{4} - \frac{1}{2}} = \frac{\frac{3}{4} - \frac{\sqrt{3}}{4\sqrt{2}}}{\frac{1}{4}} = \frac{3}{2} + \frac{\sqrt{3}}{\sqrt{2}}$$

$$\begin{aligned} 4. \quad a) \quad b^2 &= a^2 + c^2 - 2ac \cos B \\ b^2 &= 7^2 + 5^2 - 2 \cdot 5 \cdot 7 \cos 100^\circ \\ &= 74 - 70(-0.173648) \\ &= 74 + 12.15537 \\ b^2 &= 86.15537 \\ b &= 9.28199 \end{aligned}$$

$$AC = 9.3 \text{ km}$$

$$b) \quad \frac{9.3}{\sin 100^\circ} = \frac{5}{\sin \theta}$$

$$\sin \theta = \frac{5 \sin 100^\circ}{9.3} = 0.529466$$

$$\theta = 31.9694^\circ$$

$$\theta \approx 32^\circ$$

$$32^\circ - 20^\circ = 12^\circ$$

$$\text{Bearing} = 360^\circ - 12^\circ = 348^\circ$$

$$c) \quad 020^\circ$$

5.

$$\overline{\sin 60} = \sqrt{3/2} \quad \frac{1}{2}$$

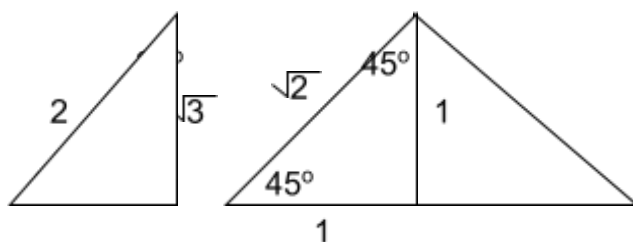
$$\overline{\sin 45} = \frac{1}{\sqrt{2}} \quad \frac{\sqrt{3}}{2} \quad \frac{1}{\sqrt{2}} - \frac{1}{2}$$

$$= \frac{\frac{\sqrt{3}}{2\sqrt{2}} - \frac{1}{\sqrt{2}}}{\sqrt{2}}$$

$$= \frac{\frac{\sqrt{6}}{4} - \frac{\sqrt{2}}{2}}{2}$$

$$= \frac{\sqrt{6} - 2\sqrt{2}}{4}$$

6.



$$1 + \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2}$$

$$\frac{1 + \sqrt{3} \times 2\sqrt{2}}{2\sqrt{2} \quad 2\sqrt{2}}$$

$$\frac{1}{1} + \frac{2\sqrt{6}}{4}$$

$$\frac{4 + 2\sqrt{6}}{4}$$

$$7. \quad \frac{\sqrt{5}(2\sqrt{2} + \sqrt{5}) + \sqrt{2}(2\sqrt{2} - \sqrt{5})}{(2\sqrt{2})^2 - (\sqrt{5})^2}$$

$$\frac{2\sqrt{10} + 5 + 4 - \sqrt{10}}{8 - 5}$$

$$- \frac{9 + \sqrt{10}}{3}$$

$$3 + \frac{1}{3}\sqrt{10}$$

$$8. a) \quad b^2 = a^2 + c^2 - 2ac \cos B$$

$$b^2 = 7^2 + 5^2 - 2 \cdot 5 \cdot 7 \cos 100$$

$$= 74 - 70(-0.173648)$$

$$= 74 + 12.15537$$

$$b^2 = 86.15537$$

$$b = 9.28199$$

$$AC = 9.3 \text{ km}$$

$$b) \quad \frac{9.3}{\sin 100} = \frac{5}{\sin \theta}$$

$$\sin \theta = \frac{5 \sin 100}{9.3} = 0.529466$$

$$\theta = 31.9694$$

$$\theta \approx 32^\circ$$

$$32 - 20 = 12^\circ$$

$$\text{Bearing} = 360^\circ - 12^\circ$$

$$= 348^\circ$$

$$c) \quad 020^\circ$$