#### **Syllabus**

# Mathematics - II for Electrical and Electronics Engineering Stream

#### **Module-1: Vector Calculus**

Introduction to Vector Calculus in EC & EE engineering applications. Vector Differentiation: Scalar and vector fields. Gradient, directional derivative, curl and divergence - physical interpretation, solenoidal and irrotational vector fields. Problems. Vector Integration: Line integrals, Surface integrals. Applications to work done by a force and flux. Statement of Green's theorem and Stoke's theorem. Problems.

Self-Study: Volume integral and Gauss divergence theorem.

Applications: Conservation of laws, Electrostatics, Analysis of streamlines and electric potentials.

# **Module-2: Vector Space and Linear Transformations**

Importance of Vector Space and Linear Transformations in the field of EC & EE engineering applications. Vector spaces: Definition and examples, subspace, linear span, Linearly independent and dependent sets, Basis and dimension. Linear transformations: Definition and examples, Algebra of transformations, Matrix of a linear transformation. Change of coordinates, Rank and nullity of a linear operator, Rank-Nullity theorem. Inner product spaces and orthogonality.

Self-study: Angles and Projections.Rotation, reflection, contraction and expansion.

Applications: Image processing, AI & ML, Graphs and networks, Computer graphics.

#### **Module-3: Laplace Transform**

Importance of Laplace Transform for EC & EE engineering applications. Existence and Uniqueness of Laplace transform (LT), transform of elementary functions, region of convergence. Properties—Linearity, Scaling, t-shift property, s-domain shift, differentiation in the s-domain, division by t, differentiation and integration in the time domain. LT of special functions periodic functions (square wave, saw-tooth wave, triangular wave, full & half wave rectifier), Heaviside Unit step function, Unit impulse function. Inverse Laplace Transforms: Definition, properties, evaluation using different methods, convolution theorem (without proof), problems, and applications to solve ordinary differential equations.

Self-Study: Verification of convolution theorem.

Applications: Signals and systems, Control systems, LR, CR & LCR circuits

#### Module-4: Numerical Methods -1

Importance of numerical methods for discrete data in the field of EC & EE engineering applications. Solution of algebraic and transcendental equations: Regula-Falsi method and Newton-Raphson method (only formulae). Problems. Finite differences, Interpolation using Newton's forward and backward difference formula, Newton's divided difference formula and Lagrange's interpolation formula (All formulae without proof). Problems. Numerical

integration: Trapezoidal, Simpson's (1/3)rd and (3/8)th rules(without proof). Problems.

Self-Study: Bisection method, Lagrange's inverse Interpolation, Weddle's rule. Applications: Estimating the approximate roots, extremum values, area, volume, and surface area.

## Module-5: Numerical Methods -2

Introduction to various numerical techniques for handling EC & EE applications. Numerical Solution of Ordinary Differential Equations (ODEs): Numerical solution of ordinary differential equations of first order and first degree - Taylor's series method, Modified Euler's method, Runge-Kutta method of fourth order and Milne's predictor corrector formula (No derivations of formulae). Problems.

Self-Study: Adam-Bashforth method.

Applications: Estimating the approximate solutions of ODE for electric circuits.

### **Laboratory experiments**

Suggested software's: Mathematica/MatLab/Python/Scilab

- 1. Finding gradient, divergent, curl and their geometrical interpretation and Verification of Green's theorem
- 2. Computation of basis and dimension for a vector space and Graphical representation of linear transformation
- 3. Visualization in time and frequency domain of standard functions
- 4. Computing inverse Laplace transform of standard functions
- 5. Laplace transform of convolution of two functions
- 6. Solution of algebraic and transcendental equations by Regula-Falsi and Newton-Raphson method
- 7. Interpolation/Extrapolation using Newton's forward and backward difference formula
- 8. Computation of area under the curve using Trapezoidal, Simpson's (1/3)rd and (3/8)th rule
- 9. Solution of ODE of first order and first degree by Taylor's series and Modified Euler's method
- 10. Solution of ODE of first order and first degree by Runge-Kutta 4th order and Milne's predictor-corrector method