

# Engineering Assignment:

## Flux

Student learning outcomes:

|       |                                                        |
|-------|--------------------------------------------------------|
| 2.7.4 | Convert from rectangular to spherical coordinates      |
| 2.3.1 | Calculate the dot product of two given vectors         |
| 2.4.1 | Calculate the cross product of two given vectors       |
| 2.4.2 | Use determinants to calculate a cross product          |
| 6.2.4 | Describe the flux and circulation of a vector field    |
| 6.4.3 | Calculate circulation and flux on more general regions |
| 6.7.3 | Use Stokes' theorem to calculate a surface integral    |

### Assignment Overview

Recall  $\text{Flux} = \int \int_S \vec{F} \cdot \vec{n} dS$  gives the flux of a vector field  $F$  with unit normal vector  $n$

through a surface  $S$ .

**Exercise 1:** Find the flux where vector field  $\vec{F} = \langle x^2, y^2, z \rangle$  and  $S$  is the surface given by the paraboloid  $z = 1 - x^2 - y^2$  and  $z \geq 0$ .

Gauss's Law for electric field states that the flux through a closed surface is

$$\Phi_E = \oint_S \vec{E} \cdot \vec{n} dA = \frac{Q}{\epsilon_0},$$

for any closed surface  $S$  containing charge  $Q$ , where  $E$  is the electric field, and

$\epsilon_0$  is a constant representing the permittivity of free space in  $C/Vm$ .

**Exercise 2:** Find the electric flux through the surface of a charged sphere  
with radius 2 meter,

when the charge  $Q$  is  $2 \times 10^{-10} \text{ C/m}^2$ . Use 2 methods with each part of Gauss's  
Law.