

Pravilnik o diplomskim radovima,

https://www.mathos.unios.hr/wp-content/uploads/2023/11/Pravilnik_o_diplomskim_radovima_-_p_otpisano.pdf

Prijedlog tema za diplomske radove:

Verižni razlomci i primjene (Ivana Jozinović)

Literatura:

1. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019.
2. A. Dujella, M. Maretić, *Kriptografija*, Element, Zagreb, 2007.
3. A. Dujella, *Verižni razlomci i problem kalendara*, Matematika i škola I (1999), 74-77.
4. T. Andrescu, T. Andrica, *An Introduction to Diophantine Equations*, GIL Publishing House, Zalau, 2002.
5. C. D. Olds, *Continued Fractions*, Random House, New York, 1963.

Zajmovi (Tea Osmanović)

(Zajmovi, interkalarna kamata, efektivna kamatna stopa (EKS) u praksi i konstrukcija barem 2 primjera iz prakse na kojima se računa EKS.)

1. G. Bronson, R. Bronson, M. Kieff. *Mathematics for Business*, Seventh Edition, Mercury Learning and Information, 2021.
2. S. A. Broverman, *Mathematics of Investment and Credit*, ACTEX Publication, 2010.
3. Odluka o efektivnoj kamatnoj stopi, NN 105/2017,
https://narodne-novine.nn.hr/clanci/sluzbeni/2017_10_105_2417.html
4. Odluka o efektivnoj kamatnoj stopi kreditnih institucija i kreditnih unija te ugovaranju usluga s potrošačima, HNB, Zagreb, 2010.
https://www.hnb.hr/documents/20182/122188/h-odluka-eks-ugovaranje-usluga-potrosacima_npt.pdf/9abdaed3-4514-4b22-835d-55ea9d98a561

Eliptičke krivulje nad poljem racionalnih brojeva

Literatura:

1. J. H. Silverman, *Rational Points on Elliptic Curves*, Springer, New York, 1992.
2. A. Dujella, *Algoritmi za eliptičke krivulje*, PMF - Matematički odjel, Sveučilište u Zagrebu, 2009.
<https://web.math.pmf.unizg.hr/~duje/elipticke/algelip.pdf>

3. S. Schmitt, H. G. Zimmer, *Elliptic Curves – A Computational Approach*, Walter de Gruyter, Berlin – New York, 2003.

Pravilnik o završnim radovima,

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Prijedlog tema za završne radove:

Linearne diofantske jednadžbe (Lucija Begić)

Uz dokaz osnovnih tvrdnji o rješivosti (uključiti Euklidov algoritam i prošireni EA), primjene ovakvih jednadžbi, sustave linearnih diofantskih jednadžbi. Uključiti i natjecateljske zadatke u kojima se javljaju linearne diofantske jednadžbe.

Literatura:

1. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019.
2. C. D. Olds, *Continued Fractions*, Random House, New York, 1963.
3. R. Radha, G. Janaki, *Applications Of Diophantine Equations In Chemical Reactions And Cryptography*, Turkish Journal of Computer and Mathematics Education **12** (2021), 3175-3178.
4. D. Kaur, M. Sambhor, *Diophantine Equations and its Applications in Real Life*, International Journal of Mathematics And its Applications **5** (2017), 217–222.
<https://ijmaa.in/index.php/ijmaa/article/download/811/798/858>
5. B. Pavković, B. Dakić, P. Mladinić, *Elementarna teorija brojeva*, Hrvatsko matematičko društvo, Zagreb, 1994.
6. *Natjecanja iz matematike u Republici Hrvatskoj*,
<http://www.antonija-horvatek.from.hr/natjecanja-iz-matematike/natjecanja-iz-matematike.htm>
7. T. Andrescu, T. Andrica, *Number Theory: Structures, Examples and Problems*, Birkhäuser, 2009.
8. T. Andrescu, T. Andrica, *An Introduction to Diophantine Equations*, GIL Publishing House, Zalau, 2002.
9. R. Amer, *The mathematical analysis of Linear Diophantine equations with two and three variables and Its Applications*, The Egyptian International Journal of

Engineering Sciences and Technology 42 (2023), 23-28.

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10. O. Cira, F. Smarandache, Solving Diophantine Equations, 2014,
<https://fs.unm.edu/SolvingDiophantineEquations.pdf>
11. M. Xiong , *Solving Linear Diophantine Equation and Simultaneous Linear Diophantine Equations with Minimum Principles*, International Mathematical Forum **17** (2022), 143 – 161.
<https://www.m-hikari.com/imf/imf-2022/1-4-2022/p/xiongIMF1-4-2022.pdf>

Pitagorine trojke (Petra Pešut)

Navesti više dokaza m, n formule za generiranje Pitagorinih trojki kao i neke druge metode za generiranje Pitagorinih trojki. (Mogu se i navesti neki kodovi koji generiraju Pitagorine trojke i/ili pronalaze sve Pitagorine trojke koje imaju jedan zadan element.)

1. K. Conrad, *Pythagorean Triples*,
<https://kconrad.math.uconn.edu/blurbs/ugradnumthy/pythagtriple.pdf>
2. B. Pavković, B. Dakić, P. Mladinić, *Elementarna teorija brojeva*, Hrvatsko matematičko društvo, Zagreb, 1994.
3. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019.
4. I. Matić, Uvod u teoriju brojeva, Sveučilište Josipa Jurja Strossmayera u Osijeku - Odjel za matematiku, Osijek, 2015.
<https://www.mathos.unios.hr/wp-content/uploads/uploads/617.pdf>
5. Journal of Mathematics Research **13** (2021), doi:10.5539/jmr.v13n3p63.
<https://doi.org/10.5539/jmr.v13n3p63>
6. D. DeWolf , B. Viswanathan, *Extending Fibonacci's Method for Computing Pythagorean Triples*, International Journal of Mathematics and Computer Science **17**(2022), 839–845. <https://future-in-tech.net/17.2/R-DarienDeWolf.pdf>
7. J. Rukavicka, *Dickson's Method for Generating Pythagorean Triples Revisited*, European Journal of Pure and Applied Mathematics **6** (2013), 363-364.
<https://www.ejpam.com/index.php/ejpam/article/view/1844/309>
8. E. Hammes, *Unifications of Pythagorean Triple Schema*, Undergraduate Honors Theses, 2019.
<https://dc.etsu.edu/cgi/viewcontent.cgi?article=1619&context=honors>

9. R. H. Dye, R. W. D. Nickalls, A new algorithm for generating Pythagorean triples, *The Mathematical Gazette* **82** (1998), 86-91.
<https://r-knott.surrey.ac.uk/Pythag/2065.pdf>

Edukativne matematičke igre (Marko Lozančić)

(Teorija vezana uz razvoj i klasifikaciju igara, primjeri digitalnih matematičkih igara.)

1. S. Adipat, K. Laksana, K. Busayanon, A. Asawasowan, B. Adipat, *Engaging students in the learning process with game-based learning: The fundamental concepts*, International Journal of Technology in Education (IJTE), 4(3), 2021, 542-552.
<https://doi.org/10.46328/ijte.169>
2. K. Becker, *What's the difference between gamification, serious games, educational games, and game-based learning?*, Academia Letters, 2021.
https://edisciplinas.usp.br/pluginfile.php/7783395/mod_resource/content/1/What_s_the_difference_between_gamificati.pdf
3. P. Felicia, *Using educational games in the classroom: guidelines for successful learning outcomes*, European Schoolnet, 2020.
<https://videogameseurope.eu/wp-content/uploads/2020/10/2020-GiS-handbook-for-teachers-FINAL.pdf>
4. A. Bouwer, S. Abrantes Garcêz Palha, urednici, *GAMMA Priručnik za nastavnike: učenje temeljeno na igri*, Erasmus+ projekt GAMMA, 2023.
https://drive.google.com/file/d/1wt_LsZxsZIEa2OdxsFRRuj6w83x2qGxe/view
5. *GAMMA games*, Erasmus+ projekt GAMMA, 2023.
<http://www.project-gamma.eu/project-outputs/io3-gamma-games/>

Aritmetičke funkcije (Ivana Pavić)

Literatura:

1. G. A. Jones, J. M. Jones, *Elementary Number Theory*, Springer-Verlag, London, 2004.
2. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019.
3. O. Cira, F. Smarandache, *Various Arithmetic Functions and their Applications*, PONS asbl, Bruxelles, 2016.

Izračunavanja u teoriji brojeva pomoću programskog paketa PARI/GP

(PARI/GP je algebarski sustav dizajniran za brza izračunavanja u teoriji brojeva. Ovdje treba napraviti uvod u PARI/GP i navesti primjere programa koji se koriste za izračunavanja u teoriji brojeva.)

Literatura:

1. A. Das, *Computational Number Theory*, CRC Press, Boca Raton, 2013. https://api.pageplace.de/preview/DT0400.9781482205824_A37765833/preview-9781482205824_A37765833.pdf
2. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019. *The PARI Group*, PARI/GP version 2.15.4, Univ. Bordeaux, 2023, <http://pari.math.u-bordeaux.fr/>.

Poligonalni brojevi (N. Matovina)

Literatura:

1. M. B. Nathanson. *Additive Number Theory: The Classical Bases*, Springer, New York, 1996. <http://www.alefenu.com/libri/nathansonbases.pdf>
2. O. Chipatala, *Polygonal numbers*, Kansas state university, 2016, Manhattan, <https://core.ac.uk/download/pdf/77977823.pdf>
3. E. Forhan, *Polygonal Numbers and Finite Calculus*, 2007. <https://documents.kenyon.edu/math/Forhan07.pdf>
4. T. Albany, *An Introduction to Polygonal Numbers, Their Patterns, and Relationship to Pascal's Triangle*, 2015. <https://bpb-us-e1.wpmucdn.com/sites.psu.edu/dist/f/26362/files/2015/04/New-Paper.pdf>

Savršeni brojevi (Iva Crndić)

1. O. Knill, *The oldest open problem in mathematics*, <https://people.math.harvard.edu/~knill/seminars/perfect/handout.pdf>
2. F. Vega, *Note for the Perfect Numbers*, <https://www.cambridge.org/engage/api-gateway/coe/assets/orp/resource/item/6626490921291e5d1d5ea0a5/original/note-for-the-perfect-numbers.pdf>
3. J. Voight, *Perfect numbers: an elementary introduction*, <https://jvoight.github.io/notes/perfelem-051015.pdf>
4. D. P. Shukla, S. Yadav, *Generalized Perfect Numbers*, <https://bibliotekanauki.pl/articles/746659.pdf>
5. P. Pollack, V. Shevelev, *On perfect and near-perfect numbers*, *Journal of Number Theory* 132 (2012), 3037-3046. <https://pollack.uga.edu/pnp-4.pdf>
6. S. J. Benkoski, P. Erdős, *On Weird and Pseudoperfect Numbers*, *Mathematics of Computation* 28 (1974), 617-623. https://users.renyi.hu/~p_erdos/1974-24.pdf

Završni radovi

Kongruencije (Stella Kobašević)

(Uključiti polinomijalne kongruencije (Henselovu lemu).)

Literatura:

1. A. Adler, J. Coury, *The Theory of Numbers.*, Jones & Bartlett Publishers, London, 1995.
2. H. H. Hardy, E. M. Wright, D. R. Heath-Brown, J. H. Silverman, *Introduction to the Theory of Numbers*, Posts and Telecom Press, 2008.
3. J. Kraft, L. Washington, *An Introduction to Number Theory with Cryptography*, CRC Press, Boca Raton, 2018.
4. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019.
5. Tattersall, *Elementary number theory in nine chapters*, Cambridge University Press, New York, 1999
6. W. Sierpinski, *Elementary Theory of Numbers*, North Holland, Warszawa, 1985.
7. A. Gorodnik, *Polynomial congruence modulo primes and prime powers*,
<https://www.math.uzh.ch/gorodnik/nt/>
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<https://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.692.576&rep=rep1&type=pdf>

Fibonaccijski brojevi (Jovana Vidović)

(Fibonaccijski brojevi u teoriji brojeva (svojstva vezana uz djeljivost, dokaz za gornju ogradu za broj koraka u Euklidovom algoritmu).)

Literatura:

1. J. R. Chasnov, *Fibonacci Numbers and the Golden Ratio*, The Hong Kong University of Science and Technology, Hong Kong, 2016.
2. A. Dujella, *Fibonaccijski brojevi*, HMD, Zagreb, 2000.
3. J. H. Halton, *On the divisibility properties of Fibonacci numbers*, *Fibonacci Quart.* **4** (1966), 217–240.
<https://www.fq.math.ca/Scanned/4-3/halton.pdf>
4. W. Raji, *An Introductory Course in Elementary Number Theory*, The University of Southern Mississippi, lecture notes, 2017.
https://www.math.usm.edu/perry/old_classes/mat421sp17/An-Introductory-Course-in-Elementary-Number-Theory.pdf

Načini obračuna kamata (Maja Kaurin)

Diplomski radovi

Kvadratne diofantske jednadžbe (Sara Matošić)

(Pellova i pellovske jednadžbe s naglaskom na jednadžbe koje se svode na pellovske.)

1. T. Andreescu, T. Andrica, *An Introduction to Diophantine Equations*, GIL Publishing House, Zalau, 2002.
2. T. Andreescu, D. Andrica, *Quadratic Diophantine Equations*, Springer, 2015.
3. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019.
4. T. Nagell, *Introduction to Number Theory*, Wiley, New York, 1951.

Kvadratni ostatci (Lorena Lamot)

Literatura:

1. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019.
2. G. A. Jones, J. M. Jones, *Elementary Number Theory*, Springer-Verlag, London, 2004.
3. R. A. Mollin, *Fundamental Number Theory with Applications*, CRC Press, New York, 2008.

Kvadratna polja (Marija Turić)

Literatura:

1. A. Dujella, *Teorija brojeva*, Školska knjiga, Zagreb, 2019.
2. I. Gusić, *Ideja jednoznačne faktorizacije I*, math.e **13**, prosinac 2008.
3. A. Baker, *A concise introduction in theory of numbers*, Cambridge University Press, Cambridge, 1984
4. K. Conrad, *Factoring in quadratic fields*,
<http://www.math.uconn.edu/~kconrad/blurbs/ugradnumthy/quadraticundergrad.pdf>

Prosti brojevi (Patricia Pružinac)

Literatura:

1. G. A. Jones, J. M. Jones, *Elementary Number Theory*, Springer-Verlag, London, 2004.
2. Pete L. Clark, *Number Theory: A Contemporary Introduction*,
<http://math.uga.edu/~pete/4400FULL.pdf> 3
3. S. P. Glasby, *Six proofs of the infinity of primes*,
<http://www.cwu.edu/~glasbys/INFINITY.PDF>
4. Gérard P. Michon, *The Set of Primes*, <http://www.numericana.com/answer/primes.htm>
5. *The Prime pages*, <http://primes.utm.edu/index.html>

