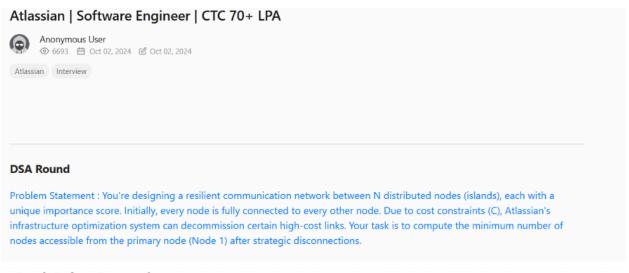
Mentor - Kumar K(https://www.linkedin.com/in/kumark1/)

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Graph Before Destruction:

```
1 (100)

/ | \

/ | \

(1) 2---3----4 (1)
```

Graph After Destruction:

```
1 (100)

/ \

/ \

(1) 2 3----4 (1)
```

(Edges 1-3, 1-4, and 3-4 remain.)

-> Interview Problem: Optimally Disconnecting Atlassian Islands

Context: You're working on a simulation tool at Atlassian that manages a network of islands connected by bridges. Initially, every island is connected to every other island. Each island has an "importance value" associated with it.

A malicious agent, **Alex** (an Atlassian engineer), can destroy some bridges between islands, but only if the total destruction cost remains within a given budget. The cost to destroy the bridge between island i and island j is importance[i] * importance[j].

Your colleague **Jordan** (an Atlassian employee) lives on island 1 and enjoys visiting other islands. After **Alex** destroys some bridges optimally to disconnect the network, we want to determine how many islands **Jordan** can still access, including his own.

Problem Statement: You are given:

- An integer N the number of islands.
- An array A of length N, where A[i] is the importance of the i-th island (1-indexed).
- A long integer C the maximum total cost Alex can spend to destroy bridges.

Each island is initially connected to every other island. Your task is to compute the minimum number of islands (including island 1) that **Jordan** can access after **Alex** destroys bridges optimally (to minimize the size of the connected component that contains island 1).

Input:

 \bullet First line: integer \top — number of test cases.

For each test case:

- Line 1: Two integers N and C.
- Line 2: N integers A[1] A[2] ... A[N] importance values

Output: For each test case, output the minimum number of islands (including island 1) **Jordan** can visit

Analysis:-> What can you do to make sure only "N-1" nodes are visited in total if you start at node-1

- -> Choose node "i" and break its connection with all other nodes so only "N-1" nodes stay connected to each other in the component with node "1"
- -> Hence if you start travelling from node "1" you can visit all N-1 nodes except node "i"
- -> possible answer => a[2]*(sum of all other numbers) -> when node-'2' is removed.

OR

 \Rightarrow a[3]*(sum of all other numbers) \Rightarrow when node-'3' is removed.

OR.

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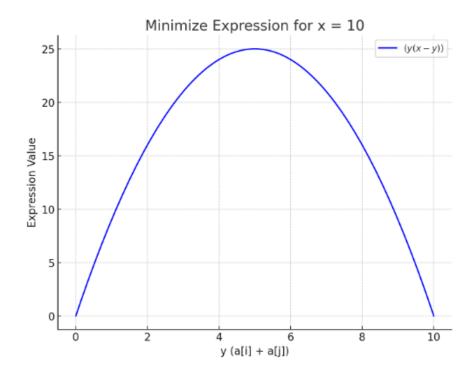
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.

Min of all possibilities \leftarrow C -> then yes it is possible to get answer as N-1

- -> Now try for N-2;
- -> (i,j) will be selected from [2....N]
- -> minimize (a[i]+a[j])*(sum of rest of the numbers)
- \rightarrow x = sum of all numbers; y = a[i]+a[j];
- -> minimize (y*(x-y))

Graph created.



-> Hence "y" can only be either sum of two largest numbers in range [2...N] or two smallest numbers in range [2...N]

-> do it and minimize;

-> Same technique if you try to get answer as N-3; N-4; 1

Implementation :->

C++ https://ideone.com/hZDGhb

Java.

Py