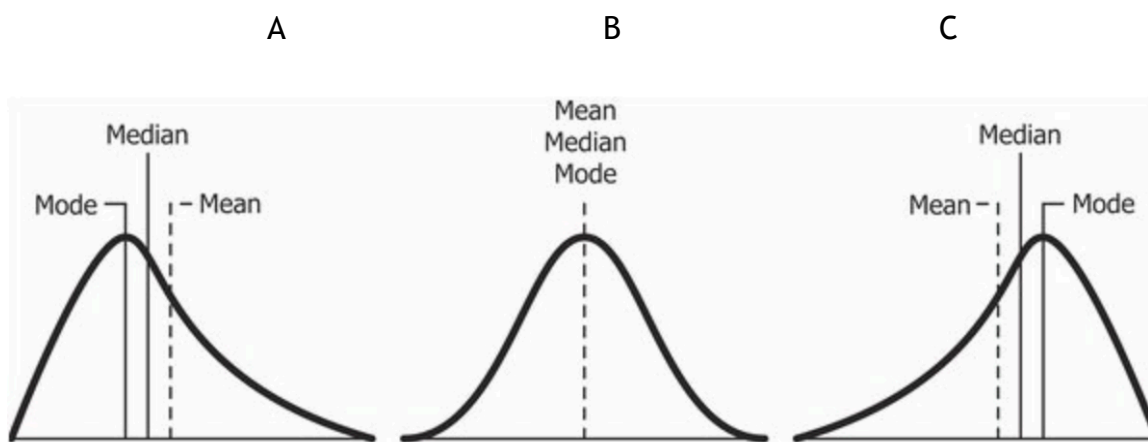


Data Analysis In-Class Worksheet #06: Distribution & CI

Distributions

1. A normal distribution has 3 SDs above the mean and 3 SDs below the mean
2. Which of the following is an outlier? ☐ $Z = -.3$ ☒ $Z = 5$ ☐ $Z = 0$
3. Which of these is a negative skew? ☒ $-.3$ ☐ 1.2 ☐ 0
4. Which of the following graphs shows a **positive skew (Right Tail)**?
☒ A ☐ B ☐ C



5. Our class dataset is a sample of the population of all Williamsburg properties
6. The Shapiro-Wilk test determines if the population from which a sample is drawn is normally distributed or not.
7. If the test result has a p (probability) value of .04, that means
☐ the population is normally distributed
☒ the population is NOT normally distributed (If $p < 0.05$, reject normality)
8. If the test result has a p (probability) value of .27, that means
☒ the population is normally distributed (If $p > 0.05$, accept normality)
☐ the population is NOT normally distributed

9. If we want to convert a non-normal variable into a normal distribution, we can try to take log or natural log of the variable.

10. The binomial distribution is the distribution of Bernoulli trials, which depends on p (probability), and n (sample size)

Confidence Interval

11. How does the point estimate differ from an interval estimate?

The point estimate is a single value (e.g., 17 years old), while the interval estimate gives you a range (e.g., 11-19 years old) with a confidence level

12. What is Standard Error? It's an estimate of the population's standard deviation

13. Which estimate indicates a higher level of confidence?

☒ I bet that Abhishek will get married between 28 and 30 years old (narrow range, higher precision)

☐ I bet that Abhishek will get married between 18 and 95 years old

14. Take a sample of 16 stocks from a large population, with a sample mean return of 5.2%, and a sample standard deviation of 1.5%

Given $n=16$

$$\mu_X = 5.2\%$$

$$\sigma_X = 1.5\%$$

$$\mu = \mu_X \pm Z_{(1-\alpha)/2} * \sigma_X / \sqrt{n}$$

μ is population mean

μ_X is sample mean

$Z_{(1-\alpha)/2}$ is Z-score corresponding to the confidence level

σ_X standard deviation

n sample size

σ_X / \sqrt{n} is standard error (SE)

15. Calculate 95% confidence interval for the population mean

Z-score corresponding to 95% confidence interval is 1.96

$$\mu = \mu_X \pm Z_{(1-\alpha)/2} * \sigma_X / \sqrt{n}$$

$$= 5.2\% \pm 1.96 * 1.5\% / \sqrt{16}$$

$$= (4.465\%, 5.935\%)$$

16. How much is the margin of error?

$$\text{Margin of Error (ME)} = Z_{(1-\alpha)/2} * \sigma_x / \sqrt{n}$$

$$1.96 * 1.5\% / \sqrt{16}$$

$$0.735\%$$

17. How much is the Standard Error?

$$\frac{\sigma_x}{\sqrt{n}}$$

$$1.5\% / \sqrt{16}$$

$$0.375\%$$

Source:

<https://financetrain.com/confidence-interval-population-mean-known-population-variance/>