

Methodological guidelines.

Methods of data grouping

SUMMARY:

The goal of the lesson is to formulate the students' understanding of data grouping as a complex filtering tool.

During the lesson, the students review tasks and filtering methods: they calculate basic statistics for individual columns of the original DataFrame or DataFrame filtered by a given condition, and they come to the conclusion that they need to learn more to work on more complex tasks. The children are introduced to functions for calculating the number of unique occurrences, `value_counts()`, and grouping, `groupby()` and `pivot_table()`, and they compare and evaluate how to use them to solve tasks. They are introduced to a new business term – the “target audience.”










LINKS AND ACCESSORIES:

- [presentation for the lesson](#);
- tasks in VSC and on the platform: [part 1](#), [part 2](#).

EDUCATIONAL OUTCOMES OF THE LESSON

<i>After the lesson, the students will:</i>	<i>The results is achieved when the students:</i>
<p>know:</p> <ul style="list-style-type: none"> • that grouping can be used to find generalized values of characteristics for certain data categories; • the syntax for the <code>value_counts()</code>, <code>groupby()</code>, and <code>pivot_table()</code> methods; • what the term “target audience” means and its significance in terms of market research; <p>understand:</p> <ul style="list-style-type: none"> • what types of tasks can be solved using grouping; • that tasks performed using <code>groupby()</code> can be accomplished more elegantly using <code>pivot_table()</code>; <p>know how to:</p> <ul style="list-style-type: none"> • choose a data grouping method to find the answer to a question; • configure the parameters for grouping methods depending on the task; • get the values of specific indicators from DataFrame and Series obtained using grouping. 	<ul style="list-style-type: none"> • answer the review questions correctly; • participate in the discussion of the new topic and ask clarifying questions; • participate in the discussion of the questions on the dataset; • access the DataFrame elements correctly; • complete the tasks on the platform; • try to correct their own mistakes.

RECOMMENDED LESSON STRUCTURE

Time	Stage	Stage aims
5 min 	Review	<ul style="list-style-type: none"> Do a review of the material from the previous lesson: <ul style="list-style-type: none"> Pandas data structures: Series, DataFrame; filtering data by one or multiple conditions.
5 min 	Discussion: "Data grouping"	<ul style="list-style-type: none"> Formulate the problem: the filtering methods we've studied won't give us the answers to lots of important questions for our analysis. Arrive at the idea that we need to learn new data grouping tools.
20 min 	New topic: "Data grouping methods: simple grouping and calculating unique values"	<ul style="list-style-type: none"> Learn the syntax of the value_counts() method. Learn the syntax of the groupby() method. Learn how to apply multiple methods to grouped data. Learn how to access an element of the Series object obtained as a result of grouping.
15 min 	VSC + Platform. Data grouping	<ul style="list-style-type: none"> Have them complete the task "Grouping. Part 1" on the platform.
5 min 	Break	<ul style="list-style-type: none"> Help the students regain their concentration.
5 min 	Discussion: "Grouping data by multiple characteristics"	<ul style="list-style-type: none"> Go over the questions that require data from multiple columns. Arrive at the idea that they need to learn additional grouping methods.
15 min 	New topic: "Grouping by multiple characteristics. Pivot tables"	<ul style="list-style-type: none"> Go over the syntax of the groupby() method using lists as parameter values. Go over the syntax of the pivot_table() method.
15 min 	VSC + Platform. Data grouping	<ul style="list-style-type: none"> Have them complete the task "Grouping. Part 2" on the platform.
5 min 	Wrapping up the lesson. Reflection	<ul style="list-style-type: none"> Discuss the outcome of the lesson with the students. Answer any questions they have.

Review

(5 min)

Do a review of the previous lesson: Pandas data structures, Series and DataFrame, and filtering data by one or multiple conditions.

Review the material from the previous lesson. Make sure that all the students can navigate the DataFrame structure and understand the essence and purpose of data filtering. Pay special attention to their understanding of the core business questions and their impact on the success of the future product.

#	App Name	Rating	Number of reviews
1	TikTok	4.3	38,330,273
2	YouTube	4.6	117,208,38
3	Instagram	3.8	122,104,613

Series

Discussion: “Data grouping”

(5 min)

Formulate the problem: the filtering methods they've studied give us the answers to lots of important questions for our analysis. Arrive at the idea that they need to learn new data grouping tools.

Procedural comment. Some of the students may say that the last three tasks can be solved using filtering and basic algorithmic constructs. Explain to the students that this is true, but the code will have over a dozen strings to solve the last task. Moreover, there are standard methods in Pandas that will let us solve tasks of this type with a single string of code, and we will discuss those methods during the lesson.

Ask the students to think over the methods to solve the tasks on the slide. Discuss the context in which entrepreneurs need to know the answers to these questions. Explain what a target audience is and what its characteristics are. **Ask the students** why entrepreneurs study markets and target audiences. **Answer:** To make the highest possible profit. For that purpose, you need to understand who the product is for and who is most likely to use it.

Arrive at the conclusion that the first two tasks can easily be solved using filtering, but to solve the remaining three, we will need to learn some more powerful methods. Tell the children that the method that can help us get the data we need is called “grouping,” and that today's lesson will be dedicated to different methods of grouping.

#	App Name	Rating	Number of reviews
1	TikTok	4.3	38,330,273
2	YouTube	4.6	117,208,38
3	Instagram	3.8	122,104,613




Series

New topic: “Methods of grouping data: simple grouping and calculating unique values”

(20 min)

Give a definition of the concept of “grouping.” Discuss how grouping is different from filtering. Next, move on to discussing the tasks that were set during the previous stage of the lesson.

In the first half of the lesson, go over the solutions to the first two tasks. Go over the syntax of the `value_counts()` and `groupby()` methods. Pay special attention to the capability of applying multiple statistical functions to grouped data using the `agg()` method. Show the results of each method.

<p>The <code>value_counts()</code> method</p> <p>The <code>value_counts()</code> method calculates the number of unique values for a characteristic in a column. The method returns the Series object containing unique values of characteristics and the number of rows in the DataFrame with each value.</p> <p>New topic, Methods of data grouping</p> 	<p>The <code>groupby()</code> method</p> <p>The <code>groupby()</code> method lets us group data by one or more characteristic and calculate the necessary statistics for the grouped data.</p> <p>New topic, Methods of data grouping</p> 	<p>The <code>aggregate()</code> method</p> <p>The <code>aggregate()</code> method (abbreviated as <code>agg()</code>) allows us to apply multiple functions to the grouped data at once to calculate statistics. As a parameter, this method takes a list of function names in the form of string constants.</p> <p>New topic, Methods of data grouping</p> 
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VSC + Platform. Data grouping

(15 min)

Have the students work with a dataset. Let the students know that they will need to write the code in VSC and then transfer the answers they get to the platform where the tasks with auto-check are.

If you see that the children are hesitant and having difficulty getting started, do a couple of tasks together with them. Encourage the students to be active in asking questions and comment on what you are doing.

You will find the answers to the tasks and the reference code to get them at the end of the methodological guidelines.

Break

(5 min)

Get the students off their computers. The purpose of the break is to shift their attention and do an activity.

Discussion: “Grouping data by multiple characteristics”

(5 min)

Return to the discussion regarding the dataset. Before answering the last question, recall how an assumption differs from a fact. Ask the students to use the data they have to put forward their own hypotheses about the relationship between the target audience, the cost of the app, and how big it is. Remind the students that a refuted hypothesis also becomes a fact. **For example**, the assumption that all paid apps for each audience are smaller relative to free apps is not true, but the opposite is true.

Discuss how to calculate the minimum and maximum size of the paid and free apps for each target audience. Use the table on the slide to make it more clear. Discuss whether grouping with the `groupby()` method can help with this task. Come to the conclusion that the `groupby()` method can help in solving this task if we apply grouping by multiple characteristics at the same time.

Make a few hypotheses about app sizes for different audiences

Type	Content Rating	min size	max size
Free	Everyone	??	??
	Everyone 10+	??	??
	Teen	??	??
Paid	Everyone	??	??
	Everyone 10+	??	??
	Teen	??	??

Suggest one hypothesis/two hypotheses!

When grouping data by multiple characteristics, we can create groups within groups.

Visually, a group within a group resembles a tree turned **upside down**.

Grouping by several columns can be performed using the `groupby()` method.

New topic: "Grouping by multiple characteristics. Pivot tables"

(15 min)

Solve the task from the previous stage using the `groupby()` method with two characteristics. Discuss that in this case the column names should be sent as a list, and the order in which the elements are sent within the list is important.

The `groupby()` method

The `by` parameter for grouping by two characteristics takes a list of column names.

In our case, it is the column type (Type) and target audience (Content Rating).

```
df.groupby(by = ['Type', 'Content Rating'])['Size'].agg(['max', 'min'])
```

The `groupby()` method groups data by multiple characteristics

Type	Content Rating	min	max
Free	Everyone	0.008301	100.0
	Everyone 10+	0.027344	100.0
	Teen	0.315430	100.0
Paid	Everyone	0.013672	100.0
	Everyone 10+	1.800000	100.0
	Teen	1.200000	99.0

First, we group by type

Then, we group by target audience

Finally, we use the `agg` method to calculate a few statistical indicators

Pay attention to the sequence in which the column names are entered!

Different sequences mean different approaches to grouping.

```
by = ['Type', 'Content Rating']
```

Type	Content Rating	min	max
Free	Everyone	100.0	0.008301
Free	Everyone 10+	100.0	0.027344
Free	Teen	100.0	0.315430
Paid	Everyone	100.0	0.013672
Paid	Everyone 10+	100.0	1.800000
Paid	Teen	99.0	1.200000

```
by = ['Content Rating', 'Type']
```

Content Rating	Type	min	max
Everyone	Free	100.0	0.008301
Everyone	Paid	100.0	0.013672
Everyone 10+	Free	100.0	0.027344
Everyone 10+	Paid	100.0	1.800000
Teen	Free	100.0	0.315430
Teen	Paid	99.0	1.200000

Discuss how to retrieve a specific value from DataFrame after grouping.

How can we retrieve a specific value from the DataFrame after grouping?

Type	Content Rating	min	max
Free	Everyone	0.008301	100.0
	Everyone 10+	0.027344	100.0
	Teen	0.315430	100.0
Paid	Everyone	0.013672	100.0
	Everyone 10+	1.800000	100.0
	Teen	1.200000	99.0

This indicator, for example

Minimum size of a free app for teens

Step 2. Access the value using the temp variable and indexes:

- The first **index** is the name of the aggregate function.
- The second **index** is the name of the first column.
- The third **index** is the name of the second column.

```
temp = df.groupby(by = ['Type', 'Content Rating'])['Size'].agg(['min', 'max'])
print(temp[222][222][222])
```

Minimum size of a free app for teens

Step 2. Access the value using the temp variable and indexes:

- The first **index** is the name of the aggregate function.
- The second **index** is the name of the first column.
- The third **index** is the name of the second column.

```
temp = df.groupby(by = ['Type', 'Content Rating'])['Size'].agg(['min', 'max'])
print(temp['min']['Free']['Teen'])
```

Discuss how a set of indexes can be converted to a value column using the `reset_index()` method. New indexes numbered starting from zero will appear in DataFrame. We will need this method in the future when building graphs.

We can't work with indexes when doing analysis

Type	Content Rating	min	max
Free	Everyone	0.008301	100.0
	Everyone 10+	0.027344	100.0
	Teen	0.35430	100.0
Paid	Everyone	0.03672	100.0
	Everyone 10+	1.800000	100.0
	Teen	1.200000	99.0

Let's turn the indexes into values!
The `reset_index()` method is used for that.

New topic: Grouping data by multiple characteristics

The `reset_index()` method

The `reset_index()` method allows us to turn indexes into values by reindexing the rows in the DataFrame.

New topic: Grouping data by multiple characteristics

The `reset_index()` method

```
temp = df.groupby(by = ['Type', 'Content Rating'])['Size'].agg(['min', 'max'])
print(temp.reset_index())
```

	Type	Content Rating	min	max
0	Free	Everyone	0.008301	100.0
1	Free	Everyone 10+	0.027344	100.0
2	Free	Teen	0.35430	100.0
3	Paid	Everyone	0.03672	100.0
4	Paid	Everyone 10+	1.800000	100.0
5	Paid	Teen	1.200000	99.0

New Index: Values
New topic: Grouping data by multiple characteristics

Discuss how easy it is to navigate in the table after grouping by multiple columns. Draw the students' attention to the fact that data structures with hierarchical indexes are difficult to understand. In contrast to those structures, show the students a pivot table where the same information is placed more compactly and it is easier to navigate.

Go over the syntax of the `pivot_table()` method. Emphasize to the students that each parameter can take as a value either a string constant (or a number if the column headings are numeric) or a list of values. Use the third task from the set of tasks discussed at the beginning of the lesson as an example for going over the method.

Pivot table

A pivot table is a means of generalizing data for further analysis.

In a pivot table, the unique elements of the **first characteristic** are placed in the top heading, and the elements of the **second characteristic** are placed in the side heading.

New topic: Grouping data by multiple characteristics

The parameters of the `pivot_table()` method

- **columns** – the name of the DataFrame column which we will take the column headings of the pivot table from,
- **index** – the name of the DataFrame column which we will take the string headers (indexes) of the pivot table from,
- **values** – the name of the DataFrame column which we will take the values of the pivot table cells from,
- **aggfunc** – the name of the aggregating function(s).

New topic: Grouping data by multiple characteristics

The `pivot_table()` method

```
df.pivot_table(columns = 'Type',
               index = 'Content Rating',
               values = 'Size',
               aggfunc = 'min')
```

New topic: Grouping data by multiple characteristics

VSC + Platform. Data grouping

(15 min)

Have the students work with a dataset. Let the students know that they will need to write the code in VSC and then transfer the answers they get to the platform where the tasks with auto-check are.

If you see that the children are hesitant and having difficulty getting started, do a couple of tasks together with them. Encourage the students to be active in asking questions and comment on what you are doing.

You will find the answers to the tasks and the reference code to get them at the end of the methodological guidelines.



Wrapping up the lesson. Reflection

(5 min)

Ask the students to answer the questions to check their understanding of the new lesson material. Ask them to share their impression of the entire lesson and to answer the question about what was the most surprising/interesting for them.

Go back to the data analysis stages from the previous lesson with the students. Tell the children that we missed one of the important steps again: getting the data ready to work with.

Explain that this time it was done on purpose because getting the data ready (or cleaning it) requires that the analyst have a certain skill. That is why in their first lessons, they worked with a dataset that was prepared for them by specialists from the Algorithmics school. Tell the students that they are now knowledgeable enough to master the skill of data cleaning.

 <p>MODULE 3, LESSON 2</p> <p>Wrapping up the lesson</p>	<p>Let's answer these questions</p> <ol style="list-style-type: none"> 1. Why do we need to know the number of unique values in a column? 2. How is grouping different from filtering? 3. What is a "pivot table" and what do we use it for? 4. Which Pandas method do you find most effective when studying a target audience? <p>Wrapping up the lesson</p>	<p>Next time</p> <p>It seems we've forgotten something again...</p>  <p>Wrapping up the lesson</p>
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Answers to the tasks

Task 1.1

Reference code

```
import pandas as pd
```

```
df = pd.read_csv('GoogleApps.csv')
```

#1 How many apps are there in the 'BUSINESS' 'Category'?

```
print(df['Category'].value_counts())
```

#2 What is the ratio of apps for teenagers ('Teen') to those for children over 10 years old ('Everyone 10+')?

#Round the answer to the nearest hundredth.

```
temp = df['Content Rating'].value_counts()
print('Ratio:', round(temp['Teen'] / temp['Everyone 10+'], 2))
```

#3.1 What is the average 'Rating' of 'Paid' apps?

#Round the answer to the nearest hundredth.

```
temp = df.groupby(by = 'Type')['Rating'].mean()
print(temp['Paid'])
```

#3.2 How much lower is the average 'Rating' of 'Free' apps than the average rating of 'Paid' apps?

#Round the answer to the nearest hundredth.

```
print(round(temp['Paid'] - temp['Free'], 2))
```

#4 What are the minimum and maximum app 'Size' in the 'COMICS' 'Category'?

#Round the answer to the nearest hundredth.

```
print(df.groupby(by = 'Category')['Size'].agg(['min', 'max']))
```

#Bonus 1. How many apps have a 'Rating' of over 4.5 in the 'FINANCE' 'Category'?

```
temp = df[df['Rating'] > 4.5]['Category'].value_counts()  
print(temp['FINANCE'])
```

#Bonus 2. What is the ratio of 'Free' to 'Paid' games with a 'Rating' greater than 4.9?

```
temp = df[(df['Category'] == 'GAME') & (df['Rating'] > 4.9)]['Type'].value_counts()  
print(temp['Free'] / temp['Paid'])
```


Tasks 1.2–1.6

✓ Part 1. My correct solution

Attempt: 1/200

Fill in the blanks

Use the data that you were able to get from the dataset while working in VSC.

How many applications are there in the 'BUSINESS' category?

Enter your answer as an integer.

✓ Part 1. My correct solution

Attempt: 1/200

Fill in the blanks

Use the data that you were able to get from the dataset while working in VSC.

1. What is the average paid app rating? Round your answer to the nearest hundredth.

2. How much lower is the average rating of free apps than the average rating of paid ones? Round your answer to the nearest hundredth.

✓ Part 1. My correct solution

Attempt: 1/200

Fill in the blanks

Use the data that you were able to get from the dataset while working in VSC.

What are the minimum and maximum sizes of apps in the 'COMICS' category? Round your answers to the nearest hundredth.

min:

max:

✓ Part 1. My correct solution

Attempt: 1/200

Fill in the blanks

Use the data that you were able to get from the dataset while working in VSC.

How many apps have a 'Rating' of over 4.5 in the 'FINANCE' category? **64**

2. What is the proportion of free to paid games with a rating greater than 4.9? **2.0**

Task 2.1

Reference code

```
import pandas as pd
df = pd.read_csv('GoogleApps.csv')

#1 Display the minimum, average, and maximum 'Rating' of paid and free apps ('Type') and
round to the nearest tenth.
print(round(df.groupby(by = 'Type')['Rating'].agg(['min', 'mean', 'max']), 1))

#2 Display the minimum, median, and maximum 'Price' of paid apps (Type == 'Paid') for #
different target audiences ('Content Rating')
print(df[df['Type'] == 'Paid'].groupby(by = 'Content Rating')['Price'].agg(['min', 'median',
'max']))

#3 Group the data by 'Category' and target audience ('Content Rating') however you prefer
#calculate the maximum number of 'Reviews' for each group.
#Compare the results for the 'EDUCATION', 'FAMILY', and 'GAME' categories:
#In which age group did the 'EDUCATION' category app receive the most reviews? 'FAMILY'?
'GAME'?

#Tip: You can select multiple columns from DataFrame at once using the following syntax:
# df[<column 1>, <column 2>, <column 3>]]
temp = df.pivot_table(index = 'Content Rating', columns = 'Category', values = 'Reviews',
aggfunc = 'max')
print(temp[['EDUCATION', 'FAMILY', 'GAME']])

#4 Group the paid (Type == 'Paid') apps by 'Category' and target audience ('Content Rating')
#Calculate the average number of 'Reviews' for each group
```

```
#Please note that some cells in the resulting table have the value "NaN" - Not a Number -
instead of a number
#That means that there are no apps in that group.
#Choose the names of the categories that have paid apps for all age groups and arrange them
in alphabetical order.
print(df[df['Type'] == 'Paid'].pivot_table(columns = 'Content Rating', index = 'Category',
values = 'Reviews', aggfunc = 'mean'))

#Bonus task. Find the categories of free (Type == 'Free') apps
#in which groups were the apps not designed for all age groups ('Content Rating')
print(df[df['Type'] == 'Free'].pivot_table(index = 'Category', columns = 'Content Rating',
values = 'Reviews', aggfunc = 'mean'))
```

Tasks 2.2–2.6

✓ Part 1. My correct solution

Attempt: 1/200

Fill in the blanks in the text

What are the minimum, average, and maximum 'Rating' of paid and free apps ('Type') equal to? Round your answers to the nearest tenth.

Free_min 1.0

Free_mean 4.2

Free_max 5.0

Paid_min 1.0

Paid_mean 4.2

Paid_max 5.0

✓ Part 1. My correct solution

Attempt: 2/200

Select all the TRUE statements that can be established after grouping:

Grouping by minimum, median, and maximum price of paid applications (Type == 'Paid') for different target audiences ('Content Rating').

- ☐ The median price for each target audience is different
- ☒ In the 'Teen' category, the median price is the highest among the entire target audience
- ☐ The maximum price of paid applications for all target audiences is the same
- ☒ In the 'Everyone' category, the maximum price is the highest among the entire target audience
- ☒ The minimum price of paid applications for all target audiences is the same

✓ Part 1. My correct solution

Attempt: 1/200

Fill in the blanks

Use the data that you were able to get from the dataset while working in VSC.

1. In which age group did the 'EDUCATION' category app receive the most reviews? **Everyone**

2. In which age group did the 'FAMILY' category app receive the most reviews? **Everyone 10+**

3. In which age group did the 'GAME' category app receive the most reviews? **Everyone 10+**

✓ Part 1. My correct solution

Attempt: 1/200

Which statement correctly lists the names of categories that have paid apps for all age groups.

Use the data that you were able to get from the dataset while working in VSC.

- ☐ FAMILY
GAME
WEATHER
- ☐ FAMILY
MEDICAL
- ☐ BOOKS_AND_REFERENCE
GAME
MEDICAL
PERSONALIZATION
- ☒ FAMILY
GAME
MEDICAL

✓ Part 1. My correct solution

Attempt: 1/200

Fill in the blanks in the text

Use the data that you were able to get from the dataset while working in VSC.

How many free app categories (Type == 'Free') have apps that are not designed for all age groups ('Content Rating')?

Number of categories: **13**

Filtering and tasks from the lesson that are solved using it

Task #1: How many times does the number of apps for the "all users" audience exceed the number of apps for the "10+" users?

```
Everyone = df[(df['Content Rating'] == 'Everyone')] ['Content Rating'].count()
```

```
Everyone10 = df[(df['Content Rating'] == 'Everyone 10+')] ['Content Rating'].count()
```

```
print('Proportion of apps for everyone to those for children:', Everyone/Everyone10)
```

Task #2: What is the average app size for each target audience?

```
print('Average app size for the Everyone audience:', df[df['Content Rating'] ==
'Everyone']['Size'].mean())
print('Average app size for the Everyone 10+ audience:', df[df['Content Rating'] == 'Everyone
10+']['Size'].mean())
print('Average app size for the Teen audience:', df[df['Content Rating'] ==
'Teen']['Size'].mean())
```

Task #3: What are the minimum and maximum size of the paid and free apps for each target audience? # Legend: a) target audience E10 - Everyone 10+; E - Everyone; T -Teen b) app type F - free; P - paid.

```
E10_min_F = df[(df['Content Rating'] == 'Everyone 10+') & (df['Type'] == 'Free')]
['Size'].min()
E_min_F = df[(df['Content Rating'] == 'Everyone') & (df['Type'] == 'Free')] ['Size'].min()
T_min_F = df[(df['Content Rating'] == 'Teen') & (df['Type'] == 'Free')] ['Size'].min()
E10_min_F = df[(df['Content Rating'] == 'Everyone 10+') & (df['Type'] == 'Free')]
['Size'].min()
E_min_F = df[(df['Content Rating'] == 'Everyone') & (df['Type'] == 'Free')] ['Size'].min()
T_min_F = df[(df['Content Rating'] == 'Teen') & (df['Type'] == 'Free')] ['Size'].min()
E10_max_F = df[(df['Content Rating'] == 'Everyone 10+') & (df['Type'] == 'Free')]
['Size'].max()
E_max_F = df[(df['Content Rating'] == 'Everyone') & (df['Type'] == 'Free')] ['Size'].max()
T_max_F = df[(df['Content Rating'] == 'Teen') & (df['Type'] == 'Free')] ['Size'].max()
E10_min_P = df[(df['Content Rating'] == 'Everyone 10+') & (df['Type'] == 'Paid')]
['Size'].min()
E_min_P = df[(df['Content Rating'] == 'Everyone') & (df['Type'] == 'Paid')] ['Size'].min()
T_min_P = df[(df['Content Rating'] == 'Teen') & (df['Type'] == 'Paid')] ['Size'].min()
E10_max_P = df[(df['Content Rating'] == 'Everyone 10+') & (df['Type'] == 'Paid')]
['Size'].max()
E_max_P = df[(df['Content Rating'] == 'Everyone') & (df['Type'] == 'Paid')] ['Size'].max()
T_max_P = df[(df['Content Rating'] == 'Teen') & (df['Type'] == 'Paid')] ['Size'].max()
print('Minimum size of free apps:', 'E10 =', E10_min_F, ';', 'E =', E_min_F, ';', 'T =',
T_min_F)
print('Maximum size of free apps:', 'E10 =', E10_max_F, ';', 'E =', E_max_F, ';', 'T =',
T_max_F)
print('Minimum size of paid apps:', 'E10 =', E10_min_P, ';', 'E =', E_min_P, ';', 'T =',
T_min_P)
print('Maximum size of paid apps:', 'E10 =', E10_max_P, ';', 'E =', E_max_P, ';', 'T =',
T_max_P)
```