Graph Traversal Worksheet

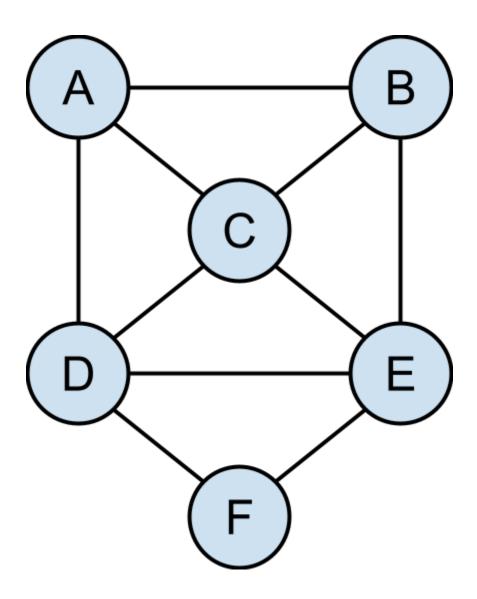
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Overview

- 1. For each problem, you are given a specific graph representation (either an image, an adjacency matrix, or an adjacency list).
- 2. Perform both **Breadth-First Search (BFS)** and **Depth-First Search (DFS)** starting from the specified node.
- 3. **At each step**, write down the current state of the algorithm (including the state of all variables used in the algorithm: queue, visited nodes, stack, etc.).
- 4. For BFS, show the state of the queue and visited nodes.
- 5. For DFS, show the state of the stack and visited nodes.

Example 1 (Graph Image)

Examine the following graph



Start Node: A

Breadth-First Search (BFS)

Perform BFS starting from node A. Show the state of the queue and visited nodes at <u>each step</u>.

- 1. Initialize the BFS with an empty queue and an empty visited set.
- 2. Queue the start node (A).
- 3. Continue the search until the queue is empty.

Depth-First Search (DFS)

Perform DFS starting from node A. Show the state of the stack and visited nodes at <u>each step</u>.

- 1. Initialize the DFS with an empty stack and an empty visited set.
- 2. Push the start node (A) onto the stack.
- 3. Continue the search until the stack is empty.

Example 2 (Adjacency Matrix)

Consider the following adjacency matrix. **Do not draw the graph!** The purpose of this exercise is to practice conducting a graph traversal when you have access to the same information in the same format the the computer has it:

	Α	В	С	D	Е
Α	0	1	1	0	0
В	1	0	1	0	0
С	1	1	0	1	1
D	0	0	1	0	1
Е	0	0	1	1	0

Start Node: C

Breadth-First Search (BFS)

Perform BFS starting from node C. Show the state of the queue and visited nodes at <u>each step</u>.

- 1. Initialize the BFS with an empty queue and an empty visited set.
- 2. Queue the start node (C).
- 3. Continue the search until the queue is empty.

Depth-First Search (DFS)

Perform DFS starting from node C. Show the state of the stack and visited nodes at <u>each step</u>.

- 1. Initialize the DFS with an empty stack and an empty visited set.
- 2. Push the start node (C) onto the stack.
- 3. Continue the search until the stack is empty.

Example 3 (Adjacency List)

Consider the following adjacency list. **Do not draw the graph!** The purpose of this exercise is to practice conducting a graph traversal when you have access to the same information in the same format the the computer has it:

- **A** → B, D
- **B** → A, C
- **C** → B, D, E
- **D** → A, C, E, F
- $\bullet \quad E \to C, \, D$
- $\bullet \quad \textbf{F} \to \textbf{D}$

Start Node: B

Breadth-First Search (BFS)

Perform BFS starting from node B. Show the state of the queue and visited nodes at <u>each step</u>.

- 1. Initialize the BFS with an empty queue and an empty visited set.
- 2. Queue the start node (B).
- 3. Continue the search until the queue is empty.

Depth-First Search (DFS)

Perform DFS starting from node B. Show the state of the stack and visited nodes at <u>each step</u>.

- 1. Initialize the DFS with an empty stack and an empty visited set.
- 2. Push the start node (B) onto the stack.
- 3. Continue the search until the stack is empty.