

Kinematics

2 Dimensional Motion

Projectile Virtual Lab

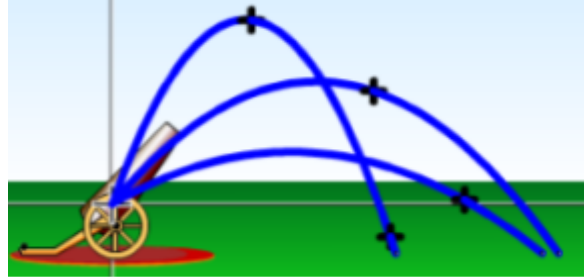
Name _____

Period _____

Purpose – To investigate projectiles fired at angles.

An object is fired at a speed of 14 m/s at three different angles.

- **Label** the trajectories in the chart below on the diagram to the right as v_1 , v_2 or v_3 .
- **Resolve** each of the velocity vectors into horizontal and vertical components. (use trig)
- **Rank** the time of flight for each velocity on the diagram on the right (1 max time, 2, 3)



Velocity	Horizontal Component	Vertical Component	Time of Flight
$v_1 = 14 \text{ m/s at } 30^\circ$			
$v_2 = 14 \text{ m/s at } 50^\circ$			
$v_3 = 14 \text{ m/s at } 70^\circ$			

Launch the Projectile Motion simulation. <http://phet.colorado.edu/en/simulation/projectile-motion>

Choose the INTRO tab from the 1st screen

Adjust the cannon height by clicking on the + symbol on the cannon and dragging down until the height is 0 m.

Adjust the speed with the slider to 14 m/s then fire three projectiles at 30° , 50° and 70° (adjust angle by clicking on the cannon and dragging it to the correct angle). Keep all other initial conditions as given.

Circle either constant, changing or zero, draw an arrow in the direction of the velocity (if not zero) and give the value of the acceleration of the projectile while in the air. Ignore air resistance.

While the projectile is ascending its:

- horizontal velocity is constant/changing/zero and points _____ and the acceleration is _____
- vertical velocity is constant/changing/zero and points _____ and the acceleration is _____

When the projectile is at the apex its:

- horizontal velocity is constant/changing/zero and points _____ and the acceleration is _____
- vertical velocity is constant/changing/zero and points _____ and the acceleration is _____

While the projectile is descending its:

- horizontal velocity is constant/changing/zero and points _____ and the acceleration is _____
- vertical velocity is constant/changing/zero and points _____ and the acceleration is _____

Equation	Horizontal Motion	Vertical Motion
$v = \frac{\Delta d}{\Delta t}$		
$a = \frac{v_f - v_i}{\Delta t}$		
$\Delta d = v_i \Delta t + \frac{1}{2} a \Delta t^2$		
$a = \frac{v_f^2 - v_i^2}{2 \Delta d}$		

In the chart above, check the box for the equations if they can be used in either horizontal or vertical motion.

Which type of motion describes the horizontal equation(s) _____

Which type of motion describes the vertical equation(s) _____

What variable ties the horizontal and vertical equations of motion together? _____

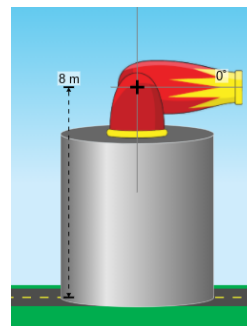
Rewrite the equations below adding the subscripts “x” and “y” to the appropriate variables. Where appropriate replace the acceleration “a” with “g”.

		Projectile Motion Equation	
Equation		Horizontal (X)	Vertical (Y)
$v = \frac{\Delta d}{\Delta t}$	becomes		
$a = \frac{v_f - v_i}{\Delta t}$	becomes		
$\Delta d = v_i \Delta t + \frac{1}{2} a \Delta t^2$	becomes		
$a = \frac{v_f^2 - v_i^2}{2 \Delta d}$	becomes		

Launching a Projectile with a non-zero Starting Height and Horizontal

Make the angle of the cannon 0 degrees. Horizontal Projectile

Adjust the height to a few different heights and at each height try different speeds and observe the actions of a projectile that is not launched at ground level.



How does adding initial height with constant speed affect **flight time**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

How does adding initial height with constant speed affect **maximum range**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

How does adding initial speed with constant height affect **flight time**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

How does adding initial speed with constant height affect **maximum range**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____



Consider this scenario and ignore air resistance. A pirate fires his cannon parallel to the water but 3.5 m above the water. The cannonball leaves the cannon with a velocity of 120 m/s. He misses his target and the cannon ball splashes into the briny deep. How far did the cannonball travel? (*please show work*)

x y

d

v_0

a

t = _____

Launching a Projectile with a zero Starting Height and Angled velocity

Make the height of the cannon 0 meters.

Adjust the angle to a few different degrees and at each angle try different speeds and observe the actions of a projectile that is launched at ground level.

How does adding initial angle with constant speed affect **flight time**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

How does adding initial angle with constant speed affect **maximum range**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

How does adding initial angle with constant speed affect **maximum height**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

How does adding initial speed with constant angle affect **flight time**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

How does adding initial speed with constant angle affect **maximum range**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

How does adding initial speed with constant angle affect **maximum height**? _____

Why do you suppose this is? _____

What formula can we use that supports your explanation? _____

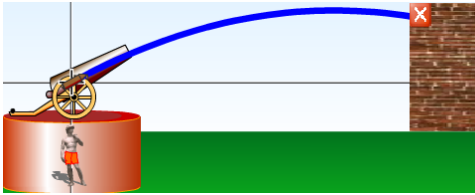
Symmetrical Trajectory (starting and ending height are the same)

A rival pirate fires his volley back at the same 3.5 m above the sea, but at an angle of 30° . Coincidentally, this scurvy dog's cannon also fires at 120 m/s. This cannonball strikes the other boat at 3.5 m above the sea (so the vertical displacement is zero). How far did this cannonball travel? *(please show work and use the xy chart)*



x y
d
 v_0
a
t = _____

The Interrupted Projectile (that hits something on the way)



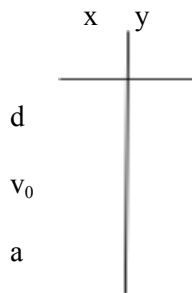
Many projectiles don't complete their entire travel to the ground. We may need to calculate the range of a projectile that lands on a hill above ground or the height when the projectile stuck its mark.

How would the flight time of a projectile that lands ABOVE the height it was launched compare to the flight time of a ground-to-ground projectile _____

Why is this? _____

What formula can we use that supports your explanation? _____

OK, one last pirate scenario. A pirate 50.0 m away from a tall ship wants to shoot the crow's nest off this ship. She angles her cannon at 25° and fires; her cannonball leaving at only 68 m/s. Somehow, the lass pegs the crow's nest. How high was the crow's nest? (*please show work*)



$t =$ _____