

ERRATA CORRIGE

“Pearls of Algorithm Engineering”

Paolo Ferragina, Cambridge University Press, 2023

<https://www.cambridge.org/core/books/pearls-of-algorithm-engineering/95061352D7263CCCBD4F243018236EB2>

CHAPTER 3

- Page 31, reference [3]: the term “Complexity” should be lowercase

CHAPTER 6

- Page 78, the definition of Δ_j should be just 2^{k-1} that is surely at most n .

CHAPTER 7

- Page 84, line +5 of section 7.2.1: Change “Since buckets 1 and 6” to “Since buckets 1 and 7”
- Page 85, last line: substitute 666 with 766.

CHAPTER 8

- Page 103, proof of Theorem 8.3: $Q(k)$ is the probability that **at least** k keys are hashed to a specific slot (as actually this is the use made of $Q(k)$ in the rest of the proof). Moreover, few lines below it is introduced a random variable X_j that is never used in the rest of the proof, but it was intended as $Q(k) = P(X_j \geq k)$, for a given slot j .
- Page 105, line -6: the inverse modulo m of $(x_0 - y_0)$ is in $[1, m-1]$
- Page 106, line +11: the condition on a can be expressed better as >0 , as then indicated in the definition of $H_{p,m}$ in the line below.

CHAPTER 9

- Page 143, line +7 from paragraph starting with “A running example...”. The occurrence of s_8 should be s_7 .
- Proof of Theorem 9.5, line +2, the phrase “no more than b/g ” should be “no more than $\lceil b/g \rceil$ ”.
- Proof of Theorem 9.5, pag. 138, when upper bounding $|B_i|$, change “we can write” into “we can write (by assuming that g divides b , for the sake of presentation):”

CHAPTER 11

- Page 203, just line -5 before the beginning of Section 11.5: In the phrase starting with “In particular, if this distribution is concentrated...”, the two occurrences of *s* should be substituted with *c*.
- Page 204 in Section 11.5 (middle of the page): it is written that “[..] we have *m-l* distinct elements of *S'* and the smallest one is larger than low [..]”. To be clearer, it should be written “larger or equal than” as reported in the following formula.
- Page 206 in Section 11.6 (middle of the page): it is written that “Elias-Fano code works on monotonically increasing sequences”. It should be written “monotonically nondecreasing sequences” and thus manage sets with repeated items. However, I mention that in the context of inverted lists for search engines, the case is the one of monotonically increasing sequences.
- Page 206 in Section 11.6 (bottom of the page): There is a counting on the number of 0s in the binary sequence *H*, which states that they are bounded by *n*. So the next phrase about the bit length of *H* should state that it is “bounded by” $2n$, and not that it is exactly $2n$. So the number of 0s is at most the number of 1s.

Actually, to make this argument hold for every value of *maxS* and *n*, we should represent only the configurations up to *maxS* (included), and encode the length of *H* into an integer, which is stored anyway by the system to correctly access *H*. In fact, if $n=15$ and $\text{maxS} = 19$, we then have $\ell = \lceil \log_2 (u/n) \rceil = \lceil \log_2 1, \dots \rceil = 1$, and $h = 4$. Thus the overall number of configurations over *h* bits is $2^h = 16$ ($= n+1$ and thus larger than *n*).

But if we limit ourselves to represent only the configurations up to *maxS*, the maximum bucket value is actually $\lfloor \text{maxS}/2^\ell \rfloor$, and thus the number of buckets is $\lfloor \text{maxS}/2^\ell \rfloor + 1$ because we have to include the configuration 0^h . This formula then expresses the maximum number of 0s in *H*, and it is bounded above by *n* as follows:

$$\begin{aligned} \lfloor \text{maxS}/2^\ell \rfloor + 1 &\leq \lfloor (u-1)/2^\ell \rfloor + 1 \\ &\leq \lfloor (u-1)/2^{\lceil \log_2 (u/n) \rceil} \rfloor + 1 \\ &\leq \lfloor (u-1)/2^{\log_2 (u/n)} \rfloor + 1 \\ &\leq \lfloor (u-1)/(u/n) \rfloor + 1 = \lfloor n - (1/(u/n)) \rfloor + 1 = (n-1) + 1 = n \end{aligned}$$

Recalling the previous example with $n=15$ and $\text{maxS} = 19 = (10011)_2$, we then have that the largest configuration is the *H*-part of *maxS*, hence $9 = (1001)_2$. Thus the number of 0s is $9+1 = 10 < 15 = n$; and, in fact, the formula above returns:

$$\lfloor \text{maxS}/2^\ell \rfloor + 1 = \lfloor 19/2 \rfloor + 1 = 10.$$

As another example (which gets exactly *n* configurations of 0s), take the one in Figure 11.8. So $n=8$, $\text{maxS} = 31 = (11111)_2$, and thus $u = 31+1 = 32$, $\ell = 2$, and $h=3$. Thus the largest high part is $(111)_2$ which means $8 = 2^3$ buckets $= n$; and in fact the formula above returns:

$$\lfloor \text{maxS}/2^\ell \rfloor + 1 = \lfloor 31/4 \rfloor + 1 = 8.$$

CHAPTER 15

- Page 278, line -1, and Page 279 line +1: both occurrences of $B[26]$ should be $B[17]$.
- Page 281, line +5 in step 6, the modulo function should be on k (i.e., number of 1s in a small block) and not on k^2 .
- Page 288, line +5: $\text{Rank1}(13)$ should be 8 instead of 6.