

Mental Math Strategies

<http://www.plpsd.mb.ca/division/Rubrics/Mental%20Math%20Strategies.pdf>

Thinking Strategies for Addition

- Counting On: Students start with a number and count on 1, 2, 3. For example, if the question is $5 + 2$, students count 5, 6, 7. Note: This strategy is only useful for adding 1, 2, or 3.
- Using Doubles: The first fact combinations students often learn are doubles.
- Making Ten: Students make combinations that equal 10. Then they extend to make combinations that are multiples of 10. Examples: $6 + 4 = 10$ extends to $76 + 4 = 80$. This can then be extended to $10 + 4 = 14$ or $50 + 8 = 58$.

Thinking Strategies for Subtraction

- Counting Back: Students start with a number and count backwards. If the question is $5 - 2$, students count 5, 4, 3. Note: This strategy is only useful for subtracting 1, 2, or 3.
- Counting Up: Students start with a number being subtracted and count up to the number from which it is being subtracted. For example, for the question $9 - 7$, students can count 8, 9.
- Using Part, Part, Whole: Given: $\text{Part} + \text{Part} = \text{Whole}$, Therefore: $\text{Whole} - \text{Part} = \text{Part}$
- Make Ten and Then Some: Given a subtraction question such as $14 - 8 = ?$, students start with the part (8), add-on to make 10 (i.e., $8 + 2$), then add-on from 10 to make 14 ($10 + 4$). Then the students add the numbers they added-on to make 14 ($4 + 2 = 6$).
- Using Doubles: For the question $13 - 6 = ?$, students think addition using doubles. For example, $6 + 6 = 12$, then add-on 1 to make 13, so $6 + 1 = 7$

Thinking in Patterns

- Skip Counting:** Starting at any number, students skip count by 10s, 2s, 3s, 5s. For example, ask students to skip count by 10s starting at 46.
- 100 Chart:** Make sure a 100 chart is visible in your classroom and that students have access to desk-size charts. Refer to the chart and practise counting skills on the chart regularly.
- Arrow Moves:** Indicate moves on the 100 chart by using arrows. For example, $23 + 11 = ?$, would be indicated with one space across from 23 to 24 and then from 24 ten spaces down to 34. Note the pattern for all additions of +11 on the chart. Extend to the addition or subtraction of other numbers.
- Chaining Operations:** Example: $8 + 2 + 4 + 6 - 3 = ?$ (Note: choose combinations that end in multiples of 10 to encourage students' visualization of the 10 frame.)

Strategies for Adding and Subtracting Large Numbers:

- Multiples of Ten:** For addition: $30 + 50 =$, $56 + 10 =$, $56 + 30 =$
- For subtraction: $50 - 30 =$, $56 - 10 =$, $56 - 30 =$
- Expanding the Second Addend or Subtrahend:**
For addition: $28 + 17 =$, $28 + 10 + 7 =$
For subtraction: $28 - 17 =$, $28 - 10 - 7 =$
- Front-end Adding: Example:** $65 + 26 = ?$ Ask students to think $60 + 20 = 80$ and $5 + 6 = 11$, so $80 + 11 = 91$.
- Compensation for 8 and 9:** Examples: $67 - 19 = 67 - 20 + 1$
 $43 + 29 = 43 + 30 - 1$
 $67 - 18 = 67 - 20 + 2$
 $43 + 28 = 43 + 30 - 2$

Compatible Numbers: Students bring together numbers that add up to 10 or multiples of 10.

Example: $8 + 5 + 12 + 7 + 5 + 3 + 4 = ?$

Think: $8 + 12 = 20$, $5 + 5 = 10$, $7 + 3 = 10$

Therefore: $20 + 10 + 10 + 4 = 44$

Multiples of 25: Students count by 25s and relate to money.

Common Zeros: For addition and subtraction operations, students remove the 0s, complete the operation, and then tack the 0 back on.

Example: $120 - 70 = ?$

Think: $12 - 7 = 5$

Add the common zero, so the answer is 50.

Strategies for Multiplying

Trailing Zeros: For multiplication, students remove the trailing 0s, multiply, and tack on all the removed zeros.

Examples: a. $5 \times 60 = ?$

Think: $5 \times 6 = 30$

Tack on the removed 0, so the answer is 300

b. $20 \times 30 = ?$

Think: $2 \times 3 = 6$

Then tack on all the removed 0s, so the answer is 600

Working with Known Facts: Work with multiplication facts that are more simple to use, then add or subtract the remaining group

Example: $15 \times 6 = ?$

Think: $15 \times 5 = 75 + 15 = 90$

Expanding the Numbers: Work according to place value for multiplication, then add up the products

Example: $25 \times 14 = ?$

Think: $20 \times 10 = 200$, $20 \times 4 = 80$, $5 \times 10 = 50$,
and $5 \times 4 = 20$

Then Add: $200 + 80 + 50 + 20 = 350$

