Summary of Trigonometric Functions

Function	Properties	Graph
Sine $f(x) = \sin x$	Domain: All Real numbers Range: $[-1, 1]$ x-Intercepts: $x = \pi n$, where n is an integer y-Intercept: $y = 0$ Asymptotes: None Symmetry: Symmetric about the origin, making it an odd function Periodic: Increases and decreases with oscillating behavior in periods of 2π Absolute maximum: 1 Absolute minimum: -1	$f(x) = \sin x$
Cosine $f(x) = \cos x$	Domain: All Real numbers Range: $[-1, 1]$ $x = \frac{\pi}{2} + \pi n,$ x-Intercepts: $y = 1$ Asymptotes: None Symmetry: Symmetric about the y-axis, making it an even function Periodic: Increases and decreases with oscillating behavior in periods of 2π Absolute maximum: 1 Absolute minimum: -1	$f(x) = \cos x$ $-2\pi - 3\pi \left[2 - \pi - 3\pi \right] = -\pi$
Tangent f(x) = tan x	Domain: All Real numbers such $x \neq \frac{\pi}{2} \pm \pi n,$ that such that n is an integer Range: $(-\infty, \infty)$ x-Intercepts: $x = \pi n$, such that n is an integer	$f(x) = tanx$ $\frac{1}{\sqrt{\pi}} \frac{1}{\sqrt{2\pi}} = tanx$ $\frac{1}{\sqrt{\pi}} \frac{1}{\sqrt{\pi}} = tanx$ $\frac{1}{\sqrt{\pi}} \frac{1}{\sqrt{\pi}} = tanx$ $\frac{1}{\sqrt{\pi}} \frac{1}{\sqrt{\pi}} = tanx$ $\frac{1}{\sqrt{\pi}} \frac{1}{\sqrt{\pi}} = tanx$

Cotangent Function $f(x) = \cot x$	y-Intercept: $y = 0$ Asymptotes: Vertical asymptotes $x = \frac{\pi}{2} \pm \pi n$, at such that n is an integer Symmetry: Symmetric about the origin, making it an odd function Period: π Extrema: None Increasing/Decreasing: Increasing on entire domain Domain: All Real numbers such that $x \neq \pi n$, x -Intercepts: $x = \frac{\pi}{2} + \pi n$, such that $x \neq $	$f(s) = \cot s$ $\frac{1}{2}$ $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$
Secant Function $f(x) = \sec x$	Domain: All Real numbers such $x \neq \frac{\pi}{2} \pm \pi n,$ that such that n is an integer Range: $(-\infty, -1] \cup [1, \infty)$ x-Intercept: None y-Intercept: $y = 1$	$f(x) = secx$ $\begin{array}{cccccccccccccccccccccccccccccccccccc$

	Asymptotes: Vertical asymptotes $x = \frac{\pi}{2} \pm \pi n,$ at such that n is an integer Symmetry: Symmetric about the y-axis, making it an even function Period: 2π	
Cosecant Function $f(x) = \csc x$	Domain: All Real numbers such that $X \neq \pi n$, such that n is an integer Range: $(-\infty, -1] \cup [1, \infty)$ x-Intercept: None y-Intercept: None Asymptotes: Vertical asymptotes at $X = \pi n$, such that n is an integer Symmetry: Symmetric about the origin, making it an odd function Period: 2π	$f(x) = cacx$ $\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} = $

Transformation of Sine and Cosine Functions

Use the standard form of the equation $y = a\sin(bx - c) + d$ or $y = a\cos(bx - c) + d$.

amplitude =
$$\frac{|a|}{|b|}$$
 period = $\frac{2\pi}{|b|}$

phase shift =
$$\frac{c}{b}$$

Transformation of Tangent Function

Use the standard form of the equation $y = a \tan(bx - c) + d$.

vertical stretch/shrink = a

period =
$$\frac{\pi}{|b|}$$

vertical shift = d	phase shift = $\frac{c}{b}$
	vertical shift = d