Divisibility

Common Factors and Greatest Common Factors

Before you can reduce a fraction, you need to learn two new terms. The two new terms are: Common Factors (CF) and Greatest Common Factor (GCF).

What is a Common Factor (CF)?

A common factor is a group of two or more whole numbers that have factors in common with one another.

Example 1: the numbers 18 and 30 have 4 common factors. Circle the common factors below.

The factors of 18 are	The factors of 30 are	
18 1 18 2 9 3 6 (1, 2, 3, 6, 9, 18)	30 1 30 2 15 3 10 5 6 (1, 2, 3, 5, 6, 10, 15, 30)	

Now, you try! Determine the common factors for 28 and 32 by drawing a Factor T or a Factor Rainbow. Then, circle the common factors.

The factors of 28 are	The factors of 32 are		

What is the Greatest Common Factor (GCF)?

The greatest common factor (GCF) is the greatest common factor of two or more whole numbers.

For instance, in the examples above, we determined the common factors. Therefore, we should be able to determine the GCF of each pair of numbers.

What is the GCF of 18 and 30?	
What is the GCF of 28 and 32?	

Example 2: What is the greatest common factor for 12 and 24?

First, list the factors of 12 and 24 by drawing a Factor T or a Factor Rainbow. Circle the common factors and highlight the GCF.

The factors of 12 are	The factors of 24 are			
Common factors:				
Greatest common factor:				
Show You Know!				
List the common factors and find the greatest common factor for 36 and 48. Show all work in the box below.				
Common factors:				
GCF:				

Next, we will be using our knowledge of the greatest common factor to **reduce fractions to lowest terms!**

Reducing Fractions to Lowest Terms Common Factors and Greatest Common Factor

How do we reduce fractions to lowest terms? Step 1: List all factors of both numbers Step 2: Circle the GCF Step 3: Divide the numerator and denominator by the GCF. Example 1: Reduce $\frac{6}{18}$ to lowest terms: Step 1: List all factors of both numbers: 18: Step 2: Circle the GCF Step 3: Divide the numerator and denominator by the GCF.

Example 2: Reduce $\frac{28}{36}$ to lowest terms

Reducing Fractions to Lowest Terms Common Factors and Greatest Common Factors

Fraction	Factors Circle GCF	GCF	Reduced Fraction
<u>4</u>	4:		4 ÷
6	6:		6 ÷
<u>10</u>	10:		<u>10</u> ÷
12	12:		12 ÷
<u>16</u>	16:		16 ÷
24	24:		24 ÷
<u>8</u>	8:		<u>8</u> ÷
16	16:		16 ÷
<u>18</u>	18:		18 ÷
20	20:		20 ÷

Fraction (Divide by GCF)	Reduced Fraction	Fraction (Divide by GCF)	Reduced Fraction
<u>18</u> ÷ 21÷		<u>8</u> ÷ 10÷	
<u>25</u> ÷ 50÷		<u>6</u> ÷ 15÷	
<u>6</u> ÷ 8÷		<u>4</u> ÷ 20÷	
48÷ 60÷		<u>9</u> ÷ 24÷	
<u>15</u> ÷ 25÷		<u>2</u> ÷ 10÷	

Reminder: If you don't find the greatest common factor you will have to divide more than once.

Example: Reduce to lowest terms:

Reduce the following fractions to lowest terms. Find the GCF first if it is helpful. Show your work.

1)
$$\frac{12}{15}$$
 = ____

11)
$$\frac{42}{60}$$
 =

2)
$$\frac{3}{30} =$$

12)
$$\frac{8}{16} =$$

3)
$$\frac{64}{80} =$$

13)
$$\frac{7}{21} =$$

4)
$$\frac{2}{4}$$
 = ____

14)
$$\frac{50}{100} = _____$$

5)
$$\frac{30}{100} = ____$$

15)
$$\frac{27}{30} =$$

6)
$$\frac{6}{24} =$$

16)
$$\frac{9}{15} =$$

7)
$$\frac{8}{32}$$
 =

17)
$$\frac{3}{6} =$$

8)
$$\frac{27}{90} =$$

18)
$$\frac{12}{24} =$$

9)
$$\frac{3}{6} =$$

19)
$$\frac{16}{32} =$$

10)
$$\frac{20}{100} = ____$$

20)
$$\frac{2}{4} =$$
