

## 1. Trigonometry 2

1. Solve the equation: (2 mks)

$$\sin \frac{5}{2}X = -\frac{1}{2} \text{ for } 0^\circ \leq X \leq 180^\circ$$

2. (a) Complete the table below, leaving all your values correct to 2 d.p. for the functions  $y = \cos x$  and  $y = 2\cos(x + 30)^\circ$  (2 mks)

$X^\circ$	$0^\circ$	$60^\circ$	$120^\circ$	$180^\circ$	$240^\circ$	$300^\circ$	$360^\circ$	$420^\circ$	$480^\circ$	$540^\circ$
$\cos X$	1.00			-1.00		0.50				
$2\cos(x+30)$	1.73		-1.73		0.00					

- (b) For the function  $y = 2\cos(x+30)^\circ$

State:

(i) The period (1 mk)

(ii) Phase angle (1 mk)

- (c) On the same axes draw the waves of the functions  $y = \cos x$  and  $y = 2\cos(x+30)^\circ$  for  $0^\circ \leq x \leq 540^\circ$ . Use the scale 1cm rep  $30^\circ$  horizontally and 2 cm rep 1 unit vertically (4 mks)

- (d) Use your graph above to solve the inequality  $2\cos(x + 30^\circ) \leq \cos x$  (2 mks)

3. Find the value of  $x$  in the equation.  
 $\cos(3x - 180^\circ) = \frac{\sqrt{3}}{2}$  in the range  $0^\circ \leq x \leq 180^\circ$  (3 marks)

4. Given that  $\tan \theta = \frac{11}{60}$  and  $\theta$  is an acute angle, find without using tables  $\cos(90 - \theta)$  (2mks)

5. Solve for  $\theta$  if  $-\frac{1}{4} \sin(2x + 30) = 0.1607$ ,  $0 \leq \theta \leq 360^\circ$  (3mks)

6. Given that  $\cos \theta = \frac{5}{13}$  and that  $270^\circ \leq \theta \leq 360^\circ$ , work out the value of  $\tan \theta + \sin \theta$  without using a calculator or mathematical tables. (3 marks)

7. Solve for  $x$  in the range  $0^\circ \leq x \leq 180^\circ$  (4mks)

$$-8 \sin^2 x - 2 \cos x = -5.$$

8. If  $\tan x^\circ = \frac{12}{5}$  and  $x$  is a reflex angle, find the value of  $5\sin x + \cos x$  without using a calculator or mathematical tables

9. Find  $\theta$  given that  $2 \cos 3\theta - 1 = 0$  for  $0^\circ \leq \theta \leq 360^\circ$

10. Without a mathematical table or a calculator, simplify:  $\cos 300^\circ \times \sin 120^\circ$  giving your answer in  $\cos 330^\circ - \sin 405^\circ$  rationalized surd form.

11. Express in surds form and rationalize the denominator.

$$\frac{1}{\frac{1}{\sqrt{3}}}$$

$$\sin 60^\circ \sin 45^\circ - \sin 45^\circ$$

12. Simplify the following without using tables;

$$\tan 45^\circ + \cos 45^\circ \sin 60^\circ$$

13. Simplify the following surds in the form of  $a + \sqrt{b} c$  where **a**, **b**, and **c** are constants

$$\frac{5}{2\sqrt{2}-\sqrt{5}} + \frac{2}{2-\sqrt{5}}$$

14. John cycles from shopping centre **A** on a bearing of  $120^\circ$  for 5 km to shopping centre **B**. He then cycles on a bearing of  $200^\circ$  for 7 km to the shopping centre **C**. Calculate to 1 decimal place.
- The direct distance from A to C.
  - The bearing of A from C.
  - Bearing of B from C.