Known errata/items to fix in Exploring Modeling with Data and Differential Equations Using R by Zobitz

| Textbook page [Github issue] | Description |
|---|--|
| Page 82 [<u>#2</u>] | Code chunk should read: # Define the windows where we make the plots t_window <- c(0, 3) x_window <- c(0, 5) # Define the differential equation system_eq <- c(dt ~ 1, dx ~ -0.7 * x * (3 - x) / (1 + x)) phaseplane(system_eq, x_var = "t", y_var = "x", x_window = t_window, y_window = x_window) |
| Page 60 [<u>#3</u>] | Differential equation in Exercise 4.2 should read: $dp/dt = 0.023p^*(1-p)$ |
| Page 92 [<u>#4</u>] | Equation 7.8 should be dl/dt + .023I = 312.8 |
| Page 146 [<u>#5</u>] | Revise part a: " has a minimum value at $b = 1.865$ " |
| Page 156 [#7] Date closed: 10/23/23 | Revise question to ask for the mean, not the median: "Display the bootstrap histogram of 1000 bootstrap samples for the standard deviation of the snowfall dataset. From this bootstrap distribution (for the standard deviation) what is the median and 95% confidence interval?" |
| Page 36 [<u>#8</u>] | I think that in the last paragraph of section 3.1, page 36 (just above section 3.2), the current sentence "For Equation (3.1), this means that we are solving dE/dt =" should read instead: "For Equation (3.1), this means that we are solving dN/dt =" |
| Page 70 [<u>#9</u>] Date closed: 12/19/23 | Revise last sentence of page 70: "Next we apply local linearization to construct a locally linear approximation L(y) for f(y) at y=*y:" |

| Page 311 [#11] Date closed: 12/19/23 | D_log is not defined - here is some revised code: |
|--|---|
| | # Many solutions n_sims <- 100 # The number of simulations |
| | # Identify the standard deviation of the stochastic noise D_logistic <- 1 |
| | <pre># Compute solutions logistic_run_r <- rerun(n_sims) %>% set_names(paste0("sim", 1:n_sims)) %>% map(~ euler_stochastic(deterministic_rate = deterministic_logistic_r,</pre> |
| | # Plot these all together ggplot(data = logistic_run_r) + geom_line(aes(x=t, y=x, color = simulation)) + ggtitle("Spaghetti plot for the logistic SDE") + guides(color="none") |
| Page 330 [#12] Date closed: 12/19/23 | Section 26.1.2, the SDE is $dX = 2 dt + dW(t)$ (not $dX = 0.2 dt + dW(t)$) |
| Page 67 [#13] Date closed: 8/12/25 | Adjust the wording on the definition of equilibrium solution to avoid any confusion in reading (perhaps expound more). |
| | Revisions in 2025 quarto edition: |
| | The **stability** of an equilibrium solution describes the long-term behavior of the family of solutions to a differential equation. Some solutions may converge to the equilibrium in the long run, while others may not. More formally stated: |
| | > The constant function \$y=y_{*}\$ is considered an asymptotically *stable* solution to a differential equation \$\displaystyle \\frac{dy}{dt} = f(y)\$ if there exists a solution \$y_{S}(t)\$, such that \$\displaystyle \\lim_{t \rightarrow \infty} y_{S}(t) = y_{*}\$. |
| | In other words, as time increases, the the family of solutions to the differential equation is approximated by the constant function \$y=y_{*}\$. You may note that the definition of stability relies on determining the solution \$y_{S}(t)\$. However we can circumvent determining this solution by using ideas from calculus and the rate of change: |
| Page XXX [#25] Date closed: 7/11/25 | Equation 4.8 should read: dl/dt = kSI - beta*I |

Exercise 19.5, page 248 [#10] Date closed: 8/12/25

This equation has an eq. soln at (0,0), but y' is mathematically not defined there. Revise this question.

Revised in the 2025 update to:

- a. There are three equilibrium solutions for this differential equation. What are they? *Hint:* first determine where y'=0 and then substitute your solutions into x'=0.
- b. For what values of x and y is the function $g(x,y)=0.5y \cdot (1-yx)$ not defined? How might that affect interpretation of the trivial ((x,y)=(0,0)) equilibrium solution?
- c. Visualize the phase plane for this system of differential equations.
- d. Compute the Jacobian matrix for all of the non-trivial equilibrium solutions (i.e. not (x,y)=(0,0)).
- e. Use the trace-determinant relationships to evaluate the stability of the non-trivial equilibrium solutions. Is the trace-determinant analysis consistent with your phase plane?

Better scaffolding Exercise 10.4 [#6] Date closed: 8/12/25

10.4 - ask for more specificity in how to do this and each part - students mashed this problem up!

Revised in the 2025 update to:

- Researchers believe that . One way to do this is to include an a. Researchers believe that \$\theta \approx 7\$. One way to do this is to include an additional term of \$(\theta-7)^{2}\$ in the cost function. Re-write your formula from [@exr-phos-09]b \$S(1.737,\theta)\$ to account for this additional (prior) information. Call this revised function \$S_{b}(1.737,\theta)\$
- 2. b. Make a graph of \$S_{b}(1.737,\theta)\$ and determine where the global optimum value occurs.
- 3. c. How does the inclusion of this additional information change the shape of the cost function and the location of the global minimum, compared to \$\$(1.737,\theta)\$?
- 4. d. Finally, reconsider the fact that \$\theta \approx 7 \pm .5\$ (as prior information). To account for this in your cost function, the additional term in \$S_{b}(1.737,\theta)\$ could be modified to \$\displaystyle \frac{(\theta-7)^{2}}{0.5^{2}}\$. How does that additional modification change \$S_{b}(1.737,\theta)\$ further and the location of the global minimum?
- 5. e. Let's say researchers believe \$\theta \approx \mu \pm \sigma\$. What would be a general expression to include in the original cost function \$\$(1.737,\theta)\$ to account for this information? Your final expression will have \$\mu\$ and \$\sigma\$ in it.
- 6. f. Use [desmos](https://www.desmos.com/calculator) or other graphic software to investigate what would happen in your general expression as \$\mu\$ and \$\sigma\$. First set \$\sigma=0.5\$ and let \$\mu=7\$ be a slider. Investigate values of \$\mu\$ between 3 and 10 and report what happens. Next set \$\mu=7\$ and let \$\sigma = 0.5\$ be a slider. Investigate values of \$\sigma\$ between 0.1 and 1 and report what happens.