

Pre-Calculus: Unit 3 Test Review

Name:

1. What is the exact value of $\tan(195 \text{ degrees})$?

2. Which expression is equivalent to $\cos(\frac{\pi}{12})\cos(\frac{5\pi}{12}) + \sin(\frac{\pi}{12})\sin(\frac{5\pi}{12})$?

a. $\cos(-\frac{\pi}{3})$

b. $\sin(\frac{\pi}{2})$

c. $\sin(-\frac{\pi}{3})$

d. $\cos(\frac{\pi}{2})$

3. What is the exact value of $\tan(\frac{19\pi}{12})$?

4. Simplify $\sin(x + \pi)$.

5. What is the value of $1 - 2\sin^2(105 \text{ degrees})$?

6. Which expression is equal to $\frac{1}{\sin(2x)} - \frac{\cos(2x)}{\sin(2x)}$?

a. $\frac{1}{\cos(x)}$

b. $\tan(x)$

c. $-\frac{1}{\cos(x)}$

d. $-\tan(x)$

7. Which statement is true about the graph of the equation $y = \csc^{-1}(x)$?
- There is a vertical asymptote at $x = \frac{\pi}{2}$.
 - There is a vertical asymptote at $x = 0$.
 - There is a horizontal asymptote at $y = 0$.
 - There is a horizontal asymptote at $y = \frac{\pi}{2}$.
8. What is the solution to the inequality $\sin(x) > \cos(x)$ over the interval $0 \leq x \leq 2\pi$.
9. Complete step 4 of the proof.

Review the proof of $\cos(A - B) = \cos A \cos B + \sin A \sin B$.

$$\text{Step 1: } \sqrt{(\cos A - \cos B)^2 + (\sin A - \sin B)^2}$$

$$= \sqrt{(\cos(A - B) - 1)^2 + (\sin(A - B) - 0)^2}$$

$$\text{Step 2: } (\cos A - \cos B)^2 + (\sin A - \sin B)^2$$

$$= (\cos(A - B) - 1)^2 + (\sin(A - B) - 0)^2$$

$$\text{Step 3: } \cos^2 A - 2 \cos A \cos B + \cos^2 B$$

$$+ \sin^2 A - 2 \sin A \sin B + \sin^2 B$$

$$= \cos^2(A - B) - 2(\cos(A - B))$$

$$+ 1 + \sin^2(A - B)$$

$$\text{Step 4: } \underline{\hspace{2cm}} - 2 \cos A \cos B - 2 \sin A \sin B$$

$$= \underline{\hspace{2cm}} - 2 \cos(A - B) + 1$$

$$\text{Step 5: } -2(\cos A \cos B + \sin A \sin B) = \cos(A - B)$$

$$\text{Step 6: } \cos A \cos B + \sin A \sin B = \cos(A - B)$$

$$\text{Step 7: } \cos(A - B) = \cos A \cos B + \sin A \sin B$$