Curriculum Units and Learning Outcomes

Content Area: 2-3 weeks Grade Level: 11 - 12

Unit 6: Advanced Functions

Unit Summary: This unit will focus on performing operations on functions, composing functions, and finding their inverses. The importance of understanding the domain and range of a function is emphasized. When graphed, function end behavior, increasing / decreasing intervals, positive / negative intervals, and relative extrema are analyzed.

Massachusetts Standards:

PC.F-BF

A. Build a function that models a relationship between two quantities.

- Write a function that describes a relationship between two quantities.
- (+) Compose functions.
- B. Build new functions from existing functions.
 - Find inverse functions.
 - (+) Verify by composition that one function is the inverse of another.
 - (+) Read values of an inverse function from a graph or a table, given that the function has an inverse.
 - (+) Produce an invertible function from a non-invertible function by restricting the domain.
 - (+) Understand the inverse relationship between exponents and logarithms and use this relationship to solve problems involving logarithms and exponents.

Enduring Understandings:

- Domain and range are important in the understanding of the behavior of functions. They also help in finding and understanding the validity of solutions.
- Not all inverses of functions are themselves functions
- Compositions of functions are created by substitutions of one function into another

Essential Questions:

- Why is finding the domain and range of a function important?
- How are the properties of functions and functional operations useful?
- How do I analyze graphs with a lens towards Calculus?
- How can real world applications be modeled using composite functions?

• How do I perform operations on functions?

Students will demonstrate KNOWLEDGE of:

- Understanding domain / range, relative extrema and end behavior of the graphs of all functions.
- Inverses and compositions of functions.
- limits of a function are the value that a function approaches but doesn't necessarily reach
- Piecewise functions

Students will be SKILLED at:

- Analyzing graphs of functions by examining the end behavior, relative extrema, increasing / decreasing intervals, positive / negative intervals
- Finding domain and range of functions graphically and algebraically
- Writing and graphing piecewise functions with linear and nonlinear functions.
- Find inverses of functions and stating the domain and range.
- Determining in inverses of functions are themselves functions
- Composing and evaluating functions
- Performing operations on functions

Estimated Duration: 2-3 weeks