

Mark Scheme

Q1.

Question	Scheme	Marks	AOs
	Integrate a w.r.t. time	M1	1.1a
	$\mathbf{v} = \frac{5t^2}{2}\mathbf{i} - 10t^{\frac{3}{2}}\mathbf{j} + \mathbf{C}$ (allow omission of C)	A1	1.1b
	$\mathbf{v} = \frac{5t^2}{2}\mathbf{i} - 10t^{\frac{3}{2}}\mathbf{j} + 20\mathbf{i}$	A1	1.1b
	When $t = 4$, $\mathbf{v} = 60\mathbf{i} - 80\mathbf{j}$	M1	1.1b
	Attempt to find magnitude: $\sqrt{(60^2 + 80^2)}$	M1	3.1a
	Speed = 100 m s^{-1}	A1ft	1.1b
(6 marks)			
Notes:			
1st M1: for integrating a w.r.t. time (powers of t increasing by 1) 1st A1: for a correct v expression without C 2nd A1: for a correct v expression including C 2nd M1: for putting $t = 4$ into their v expression 3rd M1: for finding magnitude of their v 3rd A1: ft for 100 m s^{-1}, follow through on an incorrect v			

Q2.

Question	Scheme	Marks	AOs
(a)	$\mathbf{v}_B = (-16\mathbf{i} - 3\mathbf{j}) + 5(2.4\mathbf{i} + \mathbf{j})$	M1	3.4
	$\mathbf{v}_B = (-4\mathbf{i} + 2\mathbf{j})$	A1	1.1b
	$\sqrt{(-4)^2 + 2^2}$	M1	3.1a
	$\sqrt{20} = 2\sqrt{5}, 4.5 \text{ or better (m s}^{-1}\text{)}$	A1	1.1b
		(4)	
(b)	<u>Using A as the initial position:</u> $\mathbf{r}_C = \mathbf{v}_A t + \frac{1}{2} \mathbf{a} t^2 + \mathbf{r}_A \quad \text{where } t = T$ $(4\mathbf{i} + c\mathbf{j}) = (-16\mathbf{i} - 3\mathbf{j})T + \frac{1}{2}(2.4\mathbf{i} + \mathbf{j})T^2 + (44\mathbf{i} - 10\mathbf{j})$ OR $\begin{pmatrix} 4 \\ c \end{pmatrix} = \begin{pmatrix} -16 \\ -3 \end{pmatrix}T + \frac{1}{2}\begin{pmatrix} 2.4 \\ 1 \end{pmatrix}T^2 + \begin{pmatrix} 44 \\ -10 \end{pmatrix}$ Equating i-components, to give a quadratic equation in T only. Allow t instead of T. N.B. Allow omission of 44 for this M mark. Also allow ± 4 but M0 if 4 is not used at all i.e. $4 = -16T + \frac{1}{2} \times 2.4T^2$ scores M1A0A0	M1	3.1a
	$4 = -16T + \frac{1}{2} \times 2.4T^2 + 44$	A1	1.1b
	$(T =) 10$	A1	1.1b
	ALTERNATIVE <u>using B as the initial position:</u> (The position vector of B, $\mathbf{r}_B$, should be $-6\mathbf{i} - 12.5\mathbf{j}$ but no credit for finding this) $\mathbf{r}_C = \mathbf{v}_B t + \frac{1}{2} \mathbf{a} t^2 + \mathbf{r}_B \quad \text{using their } \mathbf{v}_B \text{ from (a) and their } \mathbf{r}_B$ $(4\mathbf{i} + c\mathbf{j}) = (-4\mathbf{i} + 2\mathbf{j})t + \frac{1}{2}(2.4\mathbf{i} + \mathbf{j})t^2 + (-6\mathbf{i} - 12.5\mathbf{j})$ $\begin{pmatrix} 4 \\ c \end{pmatrix} = \begin{pmatrix} -4 \\ 2 \end{pmatrix}t + \frac{1}{2}\begin{pmatrix} 2.4 \\ 1 \end{pmatrix}t^2 + \begin{pmatrix} -6 \\ -12.5 \end{pmatrix}$ Equating i-components, to give a quadratic equation in t only. Allow if they have T instead of t.	M1	3.1a

	N.B. Allow omission of their -6 or if they use 44 for this M mark. Also allow ± 4 but M0 if 4 is not used at all. e.g. $4 = -4t + \frac{1}{2} \times 2.4t^2$ scores M1A0A0		
	$4 = -4t + \frac{1}{2} \times 2.4t^2 - 6$	A1	1.1b
	$t = 5$ so $(T =) 10$	A1	1.1b
		(3)	
(c)	Equating j-components, with <u>their value of T or t substituted</u>, to give an equation, which must have a square term, in c only. N.B. Allow $\pm c$ in their equation. (N.B. Allow omission of -10 or their -12.5 for this M mark i.e. if using A as initial position $c = (-3 \times 10) + \frac{1}{2} \times 1 \times 10^2$ scores M1M0A0 OR if using B as initial position $c = (2 \times 5) + \frac{1}{2} \times 1 \times 5^2$ scores M1M0A0)	M1	2.1
	if using A as initial position $c = (-3 \times 10) + \frac{1}{2} \times 1 \times 10^2 + (-10)$ N.B. Allow $\pm c$ and/or $\pm(-10)$ in their equation OR if using B as initial position $c = (2 \times 5) + \frac{1}{2} \times 1 \times 5^2 + (-12.5)$ N.B. Allow $\pm c$ and/or $\pm(-12.5)$ in their equation	M1	1.1b
	$c = 10$	A1	1.1b
		(3)	

(10 marks)

Notes: Accept column vectors throughout

a	M1	Use of $\mathbf{v} = \mathbf{u} + \mathbf{at}$ with $t = 5$ to give an unsimplified $\mathbf{v}_B$ M0 if $\mathbf{u} = 0$
		N.B. If using integration, they must get to the same stage i.e. have found the constant and put $t = 5$ M0 if they omit the constant altogether
	A1	Correct $\mathbf{v}_B$ with $\mathbf{i}$'s and $\mathbf{j}$'s collected
	M1	Use of Pythagoras on <i>their</i> $\mathbf{v}_B$ to give a magnitude (need the root)
	A1	Must be positive
b	M1	Equating components of $\mathbf{i}$ to give an equation in T or t only. N.B. (they could use integration to get to the same stage) for this M mark, they only need to be equating the $\mathbf{i}$ -components, and receive no credit until they do so. M0 if $\mathbf{u} = 0$
	A1	A correct equation in T or t only (could be in $(T - 5)$ if using B as initial position)
	A1	$T = 10$
c	M1	Equating components of $\mathbf{j}$ to give an equation in c only but allow omission of their initial position
	M1	With their value of T or t and must include $t = 0$ position (should be -10 if using A OR their -12.5 if using B)
	A1	cao

Q3.

Question	Scheme	Marks	AOs
(i)(a)	Integrate a wrt t to obtain velocity	M1	3.4
	$v = (t - 2t^2)\mathbf{i} + \left(3t - \frac{1}{3}t^3\right)\mathbf{j} (+C)$	A1	1.1b
	$8\mathbf{i} - \frac{28}{3}\mathbf{j} \text{ (m s}^{-1}\text{)}$	A1	1.1b
		(3)	
(i)(b)	Equate $\mathbf{i}$ component of v to zero	M1	3.1a
	$t - 2t^2 + 36 = 0$	A1ft	1.1b
	$t = 4.5$ (ignore an incorrect second solution)	A1	1.1b
		(3)	
(ii)	Differentiate r wrt to t to obtain velocity	M1	3.4
	$v = (2t - 1)\mathbf{i} + 3\mathbf{j}$	A1	1.1b
	Use magnitude to give an equation in t only	M1	2.1
	$(2t - 1)^2 + 3^2 = 5^2$	A1	1.1b
	Solve problem by solving this equation for t	M1	3.1a
	$t = 2.5$	A1	1.1b
		(6)	
(12 marks)			

Notes: Accept column vectors throughout		
(i)(a)	M1	At least 3 terms with powers increasing by 1 (but M0 if clearly just multiplying by t)
	A1	Correct expression
	A1	Accept $8\mathbf{i} - 9.3\mathbf{j}$ or better. Isw if speed found.
(i)(b)	M1	Must have an equation in t only (Must have integrated to find a velocity vector)
	A1 ft	Correct equation follow through on their v but must be a 3 term quadratic
	A1	cao
(ii)	M1	At least 2 terms with powers decreasing by 1 (but M0 if clearly just dividing by t)
	A1	Correct expression
	M1	Use magnitude to give an equation in t only, must have differentiated to find a velocity (M0 if they use $\sqrt{x^2 + y^2}$)
	A1	Correct equation $\sqrt{(2t-1)^2 + 3^2} = 5$
	M1	Solve a 3 term quadratic for t which has come from differentiating and using a magnitude. This M mark can be implied by a correct answer with no working.
	A1	2.5

Q4.

Question Number	Scheme	Marks	Notes
(a)	Integrate: $\mathbf{v} = (t^3 - 2t^2)\mathbf{i} + (3t^2 - 5t)\mathbf{j} + \mathbf{C}$ $t = 3 : \mathbf{v} = 9\mathbf{i} + 12\mathbf{j} + \mathbf{C} = 11\mathbf{i} + 10\mathbf{j}$ $\mathbf{C} = 2\mathbf{i} - 2\mathbf{j}$ $\mathbf{v} = (t^3 - 2t^2 + 2)\mathbf{i} + (3t^2 - 5t - 2)\mathbf{j}$	M1	At least 3 powers going up. Condone errors in constants. Must be two separate component equations if not in vector form. Could be in column vector form. Allow with no "+ C"
		A2	-1 each integration error. i.e. All correct A1A1 1 error A1A0, 2 or more errors A0A0 Allow with no "+ C"
		DM1	Substitute given values to find C. Dependent on the previous M mark
		A1 (5)	Correct velocity (any equivalent form)
(b)	Parallel to $\mathbf{i} \Rightarrow 3t^2 - 5t - 2 = 0$ $(3t+1)(t-2) = 0,$ $t = 2$ $ \mathbf{v} = 8 - 8 + 2 = 2 \text{ (m s}^{-1}\text{)}$	M1	Set $\mathbf{j}$ component of their $\mathbf{v}$ equal to zero and solve for t . Correct answers imply method, but incorrect answers need to show method clearly.
		A1	Correct only. Ignore $-\frac{1}{3}$ if present.
		DM1	Substitute their t to find $\mathbf{v}$. Dependent on the previous M mark.
		A1 (4)	The answer must be a scalar – the Q asks for speed. Results from negative t must be rejected.
		[9]	
A candidate who has no "+C" can score at most M1A2M0A0 M1A0M1A0			

Q5.

Q	Scheme	Marks
(a)	$t = \frac{5}{4}$	B1 M1 1.25
(b)	$\mathbf{r} = (2t^2 - 5t)\mathbf{i} + 3t\mathbf{j} + c\mathbf{k}$	Integrate the velocity vector
	$t = 0 \quad 2\mathbf{i} + 5\mathbf{j} = c$	A1 DM1 Correct
	$\mathbf{r} = (2t^2 - 5t)\mathbf{i} + 3t\mathbf{j} + (2\mathbf{i} + 5\mathbf{j})$	A1 Use $\mathbf{r}_0$ to find C
	$(2t^2 - 5t + 2)\mathbf{i} + (3t + 5)\mathbf{j}$	oe
(c)	$\mathbf{r}_Q = 11\mathbf{i} + 2\mathbf{j} - 2t\mathbf{i} + ct\mathbf{j}$	B1
	$(11 - 2t)\mathbf{i} + (2 + ct)\mathbf{j}$	Correct $\mathbf{j}$ component of $\mathbf{r}_Q$ Do not actually require the whole thing - can answer the Q by considering only the $\mathbf{j}$ component.
	$\mathbf{r}_P = (2t^2 - 5t + 2)\mathbf{i} + (3t + 5)\mathbf{j}$	
	$\mathbf{r}_Q = \mathbf{r}_P = d\mathbf{i} + 14\mathbf{j}$	$2t^2 - 5t$
	$3t + 5 = 14$	M1 Form an equation in t only
	$2t^2 - 3t - 9$ $(2t + 3)(t - 3) = 0$ $t = 3$ A1 ft	A1 A1 ft
	$t = 3$	Their t
	$2 + ct = 14 \Rightarrow c = 4$	Their t
	$d = 11 - 2 \times 3 = 5$ or	
	$d = 2 \times 3^2 - 5 \times 3 + 2 \Rightarrow d = 5$	
	Alt: $2t^2 - 5t + 2 = 11 - 2t = d \Rightarrow t = \frac{11-d}{2}$	
	$2\left(\frac{11-d}{2}\right)^2 - 5\left(\frac{11-d}{2}\right) + 2 = d,$	
	$d^2 - 19d + 70 = 0 = (d - 5)(d - 14)$	

Q6.

Question Number	Scheme	Marks	Notes
(a)	$\mathbf{a} = \frac{d\mathbf{v}}{dt} = 6\mathbf{i} + (4 - 2t)\mathbf{j}$ When $t = 1$, $\mathbf{a} = 6\mathbf{i} + 2\mathbf{j}$ $ \mathbf{a} = \sqrt{6^2 + 2^2} = \sqrt{40} = 6.32 \text{ (m s}^{-2}\text{)}$	M1 A1 DM1 DM1 A1 (5)	Differentiate $\mathbf{v}$ to obtain $\mathbf{a}$. Accept column vector or $\mathbf{i}$ and $\mathbf{j}$ components dealt with separately. Substitute $t = 1$ into their $\mathbf{a}$. Dependent on 1 st M1 Use of Pythagoras to find the magnitude of their $\mathbf{a}$. Allow with their t . Dependent on 1 st M1 Accept awrt 6.32, 6.3 or exact equivalents.
(b)	$\mathbf{r} = \int (3t^2 - 1)\mathbf{i} + (4t - t^2)\mathbf{j} \, dt$ $= (t^3 - t + C)\mathbf{i} + (2t^2 - \frac{1}{3}t^3 + D)\mathbf{j}$ $t = 0, \mathbf{r} = \mathbf{i} \Rightarrow C = 1, D = 0$ When $t = 3, \mathbf{r} = 25\mathbf{i} + 9\mathbf{j} \text{ (m)}$	M1 A1 DM1 DM1 A1 (5)	Integrate $\mathbf{v}$ to obtain $\mathbf{r}$ Condone C, D missing Use $t = 0, \mathbf{r} = \mathbf{i}$ to find C & D Substitute $t = 3$ with their C & D to find $\mathbf{r}$. Dependent on both previous Ms. cao. Must be a vector.
		10	

Q7.

(a)	Speed = $\sqrt{8^2 + 48^2} = \sqrt{2368} = 48.7 \text{ (ms}^{-1}\text{)}$	M1 A1	(2)
(b)	$\mathbf{a} = 2\mathbf{i} - 6t\mathbf{j}$ When $t = 4$, $\mathbf{a} = 2\mathbf{i} - 24\mathbf{j} \text{ (ms}^{-2}\text{)}$	M1 A1 A1	(3)
(c)	$\mathbf{r} = t^2\mathbf{i} - t^3\mathbf{j} + \mathbf{C}$ $t = 1, -4\mathbf{i} + \mathbf{j} = \mathbf{i} - \mathbf{j} + \mathbf{C}, \mathbf{C} = -5\mathbf{i} + 2\mathbf{j}$ $\mathbf{r} = (t^2 - 5)\mathbf{i} + (-t^3 + 2)\mathbf{j}$ When $t = 4, \mathbf{r} = (16 - 5)\mathbf{i} + (-64 + 2)\mathbf{j} = 11\mathbf{i} - 62\mathbf{j}$	M1 A1 DM1 DM1 A1	(5) 10

Q8.

Question Number	Scheme	Marks
(a)	$\mathbf{a} = \frac{dv}{dt} = 6t\mathbf{i} - 4\mathbf{j}$	M1 A1
(b)	Using $\mathbf{F} = m\mathbf{a}$, sub $t = 2$, finding modulus e.g. at $t = 2$, $\mathbf{a} = 12\mathbf{i} - 4\mathbf{j}$ $\mathbf{F} = 6\mathbf{i} - 2\mathbf{j}$ $\mathbf{F} = \sqrt{(6^2 + 2^2)} \approx \underline{6.32 \text{ N}}$	M1, M1, M1 A1(CSO)
	M1 Clear attempt to differentiate. Condone i or j missing. A1 both terms correct (column vectors are OK) The 3 method marks can be tackled in any order, but for consistency on open grid please enter as: M1 $\mathbf{F} = m\mathbf{a}$ (their $\mathbf{a}$, (correct $\mathbf{a}$ or following from (a)), not $\mathbf{v}$. $\mathbf{F} = \frac{1}{2} \mathbf{a}$). Condone $\mathbf{a}$ not a vector for this mark. M1 subst $t = 2$ into candidate's vector $\mathbf{F}$ or $\mathbf{a}$ ($\mathbf{a}$ correct or following from (a), not $\mathbf{v}$) M1 Modulus of candidate's $\mathbf{F}$ or $\mathbf{a}$ (not $\mathbf{v}$) A1 CSO All correct (beware fortuitous answers e.g. from $6t\mathbf{i} + 4\mathbf{j}$)) Accept 6.3, awrt 6.32, any exact equivalent e.g. $2\sqrt{10}$, $\sqrt{40}$, $\frac{\sqrt{160}}{2}$	

Q9.

Question	Scheme	Marks	AOs
(a)	$(4\mathbf{i} - \mathbf{j}) + (\lambda\mathbf{i} + \mu\mathbf{j}) = (4 + \lambda)\mathbf{i} + (-1 + \mu)\mathbf{j}$	M1	3.4
	Use ratios to obtain an equation in λ and μ only	M1	2.1
	$\frac{(4 + \lambda)}{(-1 + \mu)} = \frac{3}{1}$ or $\frac{\frac{1}{4}(4 + \lambda)}{\frac{1}{4}(-1 + \mu)} = \frac{3}{1}$	A1	1.1b
	$\lambda - 3\mu + 7 = 0$ * Allow $0 = \lambda - 3\mu + 7$ but nothing else.	A1*	1.1b
		(4)	

(b)	$\lambda = 2 \Rightarrow \mu = 3$; Resultant force = $(6\mathbf{i} + 2\mathbf{j})$ (N)	M1	3.1a
	$(6\mathbf{i} + 2\mathbf{j}) = 4\mathbf{a}$ OR $ (\mathbf{6i} + 2\mathbf{j}) = 4a$	M1	1.1b
	Use of $\mathbf{r} = \mathbf{ut} + \frac{1}{2}\mathbf{at}^2$ with $\mathbf{u} = 0$, their $\mathbf{a}$ and $t = 4$: Or they may integrate their $\mathbf{a}$ twice with $\mathbf{u} = 0$ and put $t = 4$: $\mathbf{r} = \frac{1}{2} \times \frac{(6\mathbf{i} + 2\mathbf{j})}{4} \cdot 4^2 = (12\mathbf{i} + 4\mathbf{j})$	DM1	2.1
	$\sqrt{12^2 + 4^2}$	M1	1.1b
	ALTERNATIVE 1 for last two M marks: Use of $s = ut + \frac{1}{2}at^2$, with $u = 0$, their a and $t = 4$: $s = \frac{1}{2} \times \sqrt{1.5^2 + 0.5^2} \times 4^2$ Use of Pythagoras to find mag of $\mathbf{a}$: $a = \sqrt{1.5^2 + 0.5^2}$	DM1 M1	
	ALTERNATIVE 2 for last two M marks: Use of $s = ut + \frac{1}{2}at^2$, with $u = 0$, their a and $t = 4$: $s = \frac{1}{2} \times \left(\frac{\sqrt{6^2 + 2^2}}{4} \right) \times 4^2$ Use of Pythagoras to find $ (\mathbf{6i} + 2\mathbf{j}) $: $= \sqrt{6^2 + 2^2}$	DM1 M1	
	$\sqrt{160}$, $2\sqrt{40}$, $4\sqrt{10}$ oe or 13 or better (m)	A1	1.1b
		(5)	
	(9 marks)		

Notes: Accept column vectors throughout

a	M1	Adding the two forces, $\mathbf{i}$'s and $\mathbf{j}$'s must be collected (or must be a single column vector) seen or implied
	M1	Must be using ratios; Ignore an equation e.g. $(4 + \lambda)\mathbf{i} + (-1 + \mu)\mathbf{j} = 3\mathbf{i} + \mathbf{j}$ if they go on to use ratios.

		However, if they write $4 + \lambda = 3$ and $-1 + \mu = 1$ then $3(-1 + \mu) = 3$ so $4 + \lambda = 3(-1 + \mu)$ with no use of a constant, it's M0 They may use the acceleration, with a factor of $\frac{1}{4}$ top and bottom, see alternative Allow one side of the equation to be inverted
	A1	Correct equation
	A1*	Given answer correctly obtained. Must see at least one line of working, with the LH fraction 'removed'.
b	M1	Adding F_1 and F_2 to find the resultant force, λ and μ must be substituted N.B. M0 if they use $\mu = 2$ coming from $-1 + \mu = 1$ in part (a).
	M1	Use of $F = 4a$ Or $\mathbf{F} = 4a$, where $\mathbf{F}$ is <u>their</u> resultant. (including $3\mathbf{i} + \mathbf{j}$) This is an independent mark, so could be earned, for example, if they have subtracted the forces to find the 'resultant' N.B. M0 if only using F_1 or F_2
	DM 1	Dependent on previous M mark for Either: use of $\mathbf{r} = \mathbf{ut} + \frac{1}{2}\mathbf{at}^2$ with $\mathbf{u} = 0$, their $\mathbf{a}$ and $t = 4$ to produce a displacement vector Or : integrate twice, with $\mathbf{u} = 0$, their $\mathbf{a}$ and $t = 4$ to produce a displacement Vector Or: use of $s = \mathbf{ut} + \frac{1}{2}\mathbf{at}^2$ with $\mathbf{u} = 0$, their $\mathbf{a}$ and $t = 4$ to produce a length
	M1	Use of Pythagoras, with square root, to find the magnitude of their displacement vector, a or F (M0 if only using F_1 or F_2) depending on which method they have used.
	A1	cao

Q10.

Question	Scheme	Marks	AO
(a)	Differentiate v	M1	1.1a
	$(\mathbf{a} =) 6\mathbf{i} - \frac{15}{2}t^{\frac{1}{2}}\mathbf{j}$	A1	1.1b
	$= 6\mathbf{i} - 15\mathbf{j} \text{ (m s}^{-2}\text{)}$	A1	1.1b
		(3)	
(b)	Integrate v	M1	1.1a
	$(\mathbf{r} =)(\mathbf{r}_0) + 3t^2\mathbf{i} - 2t^{\frac{5}{2}}\mathbf{j}$	A1	1.1b
	$= (-20\mathbf{i} + 20\mathbf{j}) + (48\mathbf{i} - 64\mathbf{j}) = 28\mathbf{i} - 44\mathbf{j} \text{ (m)}$	A1	2.2a
		(3)	
		(6)	

Marks		Notes
		N.B. Accept column vectors throughout and condone missing brackets in working but they must be there in final answers
a	M1	Use of $\mathbf{a} = \frac{d\mathbf{v}}{dt}$ with attempt to differentiate (both powers decreasing by 1) M0 if i 's and j 's omitted and they don't recover
	A1	Correct differentiation in any form
	A1	Correct and simplified. Ignore subsequent working (ISW) if they go on and find the magnitude.
b	M1	Use of $\mathbf{r} = \int \mathbf{v} dt$ with attempt to integrate (both powers increasing by 1) M0 if i 's and j 's omitted and they don't recover
	A1	Correct integration in any form. Condone r ₀ not present
	A1	Correct and simplified.

Q11.

Question	Scheme	Marks	AOs
	Allow column vectors throughout this question		
(a)	Differentiate $\mathbf{v}$ wrt t	M1	3.1a
	$\frac{3}{2}t^{-\frac{1}{2}}\mathbf{i} - 2\mathbf{j}$ isw	A1	1.1b
		(2)	
(b)	$3t^{\frac{1}{2}} = 2t$	M1	2.1
	Solve for t	DM1	1.1b
	$t = \frac{9}{4}$	A1	1.1b
		(3)	
(c)	Integrate $\mathbf{v}$ wrt t	M1	3.1a
	$\mathbf{r} = 2t^{\frac{3}{2}}\mathbf{i} - t^2\mathbf{j} (+C)$	A1	1.1b
	$t = 1, \mathbf{r} = -\mathbf{j} \Rightarrow C = -2\mathbf{i}$ so $\mathbf{r} = 2t^{\frac{3}{2}}\mathbf{i} - t^2\mathbf{j} - 2\mathbf{i}$	A1	2.2a
		(3)	
(d)	$\sqrt{(3t^{\frac{1}{2}})^2 + (2t)^2} = 10$ or $(3t^{\frac{1}{2}})^2 + (2t)^2 = 10^2$	M1	2.1
	$9t + 4t^2 = 100$	M(A)1	1.1b
	$t = 4$	A1	1.1b
	$\mathbf{r} = 14\mathbf{i} - 16\mathbf{j}$	M1	1.1b
	$\sqrt{14^2 + (-16)^2}$	M1	3.1a
	$\sqrt{452} \ (2\sqrt{113}) \text{ (m)}$	A1	1.1b
		(6)	
(14 marks)			

Notes:		
a	M1	Both powers decreasing by 1 (M0 if vector(s) disappear but allow recovery)
	A1	cao
b	M1	Complete method, using v , to obtain an equation in t only, allow a sign error
	DM1	Dependent on M1, solve for t
	A1	cao
c	M1	Both powers increasing by 1 (M0 if vectors disappear but allow recovery)
	A1	Correct expression without C
	A1	cao
d	M1	Use of Pythagoras on v and 10 to set up equation in t
	M(A)1	Correct 3 term quadratic in t
	A1	cao
	M1	Substitute their numerical t value into their r
	M1	Use of Pythagoras to find the magnitude of their r
	A1	cso

Q12.

Question	Scheme	Marks	AOs
(a)	$7\mathbf{i} - 3\mathbf{j}$ seen or implied by Pythagoras	B1	1.1b
	Use Pythagoras: $\sqrt{7^2 + (-3)^2}$	M1	3.1a
	$\sqrt{58}$, 7.6 or better (m s^{-1})	A1	1.1b
		(3)	
(b)	$t^2 - 3t + 7 = 2t^2 - 3$ OR $\frac{t^2 - 3t + 7}{2t^2 - 3} = \frac{1}{1} = 1$	M1	2.1
	$t = 2$ only	A1	1.1b
		(2)	
(c)	Differentiate $\mathbf{v}$ wrt t to give a vector.	M1	3.1a
	$(2t - 3)\mathbf{i} + 4t\mathbf{j}$	A1	1.1b
		(2)	
(d)	$2t - 3 = 0$	M1	3.1a
	$t = 1.5$	A1	1.1b
		(2)	
(9 marks)			

Notes: Allow column vectors throughout.

a	B1	cao
	M1	Use of Pythagoras, including the square root, on a velocity vector at $t = 0$
	A1	cao. Must come from a <u>correct</u> v .
b	M1	Equating i and j components of v or a ratio of 1:1 to obtain a quadratic in t only. If they use a constant, e.g. $t^2 - 3t + 7 = k$ and $2t^2 - 3 = k$, k must be eliminated to earn this mark. N.B. M0 (since wrong working seen) if they write down $\mathbf{i} + \mathbf{j} = (t^2 - 3t + 7)\mathbf{i} + (2t^2 - 3)\mathbf{j}$ OR $\begin{pmatrix} 1 \\ 1 \end{pmatrix} = \begin{pmatrix} t^2 - 3t + 7 \\ 2t^2 - 3 \end{pmatrix}$ OR $t^2 - 3t + 7 = 1$ and $2t^2 - 3 = 1$
		and then $t^2 - 3t + 7 = 2t^2 - 3$
	A1	$t = 2$
		N.B. Allow M1A1 for a correct trial and error method where they obtain $\mathbf{v} = 5\mathbf{i} + 5\mathbf{j}$ when $t = 2$ but M0 if they don't get $t = 2$
c	M1	At least one power decreasing by 1 in each component in their v (M0 if clearly dividing by t) Both i and j needed in their answer or a column vector Allow recovery if the i and j disappear and then reappear.
	A1	cao (must be a vector) isw e.g. if they find the magnitude or put $t = 0$ or differentiate again i's and j's do not need to be collected. N.B. Allow M1A0 for $2t - 3\mathbf{i} + 4t\mathbf{j}$
d	M1	$2t - 3 = 0$ or (their derivative of the i-component of v) $= 0$ N.B. M0 if they equate the derivative of both components of v to zero.
	A1	cao N.B. Correct answer, with no working, can score both marks.

Q13.

Question	Scheme	Marks	AOs
(a)	Use of $\mathbf{v} = \mathbf{u} + \mathbf{a}t$ or integrate to give: $\mathbf{v} = (-2\mathbf{i} + 2\mathbf{j}) + 2(4\mathbf{i} - 5\mathbf{j})$	M1	3.1a
	$(6\mathbf{i} - 8\mathbf{j}) (\text{m s}^{-1})$	A1	1.1b
		(2)	
(b)	Solve problem through use of $\mathbf{r} = \mathbf{u}t + \frac{1}{2}\mathbf{a}t^2$ or integration (M0 if $\mathbf{u} = 0$) Or any other complete method e.g use $\mathbf{v} = \mathbf{u} + \mathbf{a}T$ and $\mathbf{r} = \frac{(\mathbf{u} + \mathbf{v})T}{2}$:	M1	3.1a
	$-4.5\mathbf{j} = 2t\mathbf{j} - \frac{1}{2}t^2 5\mathbf{j}$ (j terms only)	A1	1.1b
	The first two marks could be implied if they go straight to an algebraic equation.		
	Attempt to equate j components to give equation in T only $(-4.5 = 2T - \frac{5}{2}T^2)$	M1	2.1
	$T = 1.8$	A1	1.1b
		(4)	
(c)	Solve problem by substituting <u>their</u> T value (M0 if $T < 0$) into the i component equation to give an equation in λ only: $\lambda = -2T + \frac{1}{2}T^2 \times 4$	M1	3.1a
	$\lambda = 2.9$ or 2.88 or $\frac{72}{25}$ oe	A1	1.1b
		(2)	
Notes: Accept column vectors throughout		(8 marks)	

Notes: Accept column vectors throughout		(8 marks)
2a	M1	For any complete method to give a v expression with correct no. of terms with $t = 2$ used, so if integrating, must see the initial velocity as the constant. Allow sign errors.
	A1	Cao isw if they go on to find the speed.
2b	M1	For any complete method to give a vector expression for j component of displacement in t (or T) only, using $a = (4i - 5j)$, so if integrating, RHS of equation must have the correct structure. Allow sign errors.
	A1	Correct j vector equation in t or T . Ignore i terms.
	M1	Must have earned 1 st M mark. Equate j components to give equation in T (allow t) only (no j 's) which has come from a displacement. Equation must be a 3 term quadratic in T .
	A1	cao
2c	M1	Must have earned 1 st M mark in (b) Complete method - must have an equation in λ only (no i 's) which has come from an appropriate displacement.. (e.g M0 if $a = 0$ has been used) Expression for λ must be a quadratic in T
	A1	cao

Q14.

Question	Scheme	Marks	AOs
(a)	Use of $\mathbf{v} = \mathbf{u} + \mathbf{at}$: $(10.5\mathbf{i} - 0.9\mathbf{j}) = 0.6\mathbf{j} + 15\mathbf{a}$	M1	3.1b
	$\mathbf{a} = (0.7\mathbf{i} - 0.1\mathbf{j}) \text{ m s}^{-2}$ Given answer	A1	1.1b
		(2)	
(b)	Use of $\mathbf{r} = \mathbf{ut} + \frac{1}{2} \mathbf{at}^2$	M1	3.1b
	$\mathbf{r} = 0.6\mathbf{j} t + \frac{1}{2} (0.7\mathbf{i} - 0.1\mathbf{j}) t^2$	A1	1.1b
		(2)	
(c)	Equating the $\mathbf{i}$ and $\mathbf{j}$ components of $\mathbf{r}$	M1	3.1b
	$\frac{1}{2} \leftarrow 0.7 t^2 = 0.6 t - \frac{1}{2} \leftarrow 0.1 t^2$	A1ft	1.1b
	$t = 1.5$	A1	1.1b
		(3)	
(d)	Use of $\mathbf{v} = \mathbf{u} + \mathbf{at}$: $\mathbf{v} = 0.6\mathbf{j} + (0.7\mathbf{i} - 0.1\mathbf{j}) t$	M1	3.1b
	Equating the $\mathbf{i}$ and $\mathbf{j}$ components of $\mathbf{v}$	M1	3.1b
	$t = 0.75$	A1 ft	1.1b
		(3)	
(10 marks)			

Notes:

(a)

M1: for use of $\mathbf{v} = \mathbf{u} + \mathbf{at}$

A1: for given answer correctly obtained

(b)

M1: for use of $\mathbf{r} = \mathbf{ut} + \frac{1}{2} \mathbf{at}^2$ A1: for a correct expression for $\mathbf{r}$ in terms of t

(c)

M1: for equating the $\mathbf{i}$ and $\mathbf{j}$ components of their $\mathbf{r}$ A1ft: for a correct equation following their $\mathbf{r}$ A1: for $t = 1.5$

(d)

M1: for use of $\mathbf{v} = \mathbf{u} + \mathbf{at}$ for a general t M1: for equating the $\mathbf{i}$ and $\mathbf{j}$ components of their $\mathbf{v}$ A1ft: for $t = 0.75$, or a correct follow through answer from an incorrect equation

Q15.

Question Number	Scheme	Marks
(a)	$\tan \theta = \frac{2}{9}$ $\theta = 12.5^\circ$ bearing 103°	M1 A1 A1 (3)
(b) (i) (ii)	$\mathbf{p} = (9\mathbf{i} + 10\mathbf{j}) + t(9\mathbf{i} - 2\mathbf{j})$ $\mathbf{q} = (\mathbf{i} + 4\mathbf{j}) + t(4\mathbf{i} + 8\mathbf{j})$	M1 A1 A1 (3)
(c)	$\overrightarrow{QP} = (8 + 5t)\mathbf{i} + (6 - 10t)\mathbf{j}$	M1 A1 (2)
(d)	$D^2 = (8 + 5t)^2 + (6 - 10t)^2$ $= 125t^2 - 40t + 100$ $100 = 125t^2 - 40t + 100$ $0 = 5t(25t - 8)$ $t = 0 \text{ or } 0.32$	M1 A1 M1 M1 A1 A1 (6) 14
	Notes	
(a)	M1 for $\tan \theta = \pm \frac{2}{9}$ or $\pm \frac{9}{2}$ or use $\sin \theta$ or $\cos \theta$	
	First A1 for $\theta = \pm 13^\circ$ or $\pm 77^\circ$ or $\pm 12.5^\circ$ or $\pm 77.5^\circ$ or better	
	Second A1 for 103°	
(b)	M1 for clear attempt at $\mathbf{p} = (9\mathbf{i} + 10\mathbf{j}) + t(9\mathbf{i} - 2\mathbf{j})$ or $\mathbf{q} = (\mathbf{i} + 4\mathbf{j}) + t(4\mathbf{i} + 8\mathbf{j})$ (Allow slips but must be a '+' sign and $\mathbf{r} + t\mathbf{v}$)	
(i)	First A1 for $\mathbf{p} = (9\mathbf{i} + 10\mathbf{j}) + t(9\mathbf{i} - 2\mathbf{j})$ oe	
(ii)	Second A1 for $\mathbf{q} = (\mathbf{i} + 4\mathbf{j}) + t(4\mathbf{i} + 8\mathbf{j})$ oe	
(c)	M1 for $\mathbf{p} - \mathbf{q}$ or $\mathbf{q} - \mathbf{p}$ with their $\mathbf{p}$ and $\mathbf{q}$ substituted A1 for correct answer $\overrightarrow{QP} = (8 + 5t)\mathbf{i} + (6 - 10t)\mathbf{j}$ (don't need $\overrightarrow{QP}$ but on R.H.S must be identical coefficients of $\mathbf{i}$ and $\mathbf{j}$ but allow column vectors)	
(d)	First M1 for attempt to find QP or QP^2 in terms of t only, using correct formula First A1 for a correct expression (with or without $\sqrt{}$) $125t^2 - 40t + 100$ Second M1 for $\sqrt{}$ (3 term quadratic) = 10 or (3 term quadratic) = 100. Third M1 for quadratic expression = 0 and attempt to solve (e.g. factorising or using formula) Second A1 for $t = 0$ (if they divide by t and lose this value but get 0.32, M1A0A1) Third A1 for $t = 0.32$ oe	

Q16.

Question Number	Scheme	Marks
(a)	$\tan \theta = \frac{5}{20}$ $\theta = 14.036..^{\circ}$ $\theta = 104^{\circ}$ nearest degree	M1 A1 A1 (3)
(b)	$\mathbf{p} = 400\mathbf{i} + t(15\mathbf{i} + 20\mathbf{j})$ $\mathbf{q} = 800\mathbf{j} + t(20\mathbf{i} - 5\mathbf{j})$	M1 A1 A1 (3)
(c)	Equate their $\mathbf{j}$ components: $20t(\mathbf{j}) = (800 - 5t)(\mathbf{j})$ $t = 32$ $\mathbf{s} = 800\mathbf{j} + 32(20\mathbf{i} - 5\mathbf{j})$ $= 640\mathbf{i} + 640\mathbf{j}$	M1 A1 M1 A1 (4) 10
(a)	Notes Allow column vectors throughout M1 for $\tan \theta = \pm \frac{5}{20}$ or $\pm \frac{20}{5}$ (or any other complete method) First A1 for $\pm 14.04^{\circ}$ or $\pm 75.96^{\circ}$ Second A1 for 104°	
(b) (i) (ii)	M1 for clear attempt at either $\mathbf{p}$ or $\mathbf{q}$ (allow slip but t <u>must</u> be attached to the velocity vector and position vector and velocity vector must be paired up correctly) First A1 $400\mathbf{i} + t(15\mathbf{i} + 20\mathbf{j})$ " $\mathbf{p} =$ " not needed but must be clear it's P Second A1 $800\mathbf{j} + t(20\mathbf{i} - 5\mathbf{j})$ " $\mathbf{q} =$ " not needed but must be clear it's Q	
(c)	First M1 for equating their $\mathbf{j}$ components; allow $\mathbf{j}$'s on both sides First A1 for $t = 32$ Second M1 <u>independent</u> for substituting their t value into their $\mathbf{q}$ from (b) Second A1 for $640\mathbf{i} + 640\mathbf{j}$	

Q17.

Question Number	Scheme	Marks
(a)	$\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$ $(-1+a)\mathbf{i} + (2+b)\mathbf{j}$ $\frac{-1+a}{2+b} = \frac{1}{3}$ $a = b = k = 2.5; \mathbf{F}_2 = 2.5\mathbf{i} + 2.5\mathbf{j}$ ALTERNATIVE: $\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$ $(-1+a)\mathbf{i} + (2+b)\mathbf{j} = p(\mathbf{i} + 3\mathbf{j})$ $-1+a = p$ $2+b = 3p$ $a = b = k = 2.5; \mathbf{F}_2 = 2.5\mathbf{i} + 2.5\mathbf{j}$	B1 M1 DM1 A1 DM1 A1; A1 (7) B1 M1 for LHS DM1 A1 DM1 A1; A1 (7)
(b)	$\mathbf{v} = 3\mathbf{i} - 22\mathbf{j} + 3(3\mathbf{i} + 9\mathbf{j})$ $= 12\mathbf{i} + 5\mathbf{j}$ $ \mathbf{v} = \sqrt{12^2 + 5^2} = 13 \text{ ms}^{-1}$	M1 A1 M1 A1 cso (4) 11
Notes		
(a)	B1 for $\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$ ($k \neq 1$) seen or implied in working, including for an incorrect final answer, with the wrong k value. First M1 for adding the 2 forces (for this M mark we only need $\mathbf{F}_2 = a\mathbf{i} + b\mathbf{j}$), with $\mathbf{i}$'s and $\mathbf{j}$'s collected (which can be implied by later working) but allow a slip. (M0 if a and b both assumed to be 1) Second M1, dependent on first M1, for ratio of their cpts = 1/3 or 3/1 (Must be correct way up for the M mark) First A1 for a correct equation which may involve two unknowns Third M1, dependent on first and second M1, for solving for k oe Second A1 for a correct k value Third A1 for $2.5\mathbf{i} + 2.5\mathbf{j}$	

ALTERNATIVE: Using two simultaneous equations

B1 for $\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$ ($k \neq 1$) seen or implied in working.

First M1 for adding the 2 forces (for this M mark we only need $\mathbf{F}_2 = a\mathbf{i} + b\mathbf{j}$), with $\mathbf{i}$'s and $\mathbf{j}$'s collected (LHS of equation) (M0 if a and b both assumed to be 1) but allow a slip

Second M1, dependent on first M1, for equating coeffs to produce *two* equations in 2 or 3 unknowns. Must have p and $3p$ (M0 if p is assumed to be 1 or k)

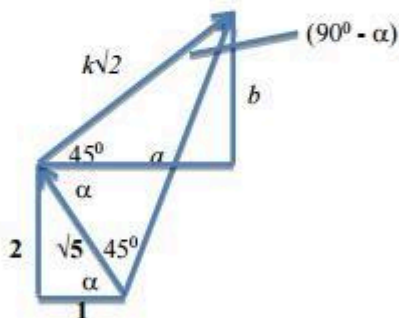
First A1 for two correct equations

Third M1, dependent on first and second M1, for solving for k or

Second A1 for a correct k value

Third A1 for $2.5\mathbf{i} + 2.5\mathbf{j}$

ALTERNATIVE: Using magnitudes and directions



$\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$, seen or implied

Correct vector triangle

$$\frac{k\sqrt{2}}{\sin 45^\circ} = \frac{\sqrt{5}}{\sin(90^\circ - \alpha)}, \quad \alpha = \arctan 2$$

$$2k = 5$$

$$k = 2.5; \quad \mathbf{F}_2 = 2.5\mathbf{i} + 2.5\mathbf{j}$$

B1
M1

DM1 A1

DM1 A1; A1
(7)

ALTERNATIVE: Using magnitudes and directions

B1 for $\mathbf{F}_2 = k\mathbf{i} + k\mathbf{j}$ seen or implied in working.

First M1 for a correct vector triangle (for this M mark we only need $\mathbf{F}_2 = a\mathbf{i} + b\mathbf{j}$). (M0 if a and b both assumed to be 1 and/or longest side is assumed to be $\sqrt{10}$)

Second M1, dependent on first M1, for using sine rule on vector triangle

First A1 for a correct equation. 45° may not appear exactly.

Third M1, dependent on first and second M1, for solving for k or

Second A1 for a correct k value

Third A1 for $2.5\mathbf{i} + 2.5\mathbf{j}$

(b)	First M1 for use of $\mathbf{v} = \mathbf{u} + \mathbf{a}t$ with $t = 3$ First A1 for $12\mathbf{i} + 5\mathbf{j}$ seen or implied. However, if a wrong $\mathbf{v}$ is seen A0 Second M1 for finding magnitude of their $\mathbf{v}$ Second A1 for 13	

Q18.

Question Number	Scheme	Marks
a	$\mathbf{F} = m\mathbf{a} : 3\mathbf{i} - 2\mathbf{j} = 0.5\mathbf{a}$ $\mathbf{a} = 6\mathbf{i} - 4\mathbf{j}$ $ \mathbf{a} = \sqrt{6^2 + (-4)^2} = 2\sqrt{13} \text{ (m s}^{-2}\text{) **}$	M1 A1 M1A1 (4)
b	$\mathbf{v} = \mathbf{u} + \mathbf{at} : \mathbf{v} = (\mathbf{i} + 3\mathbf{j}) + 2(6\mathbf{i} - 4\mathbf{j})$ $= 13\mathbf{i} - 5\mathbf{j} \text{ m s}^{-1}$	M1A1 ft A1 (3)
c	Distance = $2 \mathbf{v} = 2\sqrt{4+1} = 2\sqrt{5} = 4.47 \text{ (m)}$	M1A1 (2)
d	When $t = 3.5$, velocity of P is $(\mathbf{i} + 3\mathbf{j}) + 3.5(6\mathbf{i} - 4\mathbf{j}) = 22\mathbf{i} - 11\mathbf{j}$ Given conclusion reached correctly. E.g. $22\mathbf{i} - 11\mathbf{j} = 11(2\mathbf{i} - \mathbf{j})$	M1A1 ft A1 (3)
		[12]
Notes for Question		

Question (a)

Either:

First M1 for use of $F = m a$

First A1 for $a = 6i - 4j$

Second M1 for $a = \sqrt{6^2 + (-4)^2}$ (Allow $\sqrt{6^2 + 4^2}$)

Second A1 for $a = 2\sqrt{13} \text{ (ms}^{-2}\text{)}$ **Given answer**

Or:

First M1 for $F = \sqrt{3^2 + (-2)^2}$ (Allow $\sqrt{3^2 + 2^2}$)

First A1 $F = \sqrt{13}$

Second M1 for $\sqrt{13} = 0.5 a$

Second A1 for $a = 2\sqrt{13} \text{ (ms}^{-2}\text{)}$ **Given answer**

Question (b)

M1 for $(i + 3j) + (2 \times \text{their } a)$

First A1 ft for a correct expression

Second A1 for $13i - 5j$; isw if they go on to find the speed

Question (c)

M1 for $2\sqrt{2^2 + (-1)^2}$ or $\sqrt{4^2 + (-2)^2}$

A1 for $2\sqrt{5}$ or $\sqrt{20}$ or 4.5 or 4.47 or better

Question (d)

M1 for $(i + 3j) + (3.5 \times \text{their } a)$, or possibly, their (b) + (1.5 x their a)

First A1 ft for a correct expression *of form* $ai + bj$

Second A1 for given conclusion reached correctly *e.g.* $22i - 11j = 11(2i - j)$ oe **Given answer**

Q19.

Question Number	Scheme	Marks
(a)	$(4\mathbf{i} - 2\mathbf{j}) + (2\mathbf{i} + q\mathbf{j}) = (6\mathbf{i} + (q - 2)\mathbf{j})$ $6 = 2(q - 2)$ $q = 5$	M1A1 DM1 A1 (4)
(b)	$6\mathbf{i} + 3\mathbf{j} = 1.5\mathbf{a}$ $\mathbf{a} = (4\mathbf{i} + 2\mathbf{j}) \text{ m s}^{-2}$ $\mathbf{v} = \mathbf{u} + \mathbf{a}t = (-2\mathbf{i} + 4\mathbf{j}) + 2(4\mathbf{i} + 2\mathbf{j})$ $= 6\mathbf{i} + 8\mathbf{j}$ $\text{speed} = \sqrt{6^2 + 8^2}$ $= 10 \text{ m s}^{-1}$	M1 A1 M1 A1ft M1 A1 (6) [10]

Notes for Question

Question (a)

First M1 for $(4\mathbf{i} - 2\mathbf{j}) + (2\mathbf{i} + q\mathbf{j})$

First A1 for $(6\mathbf{i} + (q - 2)\mathbf{j})$ (seen or implied)

Second M1, **dependent on first M1**, for using 'parallel to $(2\mathbf{i} + \mathbf{j})$ ' to obtain an equation in q only.

Second A1 for $q = 5$

Question (b)

First M1 for their resultant force $= 1.5\mathbf{a}$

First A1 for $\mathbf{a} = 4\mathbf{i} + 2\mathbf{j}$

Second M1 for $(-2\mathbf{i} + 4\mathbf{j}) + 2 \times (\text{their } \mathbf{a})$ (M0 if force is used instead of $\mathbf{a}$)

Second A1 ft for their velocity at $t = 2$

Third M1 for finding the magnitude of their velocity at $t = 2$

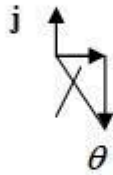
Third A1 for $10 \text{ (ms}^{-1}\text{)}$

N.B. In (b), if they use scalars throughout, M0A0M0A0M0A0

Q20.

Question Number	Scheme	Marks
	$-6\mathbf{i} + \mathbf{j} = \mathbf{u} + 3(2\mathbf{i} - 5\mathbf{j})$ $\Rightarrow \mathbf{u} = -12\mathbf{i} + 16\mathbf{j}$ $\Rightarrow u = \sqrt{(-12)^2 + 16^2} = 20$	M1 A1 A1 cso M1 A1 [5]

Q21.

Question Number	Scheme	Marks
(a)	 $\tan \theta = \frac{2}{1} \Rightarrow \theta = 63.4^\circ$ angle is 153.4°	M1 A1 A1 (3)
(b)	$(4 + p)\mathbf{i} + (q - 5)\mathbf{j}$ $(q - 5) = -2(4 + p)$ $2p + q + 3 = 0 *$	B1 M1 A1 A1 (4)
(c)	$q = 1 \Rightarrow p = -2$ $\Rightarrow \mathbf{R} = 2\mathbf{i} - 4\mathbf{j}$ $\Rightarrow \mathbf{R} = \sqrt{2^2 + (-4)^2} = \sqrt{20}$ $\sqrt{20} = m8\sqrt{5}$ $\Rightarrow m = \frac{1}{4}$	B1 M1 M1 A1 f.t. M1 A1 f.t. A1 cao (7) [14]

Q22.

Question Number	Scheme	Marks
(a)	$\tan \theta = \frac{8}{6}$ $\theta \approx 53^\circ$	M1 A1 (2)
(b)	$\mathbf{F} = 0.4(6\mathbf{i} + 8\mathbf{j}) (= 2.4\mathbf{i} + 3.2\mathbf{j})$ $ \mathbf{F} = \sqrt{(2.4^2 + 3.2^2)} = 4$	M1 M1 A1 (3)
(c)	$\mathbf{v} = 9\mathbf{i} - 10\mathbf{j} + 5(6\mathbf{i} + 8\mathbf{j})$ $= 39\mathbf{i} + 30\mathbf{j} \text{ (ms}^{-1}\text{)}$	M1 A1 A1 (3) (8 marks)

Q23.

Question Number	Scheme	Marks
(a)	$\text{speed} = \sqrt{2^2 + (-5)^2}$ $= \sqrt{29} = 5.4 \text{ or better}$	M1 A1 (2)
(b)	$((7\mathbf{i} + 10\mathbf{j}) - (2\mathbf{i} - 5\mathbf{j}))/5$ $= (5\mathbf{i} + 15\mathbf{j})/5 = \mathbf{i} + 3\mathbf{j}$ $\mathbf{F} = m\mathbf{a} = 2(\mathbf{i} + 3\mathbf{j}) = 2\mathbf{i} + 6\mathbf{j}$	M1 A1 A1 DM1 A1ft (5)
(c)	$\mathbf{v} = \mathbf{u} + \mathbf{a}t = (2\mathbf{i} - 5\mathbf{j}) + (\mathbf{i} + 3\mathbf{j})t$ $(-5 + 3t)\mathbf{j}$ $\text{Parallel to } \mathbf{i} \Rightarrow -5 + 3t = 0$ $t = 5/3$	M1 A1 M1 A1 (4) [11]

Q24.

Question	Scheme	Marks	AOs
(a)	Put $t = 2$ in v and use Pythagoras: $\sqrt{12^2 + (-6\sqrt{2})^2}$	M1	3.1a
	$\sqrt{216}, 6\sqrt{6}$ or 15 or better (m s^{-1})	A1	1.1b
		(2)	
(b)	Differentiate v wrt t to obtain a	M1	3.4
	$6t\mathbf{i} - 3t^{\frac{1}{2}}\mathbf{j}$ oe (m s^{-2}) isw	A1	1.1b
		(2)	
(c)	Integrate v wrt t to obtain r	M1	3.4
	$\mathbf{r} = t^3\mathbf{i} - 4t^{\frac{3}{2}}\mathbf{j} (+C)$	A1	1.1b
	$(\mathbf{i} - 4\mathbf{j}) = 4^3\mathbf{i} - 4 \times 4^{\frac{3}{2}}\mathbf{j} + C$	M1	3.1a
	$(-62\mathbf{i} + 24\mathbf{j})$ (m) isw e.g. if they go on to find the distance.	A1	1.1b
		(4)	
(8 marks)			

Notes: Accept column vectors throughout apart from the answer to (b).

a	M1	Need square root but -ve sign not required. Allow $\mathbf{i}$'s and/or $\mathbf{j}$'s to go missing from their v at $t = 2$, provided they have applied Pythagoras correctly.
	A1	cao N.B. Correct answer with no working can score 2 marks.
b	M1	Both powers decreasing by 1. Allow a column vector. M0 if $\mathbf{i}$ or $\mathbf{j}$ is missing but allow recovery in (b).
	A1	cao. Do not accept a column vector.
c	M1	Both powers increasing by 1 M0 if $\mathbf{i}$ or $\mathbf{j}$ is missing but allow recovery.
	A1	($r =$) not required
	M1	Putting $\mathbf{r} = (\mathbf{i} - 4\mathbf{j})$ and $t = 4$ into their displacement vector expression which must have C (allow C) to give an equation in C only, seen or implied. Must have attempted to integrate v for this mark to be available. N.B. C does not need to be found and <u>this is a method mark, so allow slips.</u>
	A1	cao