

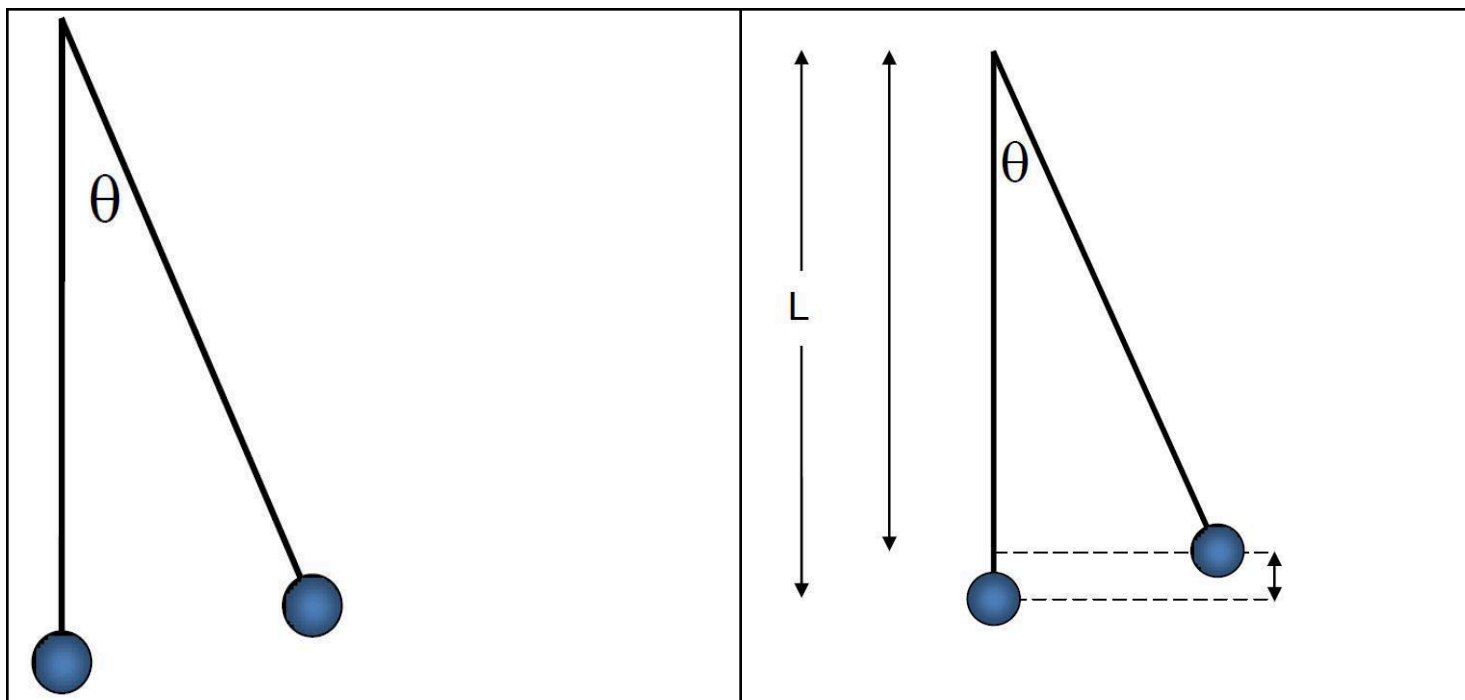
## S.H.M. – Pendulum

### [Instructional Video 1 - 6](#)

#### **(T) Period of a Pendulum**

- Determined by .... \_\_\_\_\_
- Equation \_\_\_\_\_
- Frequency \_\_\_\_\_

Finding the height of a pendulum with a length of  $L$  and an angle  $\theta$  \_\_\_\_\_



**Ex 1)** A pendulum is pulled back at an angle of 10. degrees from the vertical and is released. When the ball reaches the lowest point, it has a velocity of 2.0 m/s.

a) What is the frequency of the pendulum?

### **Example Problems**

1. A simple pendulum oscillates with a period  $T$ . If the mass of the pendulum is doubled what is the new period of the pendulum?

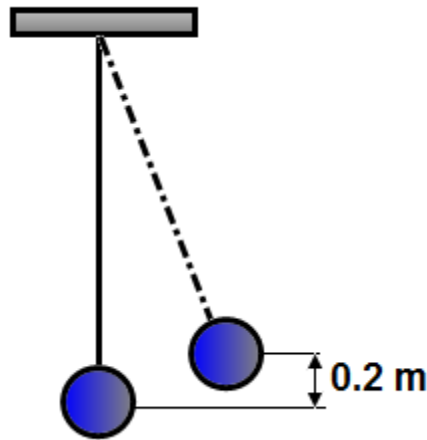
A)  $T/2$       B)  $2T$       C)  $T$       D)  $\sqrt{2} T$       E)  $\frac{T}{\sqrt{2}}$

2. A simple pendulum oscillates with a period  $T$ . If the length of the pendulum is doubled what is the new period of the pendulum?

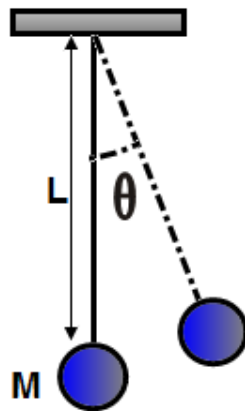
A)  $T/2$       B)  $2T$       C)  $T$       D)  $\sqrt{2} T$       E)  $\frac{T}{\sqrt{2}}$

3. What is the length of a simple pendulum if it oscillates with a period of 2 s?

A) 2.0 m      B) 1.0 m      C) 0.5 m      D) 0.4 m      E) 0.1 m

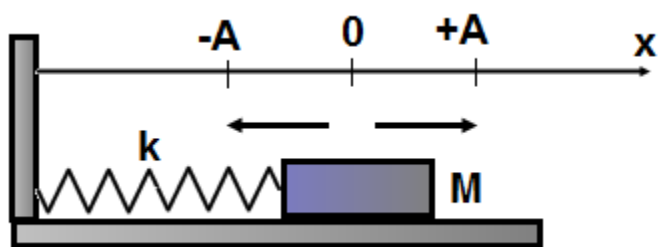


4. A simple pendulum consists of a mass  $M$  attached to a vertical string  $L$ . When the string is displaced to the right the ball moves up by a distance  $0.2\text{ m}$ . When the ball is released from rest what is the maximum speed?
- A)  $1\text{ m/s}$       B)  $2\text{ m/s}$       C)  $3\text{ m/s}$       D)  $4\text{ m/s}$       E)  $5\text{ m/s}$

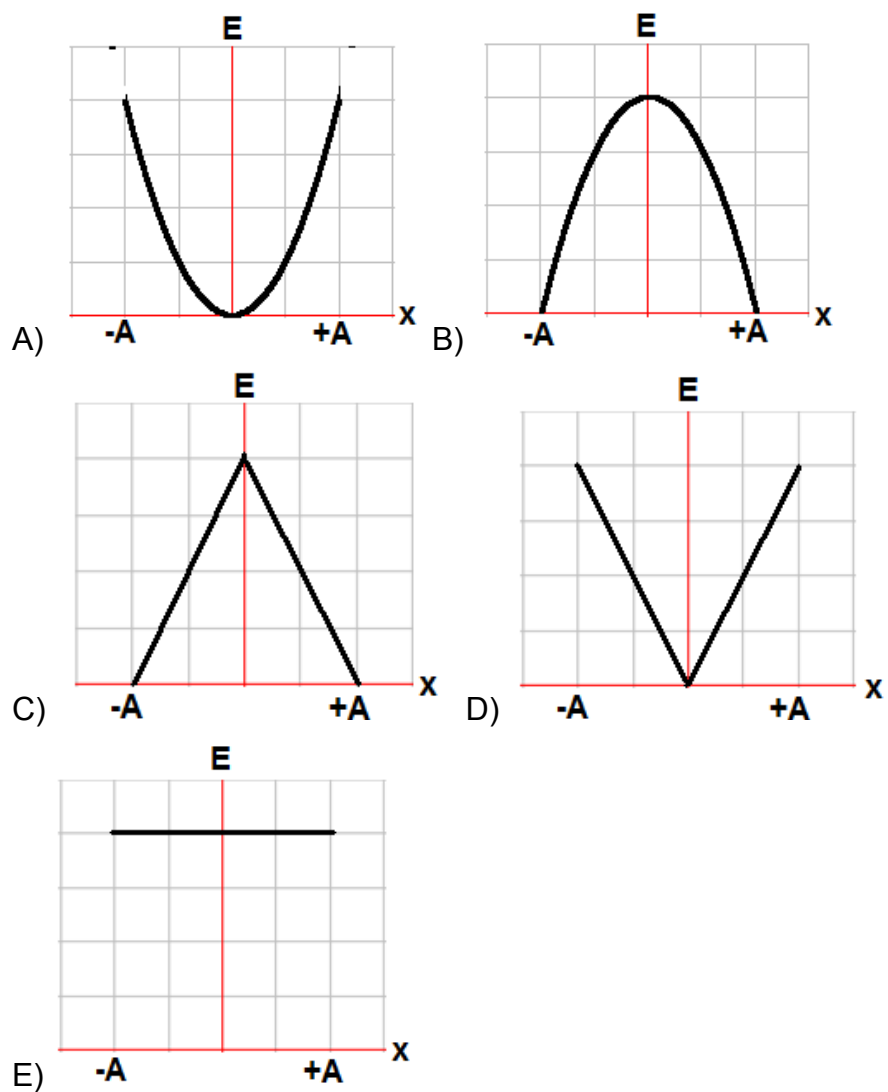


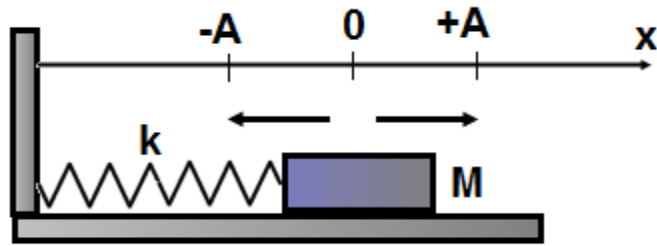
5. A simple pendulum consists of a mass  $M$  attached to a vertical string  $L$ . The string is displaced to the right by an angle  $\theta$ . When the pendulum is released from rest what is the speed of the ball at the lowest point?

- A)  $2\text{ gL}$       B)  $\sqrt{2gL}$       C)  $\sqrt{2mgL}$       D)  $\sqrt{2gL(1 - \cos\theta)}$       E)  $\sqrt{1gL\cos\theta}$

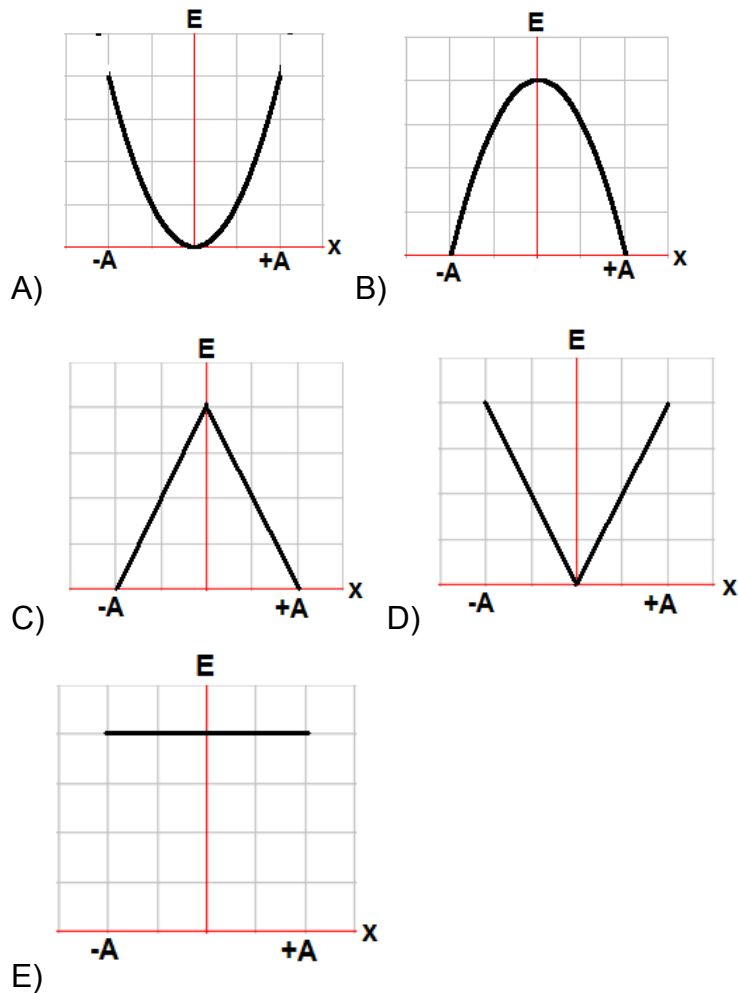


6. A block of mass  $M$  is attached to a horizontal spring  $k$ . The block undergoes SHM with amplitude of  $A$ . Which of the following graphs represents the elastic potential energy as a function of position  $x$ ?





7. A block of mass  $M$  is attached to a horizontal spring  $k$ . The block undergoes SHM with amplitude of  $A$ . Which of the following graphs represents the kinetic energy as a function of position  $x$ ?

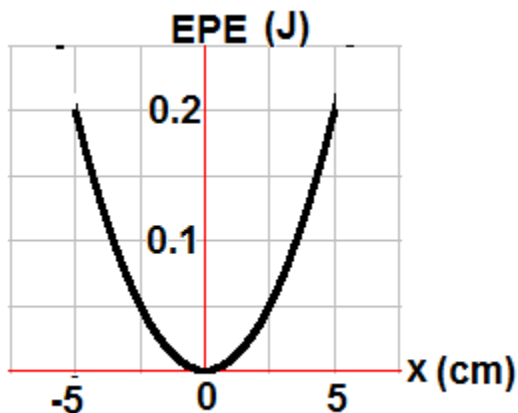


8. A  $0.9 \text{ kg}$  block is attached to an unstretched spring with a spring constant of  $10 \text{ N/m}$ . The block is released from rest. How long does it take for the block to return to its initial position?

- A)  $0.3\pi \text{ s}$       B)  $0.5\pi \text{ s}$       C)  $0.4\pi \text{ s}$       D)  $0.9\pi \text{ s}$       E)  $0.6\pi \text{ s}$

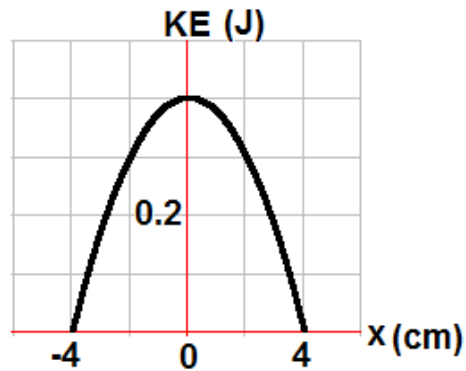
### **Free Response Problems**

1. A 0.4 kg object is attached to a horizontal spring undergoes SHM with the total energy of 0.2 J. The potential energy as a function of position presented by the graph below:

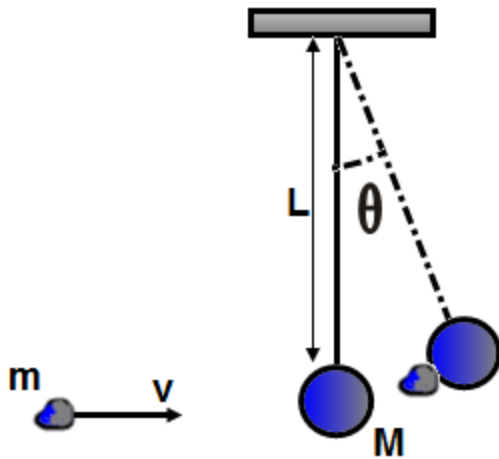


- What is the amplitude of oscillations?
- What is the spring constant? Answer:
- What is the kinetic energy of the system at point  $x = 2.5$  cm?
- Indicate point or points where the kinetic energy equals the potential energy of the system.
- What is the maximum speed of the object?

2. A 0.20 kg object is attached to a horizontal spring undergoes SHM with the total energy of 0.40 J. The kinetic energy as a function of position presented by the graph below:



- What is the maximum displacement from equilibrium?
- What is the maximum speed of the object?
- What is the spring constant?
- Indicate point or points where the kinetic energy equals the potential energy of the system.  
 **$\pm 3$  cm**
- What is the potential energy of the system at point  $x = 2$  cm?

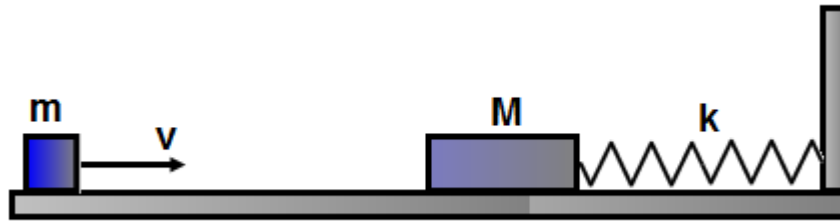


3. A 20. g piece of clay moving at a speed of 50. m/s strikes a 500. g pendulum bob at rest. The length of a string is 0.80 m. After the collision, the clay-bob system starts to oscillate as a simple pendulum.
  - a. What is the speed of the clay-bob system after the collision?
  - b. What is the maximum angular displacement of the pendulum?
  - c. What is the period of the clay-bob oscillating system?
  - d. What is the total energy of the oscillating system?

The pendulum bob makes one complete oscillation and the string breaks at the lowest point.

- e. What is the maximum horizontal distance of the bob when it strikes the floor 0.70 m below?





4. A small block moving with a constant speed  $v$  collides inelastically with a block  $M$  attached to one end of a spring  $k$ . The other end of the spring is connected to a stationary wall. Ignore friction between the blocks and the surface.

**a.** What is the speed of the system of two blocks after the collision?

**b.** What is the amplitude of oscillations of the system of two blocks?

**c.** What is the period of oscillations?

**d.** What is the total energy of the oscillating system?