



CSXX0238: Theory of Learning and Kernel methods

L - T - P – Cr: 2 - 0 - 2 – 3

Pre-requisites: Probability and Statistics, Machine Learning, Programming Knowledge.

Course Objectives:

- Understand the theoretical foundations of machine learning.
- Study formal models of learning, generalization, and hypothesis classes.
- Learn kernel methods and their application in machine learning.
- Understand the interplay between theory and practice in model selection and regularization.

Course Outcomes:

By the end of this course, students will be able to:

1. Understand and evaluate theoretical learning frameworks.
2. Apply empirical risk minimization and structural risk minimization principles.
3. Develop and analyze linear models with various loss functions and regularization techniques.
4. Implement and utilize kernel methods.
5. Explore advanced kernel-based techniques.

CO-PO Mapping

Course Outcomes (COs)	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12
CO1	3	3	2	2	1	–	–	–	–	–	–	2
CO2	3	3	2	2	1	–	–	–	–	–	–	2
CO3	3	3	3	2	2	–	–	–	–	–	–	2
CO4	3	3	3	2	3	–	–	–	–	–	–	2
CO5	2	3	3	3	3	–	–	–	1	1	1	3

Detailed Syllabus

UNIT 1: Foundations of Statistical Learning

Lectures: 05

hrs

Introduction to supervised learning, Hypothesis spaces and inductive bias, Empirical Risk Minimization (ERM), Consistency and generalization, Bias-variance decomposition.

UNIT 2: Theoretical Learning Models

Lectures: 06

hrs

PAC (Probably Approximately Correct) learning, Sample complexity, VC-Dimension and VC-theory
Structural Risk Minimization (SRM), Rademacher complexity, No Free Lunch theorem.

UNIT 3: Linear Models and Regularization

Lectures: 05

hrs

Linear classifiers and regressors, Loss functions: hinge, logistic, squared, Regularization (L1, L2)
Ridge regression and Lasso, Duality and Representer Theorem.

UNIT 4: Kernel Methods and SVM

Lectures: 07

hrs

Kernel trick and feature spaces, Common kernels: linear, polynomial, RBF, sigmoid, Mercer's theorem, SVMs: hard and soft margin, Dual formulation and kernelized SVM, Sequential Minimal Optimization (SMO)

UNIT 5: Advanced Topics and Applications

Lectures: 05

hrs

Kernel PCA, Multiple Kernel Learning (MKL), Graph and string kernels, Applications in NLP, vision, and bioinformatics, Generalization in deep learning (overview), Double descent phenomenon.

Textbooks & References

1. *Understanding Machine Learning: From Theory to Algorithms* by Shai Shalev-Shwartz and Shai Ben-David
2. *Machine Learning with SVM and other kernel methods*, K.P. Soman, R Loganathan, and V. Ajay, PHI publisher.
3. *Learning with Kernels* by Bernhard Schölkopf and Alexander J. Smola
4. *Pattern Recognition and Machine Learning* by Christopher M. Bishop

Research papers on PAC learning, kernel methods, and VC-dimension