

## Motion in a Plane Notes

### **I. 2-Dimensional Motion and Trajectories**

What kinds of objects have a 2-dimensional motion?

- Objects moving along Earth's surface (projectiles)
- Planets around the sun
- Pendulums

A) Objects moving along the Earth's surface (projectiles)

1. Projectile fired horizontally

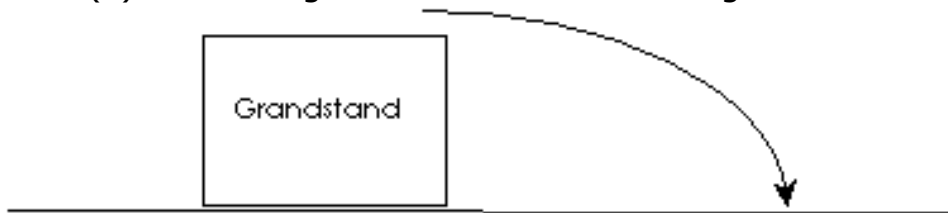
*What you need to know before solving this type of problem:*

### **B) Projectile fired horizontally - Solving Word Problems**

*Use all the same motion equations you used before*

Ex) A baseball is thrown horizontally from a grandstand 20. m above ground at a speed of 10. m/s.

(a) How long will the ball remain in flight before reaching the ground?



(b) What is the projectile's maximum range before it hits the ground?

## Motion in a Plane Notes

### 2. Projectile fired at an angle

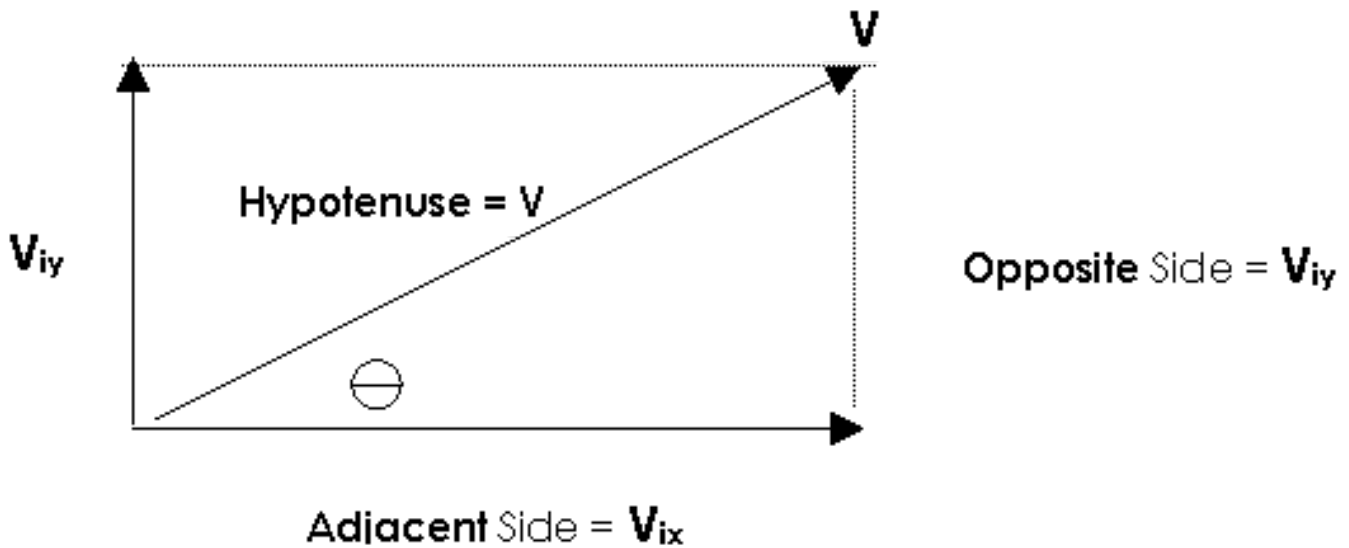
Projectiles move in a \_\_\_\_\_ path

#### Angle and Initial Velocities

Projectile fired at 5 m/s: if  $\theta = 0$  \_\_\_\_\_ if  $\theta = 90$  \_\_\_\_\_

If the angle not 0 or 90 the initial velocity is \_\_\_\_\_

#### Finding the horizontal and vertical components parts



$V$  - \_\_\_\_\_ that projectile is fired

$V_{ix}$  - initial  $V$  in \_\_\_\_\_ direction

$V_{iy}$  - initial  $V$  in \_\_\_\_\_ direction

$V_x =$  \_\_\_\_\_  $V_y =$  \_\_\_\_\_

Ex) A baseball is thrown upward at an angle of  $30.^\circ$  and a velocity of 6.0 m/s.

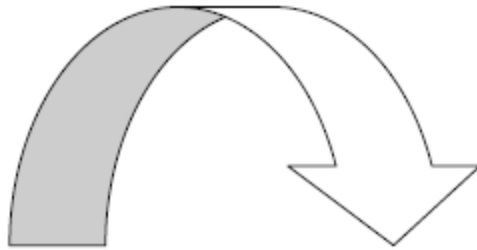
Find the initial horizontal & vertical components of the baseball's velocity.

### 3. Other important facts about projectile motion

$$d_x = V_x t \text{ (memorize)}$$

$$a_y = \text{_____} \text{ ascending}$$

$$a_y = \text{_____} \text{ descending}$$



#### Angles and Ranges

Max Range \_\_\_\_\_ Minimum Range \_\_\_\_\_

What angle would have the same Range as 55 degrees? \_\_\_\_\_

Angle with the longest time in the air? \_\_\_\_\_

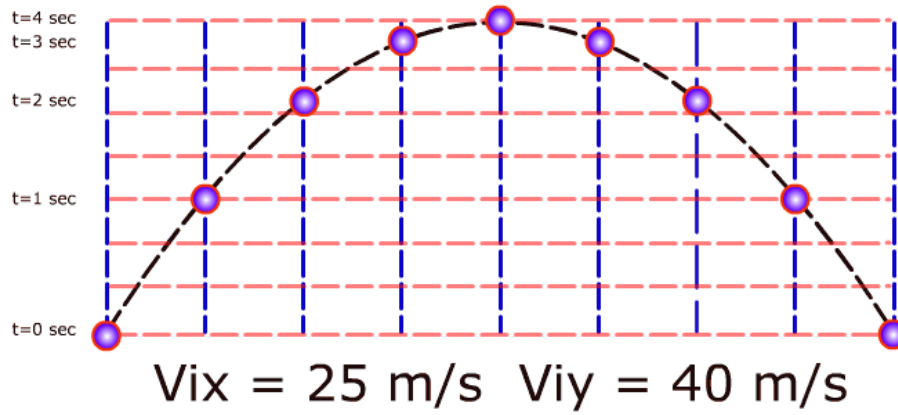
**Ex)** Which projection angle causes a projectile to stay in the air longer?

50 or 70 degrees? Why?

## Motion in a Plane Notes

### **Projectile projected upward at an angle.**

Where  $V_{ix} = 25 \text{ m/s}$   $V_{iy} = 40 \text{ m/s}$



t (sec)	$V_x$ (m/s)	$V_y$ (m/s)
0	25	40
1		
2		
3		
4		
5		
6		
7		
8		

## Motion in a Plane Notes

### 4. Projectile Fired at an Angle - Word Problems

**Ex)** An athlete doing a running jump leaves the ground at an angle of  $25^\circ$  and a velocity of 10. m/s.

**(a)** What is the athlete's velocity's initial vertical component ( $V_{iy}$ )?

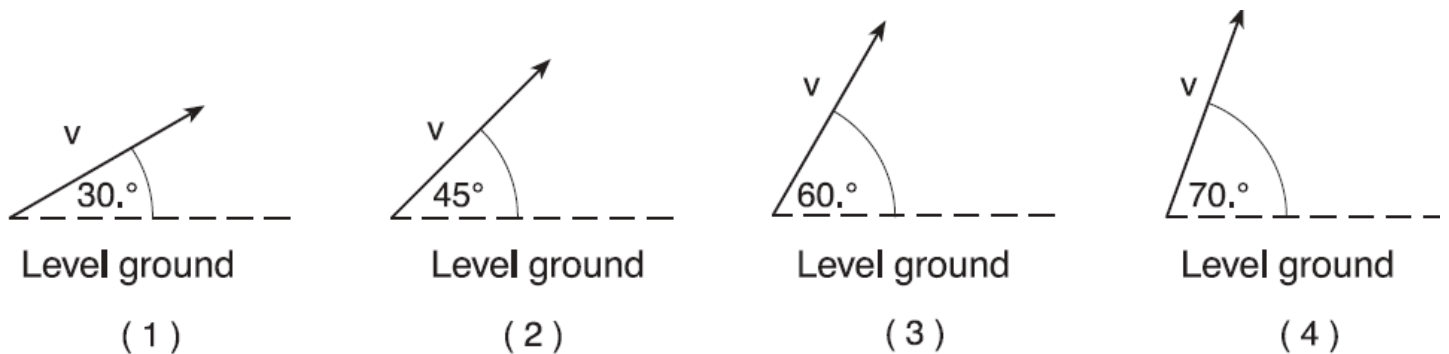
**(b)** How long does it take for the athlete to reach her maximum height?

**(c)** How long did it take for the athlete to complete the entire jump? \_\_\_\_\_

Total time equals \_\_\_\_\_

**(d)** How far did she jump?

**Ex)** Rank the horizontal displacements from **least to greatest**.



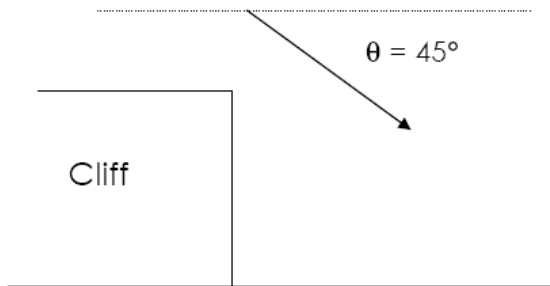
## Motion in a Plane Notes

**Ex)** A projectile leaves the ground at an angle of  $60^\circ$  and a speed of 100. m/s.

**(a)** Find the initial vertical component of the object's velocity

**(b)** Find the object's maximum height.

**Ex)** A rock is thrown from a cliff with an initial speed of 40m/s at an angle of  $45^\circ$  below the horizontal.



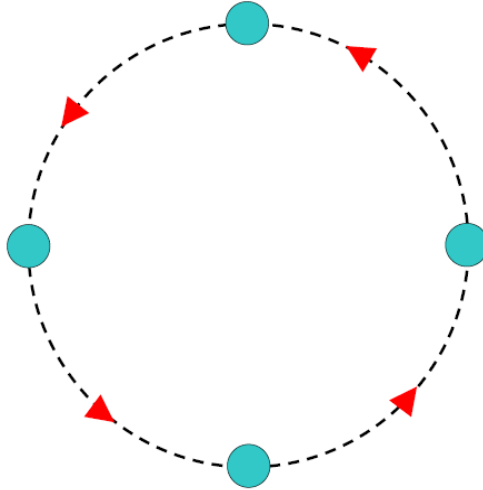
**(a)** What is the vertical component of the initial velocity?

**(b)** If the rock strikes the ground in 1.0 sec what is the height of the cliff?

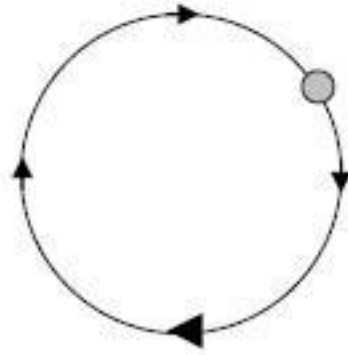
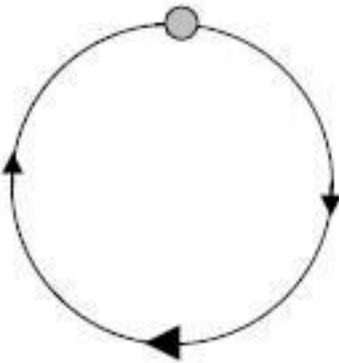
## Motion in a Plane Notes

### **I. Uniform Circular Motion**

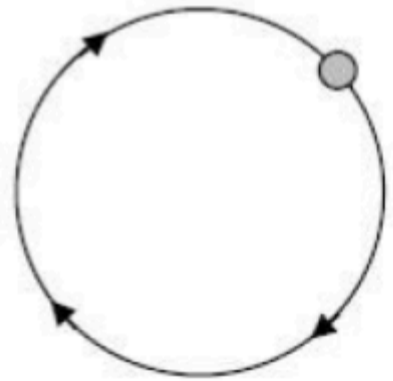
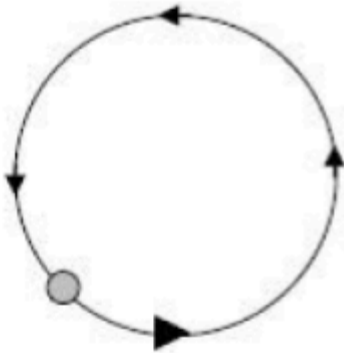
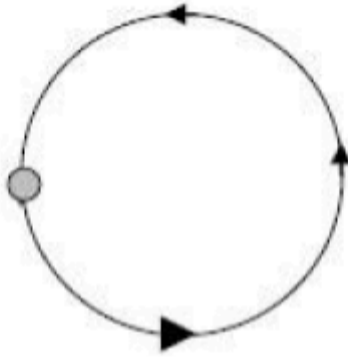
For an object to move at constant speed in a circle, an outside \_\_\_\_\_ must constantly pull the object toward \_\_\_\_\_ of a circular path.



- 1.** Draw the centripetal force on each sphere   **2.** Draw the tangential velocity



## Motion in a Plane Notes



[Instructional Video](#)



## Motion in a Plane Notes

### **A. The Equations and Vectors**

1. \_\_\_\_\_ (ac) –

Mass moving with circular motion.

a Equation: \_\_\_\_\_ (On reference table)

Units

a) (v) \_\_\_\_\_ velocity - \_\_\_\_\_

to circle, in the direction of the motion

b) \_\_\_\_\_ acceleration - directed toward the

\_\_\_\_\_ of the circle

### **Example Problem**

**Ex)** A car moving in a circular path with a radius of 2.0 m has a velocity of 8.0 m/s. What is the centripetal acceleration of this car?

**B. Different ways we can change centripetal acceleration**

1. How does acceleration change with velocity?

$$a_c = v^2/r$$

.. \*\*\*Answer - \_\_\_\_\_ Relationship  
(Both variables on top, one is squared)

V	ac
X2	X
X3	X
X4	

1. How does acceleration change with the radius of the circle?

.. \*\*\* Answer - \_\_\_\_\_ Relationship

ac	R
X	X2
X	X3
	X4

**C. More Circular Motion Word Problems**

**Example:** A 2 kg cart travels in a horizontal circle at a constant speed of 6m/s. If the radius of the circle is 3m, what is the centripetal acceleration?

Equation:

**Challenge Example:** Calculate the speed an earth satellite must have to enter a circular orbit at an altitude of 200 km where the acceleration due to gravity at 200,000 m is  $9.2 \text{ m/s}^2$  and the radius of the earth is 6,400,000 m

## Motion in a Plane Notes

Centripetal Force ( $F_c$ ) - \_\_\_\_\_ directed toward \_\_\_\_\_

which keeps an object moving in a \_\_\_\_\_ path

$$F_c = ma_c =$$

Force units (\_\_\_\_\_) or

Ex) A 5.0 kg object moves in a circle at a constant speed of 10. m/s. What is the radius of the object's circular path if the object's centripetal force is 1000. Newtons?

### **D. Changing the Centripetal Force**

1. How does centripetal force change with mass?

m	$F_c$
X2	X
X3	X
	X4

2. How does centripetal force change with radius?

.. \_\_\_\_\_ Relationship (One variable on top, other on bottom)

$F_c$	r
X	X2
X	X3
	X4

## Motion in a Plane Notes

3. How does centripetal force change with velocity?

\_\_\_\_\_ Relationship (Both variables on top, one is squared)

v	F <sub>c</sub>
X <sup>2</sup>	X
X <sup>3</sup>	X
X <sup>4</sup>	

## Motion in a Plane Notes

### **I. Satellite Motion**

Satellite - \_\_\_\_\_

Natural Satellites - ex) Moon, all 8 planets, comet

Artificial Satellites - weather, spy, communications

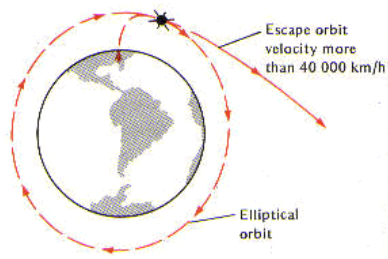
#### **A. Satellite Motion**

1. To send artificial satellite \_\_\_\_\_

around the earth, it must first achieve a speed of \_\_\_\_\_

- If greater than 7900 m/s satellite has an \_\_\_\_\_ orbit
- If velocity is greater than 11 km/s then the satellite \_\_\_\_\_

#### **Escape Velocity**



2. Air resistance slows down satellites and \_\_\_\_\_

#### **B. Geosynchronous Orbits -**

- A.** When a satellite orbits \_\_\_\_\_ with the earth's rotation it is called \_\_\_\_\_.
- B.** Time for one revolution - \_\_\_\_\_
- C.** A satellite at a distance of \_\_\_\_\_ from Earth's center will orbit the Earth every \_\_\_\_\_ hrs.
- D.** Since both satellite and Earth \_\_\_\_\_