

Data Analysis In-Class Worksheet #14: Logistic Regression

Student Name _____ Section ☐ 1 ☐ 2

Part #1: Logistic Regression Fundamentals

What does the “odds” measure? _____

If the probability of winning a 30% coupon at Kohl’s is 10%, then what’s the odds of winning a 30% coupon? _____

$\log_{10}(10000) = \underline{\hspace{2cm}}$

Why do we need to use $\log(\text{odds})$, not probabilities, in estimating logistic regression?

Reason #1: _____

Reason #2: _____

Suppose we have this logistic regression model.

$$\hat{Y} = 2 + 1 * \text{BED}$$

If $\text{BED} = 3$, then $\hat{Y} = \underline{\hspace{2cm}}$

$\hat{Y}$ is ☐ probability ☐ odds ☐ $\ln(\text{odds})$

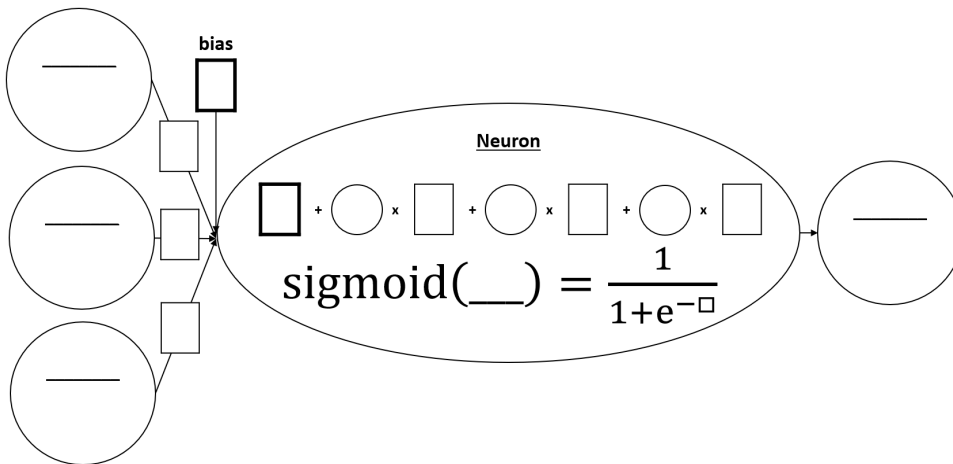
Convert $\hat{Y}$ back into probability using the _____ function = _____ = _____
(Reminder: You can use the formula set up in Google Sheets to compute the value.)

Why do we need to convert $\hat{Y}$ back into probability?

Make a binary decision using the probability:

Convert any probability $> .5$ into YES, and any probability $\leq .5$ into NO. The decision is _____.

Illustrate this logistic regression model as a deep learning neuron with a sigmoid unit:



Part #2: Logistic Regression Application

Does Property Age predict the Property's Zipcode Location?

To answer this question, we can rephrase it as a pair of hypotheses:

H_0 : _____

H_1 : _____

Express these hypotheses in terms of the regression β_1 slope

H_0 : _____

H_1 : _____

For H_0 : $\hat{Y} =$ _____

For H_1 : $\hat{Y} =$ _____

In our class dataset, Zipcode has only two possible outcomes: 23185 and 23188. Therefore, Zipcode is a _____ variable.

- ☐ Binary (categorical)
- ☐ Numeric

If the probability (p) of being in 23185 is 80%, then the probability of being in 23188 would be ____%. The odds of being in 23185 would be ____ / ____ = _____. The natural log of this odds is _____

If the probability (p) of being in 23185 is 50%, then the probability of being in 23188 would be ____% The odds of being in 23185 would be ____ / ____ = _____. The natural log of this odds (ln(odds)) is _____

Coefficients

	Estimate	Standard Error	z	Wald Test		
				Wald Statistic	df	p
(Intercept)	0.152	0.327	0.466	0.217	1	0.641
Age	-0.029	0.011	-2.532	6.412	1	0.011

Note. Zipcode level '23188' coded as class 1.

$$\hat{Y} = \text{_____} + \text{_____} * \text{Age}$$

The predicted value ($\hat{Y}$) from a logistic regression is

- ☐ Probabilities
- ☐ Binary categories
- ☐ Odds
- ☐ Natural log of odds (ln(odds) or logit)

The intercept is _____, which tells us _____

The slope is _____, which tells us _____

When a property is a year older, its odds of being in 23188 (Class 1) would _____

Abdullah's $\hat{Y} = 0.429$. Convert it into odds: _____

Convert odds into probability value: _____

Use the probability value to predict if the property is in 23185 or 23188:

Abdullah's property is located in 23188.

This is a ☐ correct ☐ incorrect prediction.

If we get a confusion matrix like this one, calculate the overall accuracy rate:

		Predicted	
		23185	23188
Actual	23185	4	6
	23188	16	24

APA Writeup

A logistic regression was performed to ascertain the effect of _____ on the likelihood of _____. The logistic regression model was statistically (in)significant, χ^2 (____) = _____, p _____, McFadden's R^2 = _____. The model correctly classified _____% of cases.