## PSN COLLEGE OF ENGINEERING AND TECHNOLOGY



(An Autonomous Institution, Affiliated to Anna University, Chennai) Approved by AICTE and Recognized by UGC Under section 2 (f), 12 (B)



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## DEPARTMENT OF MECHANICAL ENGINEERING

## **Question Bank / End Semester Examinations, October / November 2023**

Year & Sem	IV Yr & VII Sem	Branch	B.E. Mechanical Engineering
<b>Course Code</b>	510023	Course Name	Finite Element Analysis
Regulation	2018	Academic Year	2023 – 24 (Odd)

Course Outcomes (COs): At the end of the course, the student will be able to

**CO1**: Apply the numerical methods to formulate the simple finite element problems.

CO2: Apply one dimensional finite element method to solve bar, beam and truss type Problems

**CO3:** Apply finite element method for plane stress, plane strain and axis symmetric conditions.

**CO4:** Identify temperature distribution of one- and two-dimensional heat transfer problems using one- and two-dimensional finite elements.

**CO5:** Apply the numerical methods to formulate the higher order and isoperimetric problems.

**BL** – Bloom's Level (1- Remembering, 2- Understanding, 3 – Applying, 4 – Analysing, 5 – Evaluating, 6 - Creating); **CO** – Course Outcome;

	Unit I: INTRODUCTION TO FINITE ELEMENT ANALYSIS					
Q. No.	Part – A (2 Marks)	Marks	СО	BL		
1	Classify boundary conditions.	2	CO1	1		
2	Name the weighted Residual methods.	2	CO1	1		
3	State the method of engineering analysis.	2	CO1	1		
4	What are the limitations of using a finite difference method?	2	CO1	1		
5	What is Galerkin method of approximation?	2	CO1	1		
6	Mention the basic steps of Reyleigh – Ritz method.	2	CO1	1		
7	List the different types of nodes.	2	CO1	1		

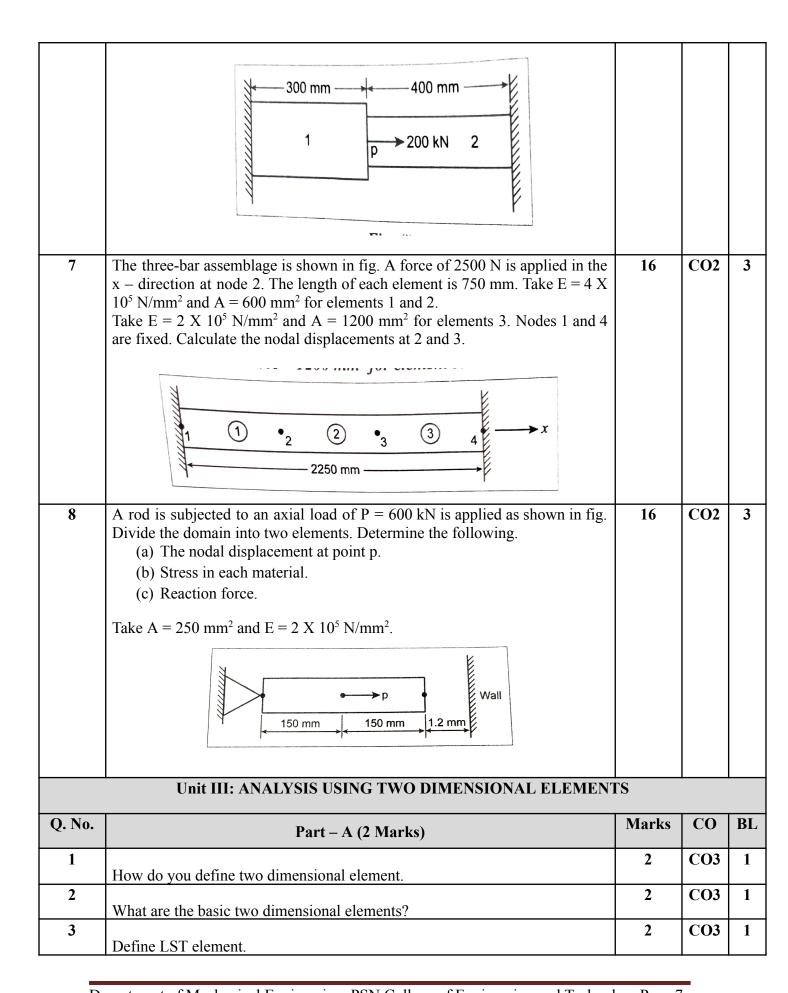
8		2	CO1	1
9	What is the basis of finite element method?	2	CO1	1
	Name the variational methods.	2	COI	1
10	What is interpolation function?	2	CO1	1
11	Why are polynomial type of interpolation function preferred over	2	CO1	1
	trigonometric functions?			
12	Name the FEA software's.	2	CO1	1
13	List the variational methods.	2	CO1	1
14	State the three phases of finite element method.	2	CO1	1
15	Write the advantages and disadvantages of FEA.	2	CO1	1
Q. No.	Part – B (16 Marks)	Marks	CO1	BL
1	The following differential equation is available for a physical phenomenon	16	CO1	1
	$AE \frac{d^2y}{dx^2} + q_0 = 0$ with boundary conditions y (0) = 0 and $\frac{dy}{dx} = 0$			
	Find the value of $f(x)$ using weighted residual method.			
2	The governing differential equation for the fully developed laminar is given	16	CO1	1
	by $\mu \frac{d^2y}{dx^2} + \rho g \cos\Theta = 0$			
	If boundary conditions $\frac{dy}{dx}$ ] <sub>x=0</sub> = 0 u (L) = 0.			
	Find the velocity distribution $u(x)$ .			
3	The following differential equation is available for a physical phenomenon.	16	CO1	1
	$\frac{d^2u}{dx^2} + 50 = 0, \ 0 \le x \le 20$			
	The trail function is $y = a \times (x - 10)$			
	Boundary conditions are $y(0) = 0$ y(10) = 0			
	find the value of 'a' by the following methods. (i). Point Collocation; (ii).			
4	Subdomain collocation.  The differential equation of a physical phenomenon is given by,	16	CO1	3
	$\frac{d^2u}{dx^2} + 500x^2 = 0, \ 0 \le x \le 1$			
	Boundary conditions are $y(0) = 0$			
	y(1) = 0 Calculate the value of the parameter $a_1$ by the following methods: (i). Point Collocation; (ii). Least Squares			
5	Find the solution for the following differential equation	16	CO1	1
	$EI\frac{d^4y}{dx^4} - q_0 = 0.$			
	The boundary conditions $u(0) = 0$ and $\frac{du}{dx}(0) = 0$			

	$J^2$ $J^3$			
	$\frac{d^{2}u}{dx^{2}}(L) = 0  \frac{d^{3}u}{dx^{3}}(L) = 0$			
6	The following differential equation is available for a physical phenomenon. $\frac{d^2u}{dx^2} + 50 = 0, \ 0 \le x \le 10$ The trail function is $y = a_1 x (10 - x)$ . Boundary conditions are $y (0) = 0$	16	CO1	1
7	y (10) = 0 find the value of 'a1' by the following methods. (i). Point Collocation; (ii). Subdomain collocation; (iii). Least squares; (iv). Galerkin. The following differential equation is available for a physical phenomenon.	16	CO1	1
,	$\frac{d^2u}{dx^2} + 100 = 0, \ 0 \le x \le 10$ Boundary conditions are $y(0) = 0$ $y(10) = 0$ find the value of 'a1' by the following methods. (i). Point Collocation; (ii). Subdomain collocation; (iii). Least squares; (iv). Galerkin.	10		-
8	The differential equation of physical phenomenon is given by $\frac{d^2y}{dy^2} + 500x^2 = 0, \ 0 \le x \le 1$ By using trial function, $y = a_1(x - x^3) + a_2(x - x^5)$ , calculate the value of the parameters $a_1$ and $a_2$ by using any two weighted residual method.	16	CO1	3
	A bar of uniform cross section is clamped at one end and left free at the other end and is subjected to a uniform load 'P' axially as shown in figure. Calculate the displacement and stresses in the bar using two terms polynomial.  Load, P $x = 0$			
9	A bar of uniform cross section is clamped at one end and left free at the other end and is subjected to a uniform load 'P' axially as shown in figure. Calculate the displacement and stresses in the bar using three terms polynomial.  Load, P $x = 0$			3
	Unit II: ANALYSIS OF ONE DIMENSIONAL ELEMENTS			

Q. No.	Part – A (2 Marks)	Marks	СО	BL
1	What are the types of problems treated as one dimensional problem?	2	CO2	1
2	Define normal mode.	2	CO2	1
3	List the types of dynamic analysis.	2	CO2	1
4	List out the properties of stiffness matrix.	2	CO2	1
5	Why are the polynomial terms are preferred for shape functions in finite element method?	2	CO2	1
6	Define shape function.	2	CO2	1
7	Write the shape function for one dimensional 2 noded element.	2	CO2	1
8	Write down the general finite element equation.	2	CO2	1
9	Determine the element mass matrix for one dimensional dynamic structural analysis problem. Assume two noded linear element.	2	CO2	1
10	What is meant by dynamic analysis?	2	CO2	1
11	Draw the shape function of a two noded line element.	2	CO2	1
12	Write the expression for stiffness matrix for truss element.	2	CO2	1
13	State the assumptions made while finding the force in a truss.	2	CO2	1
14	Write the stiffness matrix equation for 1 – D heat conduction element.	2	CO2	1
15	Name the boundary conditions involved in any heat transfer analysis.	2	CO2	1
Q. No.	Part – B (16 Marks)	Marks	СО	BL
1	One dimensional bar is shown in fig. Cross sectional area of the bar is 750 mm² and young's modulus is 2 X $10^5$ N/mm². If $u_1 = 0.5$ mm and $u_2 = 0.625$ , calculate the following:  (i). Displacement at point 'P' (ii). Stress ' $\sigma$ ' (iii). Strain 'e' (iv). Element Stiffness Matrix (K) and Strain Energy (U)	16	CO2	3
2	A steel bar of uniform length 800 mm is subjected to an axial load of 3 kN as shown in fig. calculate the elongation of the bar, neglecting self-weight.	16	CO2	3

	800 mm 3 kN			
3	A thin plate of uniform thickness 25 mm is subjected to a point load of 420 N at mid-point as shown in fig. the plate is also subjected to self-weight. If young's modulus E = 2 X 10 <sup>5</sup> N/mm <sup>2</sup> and unit weight density = 0.8 X 10 <sup>4</sup> N/mm <sup>3</sup> . Calculate  i. Displacement at each nodal point.  ii. Stresses in each element.	16	CO2	3
4	Consider a taper steel plate of uniform thickness, $t = 25$ mm as shown in fig. The Young's modulus of the plate $E = 2 \times 10^5 \text{ N/mm}^2$ and weight density, $\rho = 0.82 \times 10^{-4} \text{ N/mm}^3$ . In addition to its self-weight, the plate is subjected to a point load $p = 100 \text{ N}$ at its mid-point. Calculate the following by modelling the plate with two finite elements:  (i). Global force vector $\{F\}$ (ii). Global stiffness matrix $[K]$ (iii). Displacements in each element.  (v). Reaction force at the support	16	CO2	3

	150 mm  300 mm			
5	For a tapered plate of uniform thickness, $t=15$ mm as shown in fig. find the displacements at the nodes by forming into two element model. The bar has a mass density $\rho=7800$ kg/m³, Young's modulus of the plate $E=2$ X $10^5$ MN/m². In addition to its self-weight, the plate is subjected to a point load $p=10$ kN at its centre. Also find the reaction force at the support.	16	CO2	3
6	Consider a bar as shown in fig. an axial load of 200 kN is applied at point p. take A <sub>1</sub> = 2400 mm <sup>2</sup> , E <sub>1</sub> = 70 X 10 <sup>9</sup> N/mm <sup>2</sup> , A <sub>2</sub> = 600 mm <sup>2</sup> , E <sub>2</sub> = 200 X 10 <sup>9</sup> N/m <sup>2</sup> . Calculate the following:  (a) The nodal displacement at point p.  (b) Stress in each material.  (c) Reaction force.	16	CO2	3



4	What is CST element?	2	CO3	1
5		2	CO3	1
6	What is QST element?  What is meant by plane stress analysis?	2	CO3	1
7	Define plain strain analysis.	2	CO3	1
8	Write a displacement funtion agaution for CST element	2	CO3	1
9	Write a displacement funtion equation for CST element.	2	CO3	1
10	Write down the stress extrain relationship matrix for plane stress and displacement.	2	CO3	1
11	Write down the stress – strain relationship matrix for plane stress condition.	2	CO3	1
12	Write down the stress – strain relationship matrix for plane strain condition.  Write down the stiffness matrix equation for two dimensional CST element.	2	CO3	1
13	What are the difference between 2 dimensional scalar variable and vector	2	CO3	1
14	variable elements?	2	CO3	1
15	Differentiate CST and LST element.  What do you mean by axisymmetric element?	2	CO3	1
	what do you intail by axisymmetric element?			l I
Q. No.	Part – B (16 Marks)	Marks	СО	BL
Q. No.		Marks 16		
	For the constant strain triangular element (CST) shown in fig. Assemble strain – displacement matrix. Take $t = 20 \text{ mm}$ and $E = 2 \times 10^5 \text{ N/mm}^2$ .		СО	BL

	(50, 120) (20, 30) (80, 30)			
3	Calculate the element stresses $\sigma_x$ , $\sigma_y$ , $\tau_{xy}$ , $\sigma_1$ and $\sigma_2$ and the principle angle $\Theta_P$ for the element shown in fig.  Nodal displacements are $u_1 = 2.0 \text{ mm}$ , $v_1 = 1.0 \text{ mm}$ , $u_2 = 0.5 \text{ mm}$ , $v_2 = 1.0 \text{ mm}$ , $u_3 = 2.0 \text{ mm}$ and $v_3 = 1.0 \text{ mm}$ . take $E = 2.1 \times 105 \text{ N/mm2}$ and $\gamma = 0.25$	16	CO3	3
4	For the plane strain element shown in fig, the nodal displacements are $u_1 = 0.005$ mm; $v_1 = 0.002$ mm, $u_2 = 0.0$ mm; $v_2 = 0.0$ mm, $u_3 = 0.005$ mm; $v_3 = 0.0$ mm. Determine the element $\sigma_x$ , $\sigma_y$ , $\tau_{xy}$ , $\sigma_1$ and $\sigma_2$ and the principle angle $\Theta_P$ . Let $E = 70$ GPa and $\gamma = 0.3$ and use unit thickmess for the plane strain. All coordinates are in millimeters.	16	CO3	4
5	For the triangular element shown in fig., obtain strain displacement relation matrix [B] and dertemine the strains $e_x$ , $e_v$ and $\tau_{xv}$ .	16	CO3	4

6	Nodal displacements are $u_1 = 0.001$ mm; $v_1 = -0.004$ mm, $u_2 = 0.003$ mm; $v_2 = 0.002$ mm, $u_3 = -0.002$ mm; $v_3 = 0.005$ mm. All coordinates are in millimeteres.  Calculate the element stiffness matrix and the temperarure force vector for the plane stress element shown in fig. the element exleriences a $20^{0}$ C increase in temperature. Assume coefficient of thermal expansion as $6X10^{-6}/^{0}$ C.  Take, Young's modulus, $E = 2X105$ N/mm2 Poission's ratio $\gamma = 0.25$ and	16	CO3	3
	Thickness t = 5 mm.  Unit IV: DYNAMIC ANALYSIS			
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Q. No	Part – A (2 Marks)	Marks	CO	BL
1	Define frequency of vibration and domning ratio	2	CO4	1
<del>-</del>	Define frequency of vibration and damping ratio.	2	CO4	1
2				
	Define longitudinal vibration and tranverse vibration.	2	COA	1
3	Define longitudinal vibration and tranverse vibration.  Define magnification factor.	2	CO4	1
	Define magnification factor.	2	CO4	1
3				

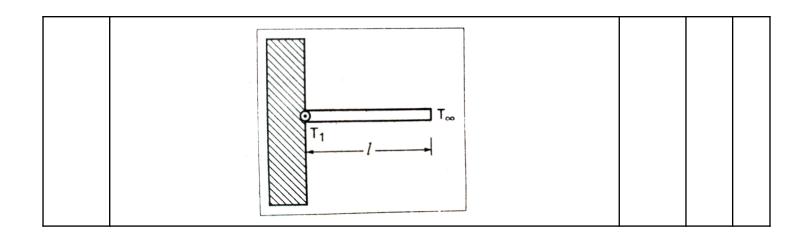
7	Write down the expression for tranverse vibration for beam element.	2	CO4	1
8	What are th types of Eigen value problems?	2	CO4	1
9	Define dynamic analysis.	2	CO4	1
10		2	CO4	3
11	What are the methods used for solving transient vibration problems?  Write down the equation for undamped system of Direct Integration Method	2	CO4	1
12	in central difference method.  State the difference between direct and iterative methods for solving system	2	CO4	1
13	Define linear independence and independence of vectors.	2	CO4	1
14	Show that the matrix A = is orthogonal.	2	CO4	1
15	Prove that the vectors (1, 4, -2), (-2, 1, 3) and (-4, 11, 5) are linearly dependent.	2	CO4	1
Q. No.	Part – B (16 Marks)	Marks	СО	BL
2	and cross section area A, determine the first two frequencies using lumped mass matrix.  Consider a uniform cross section bar shown in figure of length "L" made up of a material whose young's modulus and density are given by E and $\rho$ .	16	CO4	5
	Estimate natural frequencies of axial vibration of the bar using lumped mass matrix			
3	For the bar shown in figure with 2L, modulus of elasticity E, mass density $\rho$ , and cross section area A, determine the first two frequencies using consistent mass matrix.	16	CO4	4

	2 L			
4	Consider a uniform cross section bar shown in figure of length "L" made up of a material whose young's modulus and density are given by E and ρ. Estimate natural frequencies of axial vibration of the bar using consistent mass matrix	16	CO4	5
5	Consider a simply supported beam shown in figure. Let the length $L=1$ m, $E=2 \times 10^{11}$ N/m², Area of cross section $A=30$ cm², Moment of inertia $I=100$ mm⁴, Density = $7800$ kg/m³. Determine the natural frequency using the lumped mass matrix.	16	CO4	4
6	Determine the natural frequency of vibration using lumped mass matrix for a beam fixed at both ends as shown in figure. The beam has mass density of ρ, modulus of elasticity E, cross sectional area A, moment of inertia I. For simplicity of the long hand calculation, beam is discretized into two elements of length "L".	16	CO4	4

Q. No	Part – A (2 Marks)	Marks	СО	BL
1	List the different modes of heat transfer.	2	CO5	1
2	Write down the stiffness matrix equation for the on edimensional heat conduction element.	2	CO5	1
3	Write down the expression of shape funtion N and temperature funtion T for one dimensional heat conduction element.	2	CO5	1
4	Write down the finite element equation for one dimensional heat conduction with free end convection.	2	CO5	1
5	Write down the governing equation for two dimensional heat conduction.	2	CO5	1
6	Write down the shape function for two dimensional heat transfer.	2	CO5	1
7	Write down the stiffness matrix in two dimensional heat conduction and convection.	2	CO5	1
8	Define element capacitance matrix for unsteady state heat transfer problems.	2	CO5	1
9	Write analogies between structural and heat transfer.	2	CO5	1
10	What is steady state heat transfer and write its governing equation.	2	CO5	1
11	Write down the governing equation for two dimensional steady state heat conduction.	2	CO5	1
12	Write down thw expression for governing equation in 2 -D fluid mechanics.	2	CO5	1
13	Write down thw expression for shape function for 2 -D fluid mechanics.	2	CO5	1
14	Write down thw expression for stiffness matrix in 2 -D fluid mechanics.	2	CO5	1
15	Write down thw expression for velocity gradient in fluid mechanics.	2	CO5	1
Q. No.	Part – B (16 Marks)	Marks		BL
1	A wall of 0.75 m thickness having thermal conductivity of 2.2 W/m K. The wall is to be insulated with a material of thickness 1 m having an average thermal conductivity of 0.5 W/m K. The inner surface temperature is 900°C and outside of the insulation is exposed to atmospheric air at 30°C with heat transfer coefficient of 40 W/m² K. Calculate the nodal temperatures.	16	CO5	3

			_	
	Conduction — Convection  Wall Insulation $T_1$ $T_2$ $T_3$ $T_{\infty}$ $T_1$ $T_2$ $T_3$ $T_{\infty}$			
2	A wall of 0.6 m thickness having thermal conductivity of 1.2 W/m K. The wall is to be insulated with a material of thickness 0.06 m having an average thermal conductivity of 0.3 W/m K. The inner surface temperature is $1000^{\circ}$ C and outside of the insulation is exposed to atmospheric air at $30^{\circ}$ C with heat transfer coefficient of 35 W/m <sup>2</sup> K. Calculate the nodal temperatures.	16	CO5	3
3	A wall of 0.5 m thickness having thermal conductivity of 6 W/m K. The wall is to be insulated with a material of thickness 0.1 m having an average thermal conductivity of 0.3 W/m K. The inner surface temperature is 1200°C and outside of the insulation is exposed to atmospheric air at 30°C with heat transfer coefficient of 40 W/m² K. Calculate the nodal temperatures.	16	CO5	3
4	A furnace wall made up of three layers, inside layer with thermal conductivity 8.5 W/m K, the middle layer with conductivity 0.25 W/m K, the outer layer with conductivity 0.08 W/ m K. The respective thickness of the	16	CO5	4

CO5	16
	16



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